早期宇宙與基礎物理

Toy Story



高文芳

交大物理所

Stardate: 1120120403

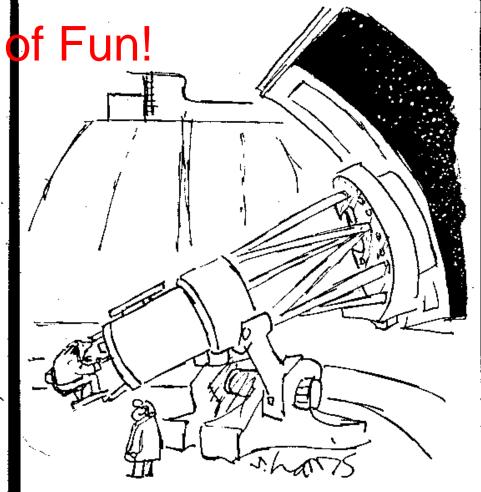
http://web.it.nctu.edu.tw/~wfgore/physics21.

ppt



Popular Science of Fun!

The universe will either continue expanding at its present rate, expand at a slower rate, or it will begin to contract. None of this, however, can account for the fact that it sometimes takes four days to get a letter from Chicago."



Let's see, now ... picking up where we left off ... one billion, sixty-two million, thirty thousand, four hundred and thirteen ... one billion, sixty-two million, thirty thousand, four hundred and fourteen ... "

圖片來源

知識是人類共有財富

所有圖片取自

- 1. NASA網站 mostly HST pictures
 - 2. 許瑞榮教授講義
- 3. 物理學家照片取自 APS等網站
 - 4. 部分取自圖片附加說明網站

some of the transparencies were extracted from http://www.aip.de/~mstein/classes/Cosmology_201/

5. 如需轉載 請逕洽相關網站

一棵開花的樹/席慕容

如何讓你遇見我 在這最美麗的時刻 為這 我已在佛前 求了五百年 求祂讓我們結一段塵緣

佛於是把我化作一棵樹 長在你必經的路旁 陽光下慎重地開滿了花 朵朵都是我前世的盼望 Feynman 說教書 會讓自己覺得自己是有用的人 所以先謝謝大家搭乘企業號 讓我有機會變成有用的人

當你走近 請你細聽 那顫抖的葉是我等待的熱情 而當你終於無視地走過 在你身後落了一地的 朋友啊 那不是花瓣 是我凋零的心





十大驚奇

• 什麼物理現象最令人讚嘆?

大自然讀過物理?

電子為何這麼聽話?

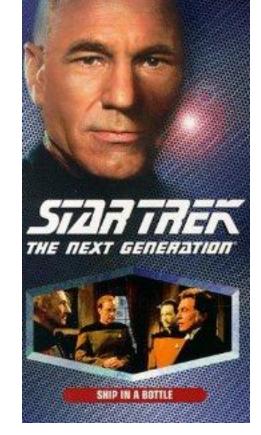




Professor James Moriarty



Countess Regina Bartholomew



www.imdb.com



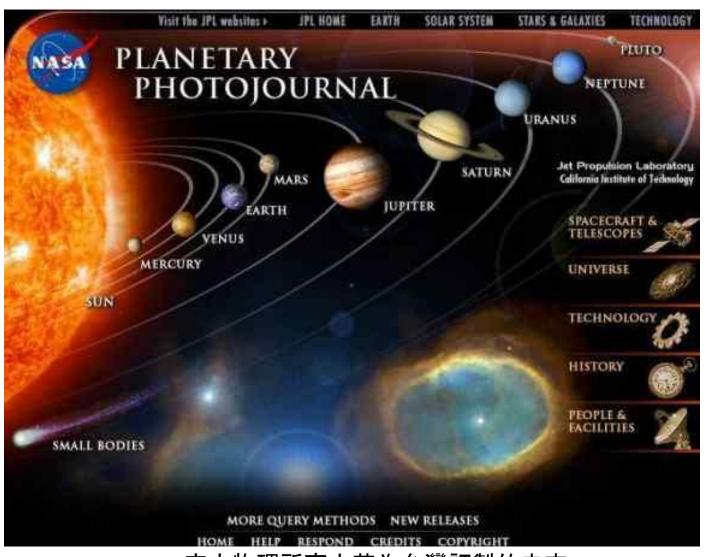
memory-alpha.org

Captain Picard: In a sense, who knows? Our reality may be very much like theirs. All this might just be an elaborate simulation running inside a little device sitting on someone's table.

給我五分鐘 我給你一個溫暖的家

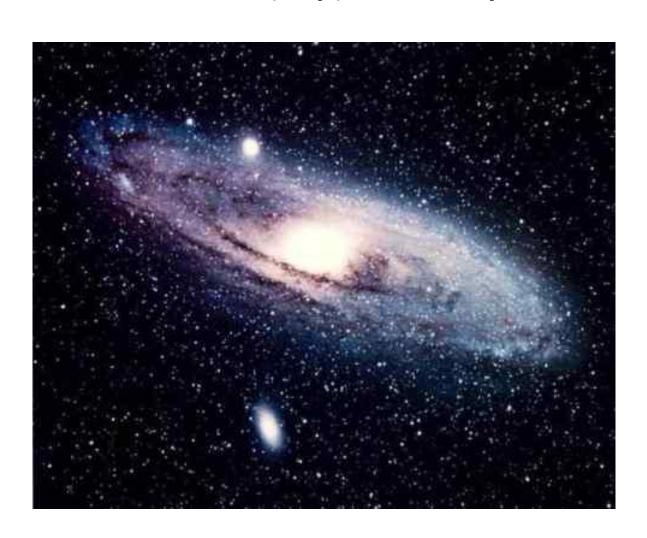
給我十分 我給你一個浩瀚的宇宙

台灣100分,台灣的未來都滿分



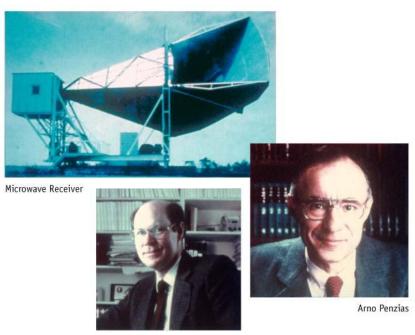
交大物理所高文芳為台灣訂製的未來 2004.8

仙女座 M31.NGC 224 Andromeda d~2500 (kly)~10⁶ ly



圖VII: AT&T研究人員彭佳士與威爾遜與他們的電波天線。 1964年,他們發現電波天線偵測到一個背景噪音。幾經努力, 他們確信這個噪音不是來自儀器的雜訊, 而是來自銀河系外。 經過一些仔細、深入的測量與分析, 他們推測這些噪音是波長 約為λ≒7.35 cm 的電磁輻射, 更進一步測量不同波長雜訊的 輻射強度, 發現其輻射強度和波長的關係, 暗示輻射源是大約 2.73 K的黑體輻射。

DISCOVERY OF COSMIC BACKGROUND



MAP990045 Robert Wilson

Alpher-Bethe-Gamow theory

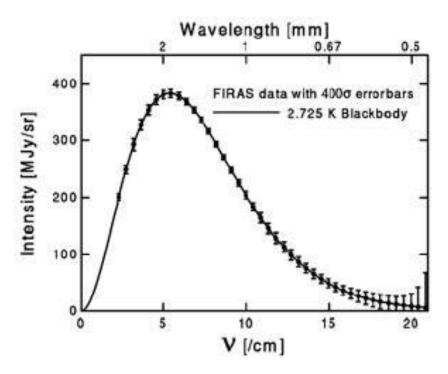
Gamow produced an important cosmogony paper with his student Ralph Alpher, which was published as "The Origin of Chemical Elements" (Physical Review, April 1, 1948). This paper became known as the Alpher-Bethe-Gamow theory. Gamow had the name of Hans Bethe listed on the article as "H. Bethe, Cornell University, Ithaca, New York" to make a pun on the first three letters of the Greek alphabet, alpha, beta and gamma. Bethe was also known for his sense of humor, but had no other role in the α - β - γ paper, and his name had been added without his knowledge. Gamow's lifetime interest in playing pranks, punning, and doggerel verse come across in some of his popular writings, notably his Mr. Tompkins... series of books (1939–1967).



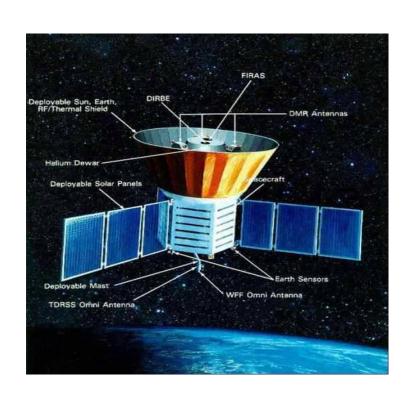
George Gamov 1904-1968

The results of these calculations were first announced in a letter to The Physical Review, April 1, 1948. This was signed Alpher, Bethe, and Gamow, and is often referred to as the 'alphabetical article.' It seemed unfair to the Greek alphabet to have the article signed by Alpher and Gamow only, and so the name of Dr. Hans A. Bethe (in absentia) was inserted in preparing the manuscript for print. Dr. Bethe, who received a copy of the manuscript, did not object, and, as a matter of fact, was quite helpful in subsequent discussions. There was, however, a rumor that later, when the alpha, beta, gamma theory went temporarily on the rocks, Dr. Bethe seriously considered changing his name to Zacharias.

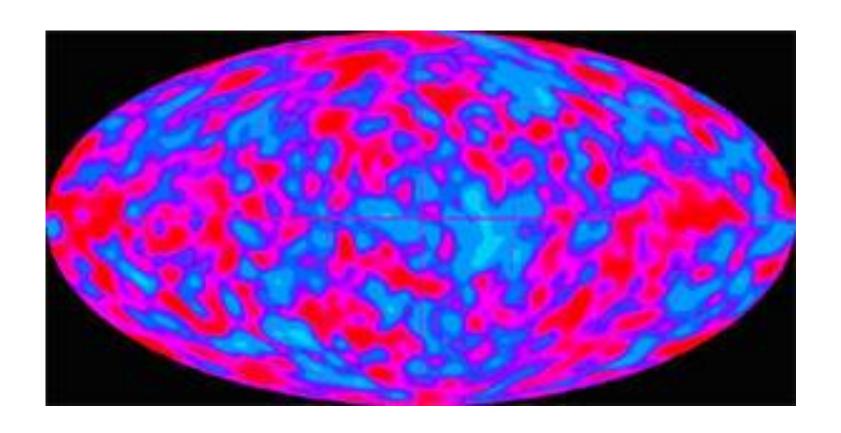
圖VIII: COBE (cosmic microwave background radiation explorer) 衛星與COBE所測得的宇宙背景輻射其強度與波長之間的關係圖,這個圖就是引爆量子力學革命的黑體輻射特性圖。



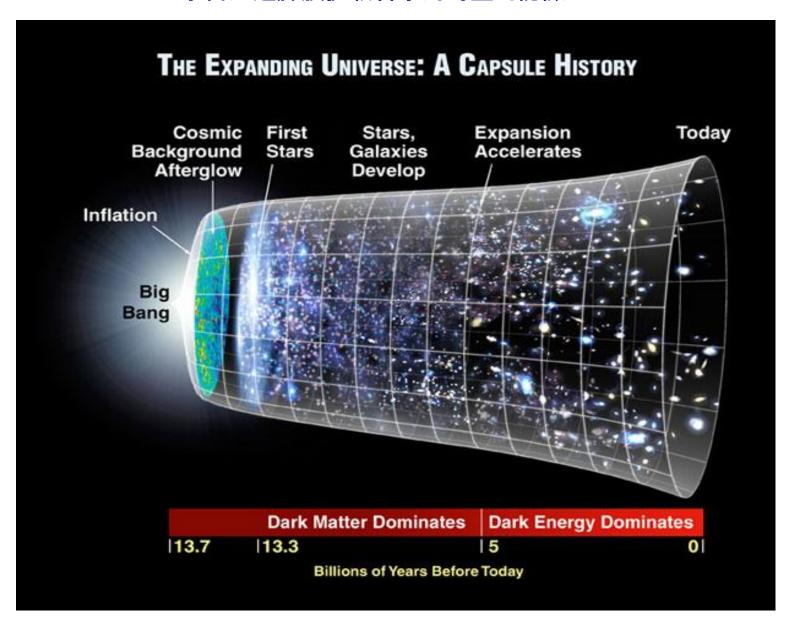
1 Jy(Jansky)=10⁻²⁶ W/m²/hz



圖IX: COBE所量得的宇宙黑體溫度分布圖, 紅色代表溫度較高, 其溫差上下僅為10⁻⁴K。



宇宙加速膨脹挑戰科學對時空的認識



History of the Universe WE ARE HERE 1 Galaxy and Star \odot THE UNIVERSE BECOMES TRANSPARENT 0 e 0 10² sec. 8 00 LEPTON EPOCH P 10⁻¹⁰ sec. Ū v ? v 10⁻⁴³ sec. 0 0

Standard Model of

FUNDAMENTAL PARTICLES AND INTERACTIONS

The Standard Model summarizes the current knowledge in Particle Physics. It is the quantum theory that includes the theory of strong interactions (quantum chromodynamics or QCD) and the unified theory of weak and electromagnetic interactions (electroweak). Gravity is included on this chart because it is one of the fundamental interactions even though not part of the "Standard Model."

FERMIONS

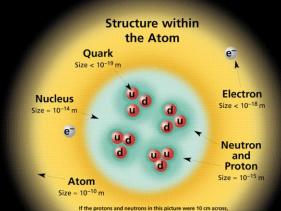
matter constituents spin = 1/2, 3/2, 5/2, ...

Leptons spin = 1/2			Quarks spin = 1/2			
Flavor	Mass GeV/c ²	Electric charge	Flavor	Approx. Mass GeV/c ²	Electric charge	
ν _e electron neutrino	<1×10 ⁻⁸	0	U up	0.003	2/3	
e electron	0.000511	-1	d down	0.006	-1/3	
$ u_{\mu}^{\text{muon}}$ neutrino	<0.0002	0	C charm	1.3	2/3	
μ muon	0.106	-1	S strange	0.1	-1/3	
ν _τ tau neutrino	<0.02	0	t top	175	2/3	
τ tau	1.7771	-1	b bottom	4.3	-1/3	

Spin is the intrinsic angular momentum of particles. Spin is given in units of h, which is the guantum unit of angular momentum, where $\hbar = h/2\pi = 6.58 \times 10^{-25}$ GeV s = 1.05x10⁻³⁴ J s.

Electric charges are given in units of the proton's charge. In SI units the electric charge of the proton is 1.60×10^{-19} coulombs.

The energy unit of particle physics is the electronvolt (eV), the energy gained by one electron in crossing a potential difference of one volt. Masses are given in GeV/c2 (remember $E = mc^2$), where 1 GeV = 10^9 eV = 1.60×10^{-10} joule. The mass of the proton is 0.938 GeV/ c^2 $= 1.67 \times 10^{-27} \text{ kg}$



then the quarks and electrons would be less than 0.1 mm in

size and the entire atom would be about 10 km across.

PROPERTIES OF THE INTERACTIONS

Flavor

Quarks, Leptons

W+ W- Z⁰

10-4

10-7

BOSONS

force carriers spin = 0, 1, 2, ...

Unified Electroweak spin = 1					
Name	Mass Elect GeV/c ² charg				
γ photon	0	0			
W-	80.4	-1			
W ⁺	80.4	+1			
Z ⁰	91.187	0			

Strong (color) spin = 1				
Name	Mass GeV/c ²	Electric charge		
g gluon	0	0		

Color Charge

Each quark carries one of three types of "strong charge," also called "color charge. These charges have nothing to do with the colors of visible light. There are eight possible types of color charge for gluons. Just as electri-

cally-charged particles interact by exchanging photons, in strong interactions color-charged particles interact by exchanging gluons. Leptons, photons, and W and Z bosons have no strong interactions and hence no color charge.

Quarks Confined in Mesons and Baryons

One cannot isolate quarks and gluons; they are confined in color-neutral particles called hadrons. This confinement (binding) results from multiple exchanges of gluons among the color-charged constituents. As color-charged particles (quarks and gluons) move apart, the energy in the color-force field between them increases. This energy eventually is converted into additional quark-antiquark pairs (see figure below). The quarks and antiquarks then combine into hadrons; these are the particles seen to emerge. Two types of hadrons have been observed in nature: mesons $q\bar{q}$ and baryons qqq.

Residual Strong Interaction

See Residual Strong

Hadrons

Mesons

Not applicable

to quarks

20

Interaction Note

Strong

Fundamental

Color Charge

Ouarks. Gluons

Gluons

25

Not applicable

to hadrons

Electric Charge

Electrically charged

The strong binding of color-neutral protons and neutrons to form nuclei is due to residual strong interactions between their color-charged constituents. It is similar to the residual electrical interaction that binds electrically neutral atoms to form molecules. It can also be viewed as the exchange of mesons between the hadrons.

Property

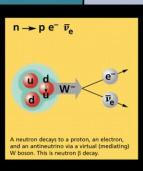
Baryons qqq and Antibaryons qqq

Baryons are fermionic hadrons. There are about 120 types of baryons.							
Symbol	Name	Quark content	Electric charge	Mass GeV/c ²	Spin		
р	proton	uud	1	0.938	1/2		
p	anti- proton	ūūd	-1	0.938	1/2		
n	neutron	udd	0	0.940	1/2		
Λ	lambda	uds	0	1.116	1/2		
Ω^-	omega	SSS	-1	1.672	3/2		

Matter and Antimatter

For every particle type there is a corresponding antiparticle type, denoted by a bar over the particle symbol (unless + or - charge is shown). Particle and antiparticle have identical mass and spin but opposite charges. Some electrically neutral bosons (e.g., Z^0 , γ , and $\eta_c = c\bar{c}$, but not $K^0 = d\overline{s}$) are their own antiparticles.

These diagrams are an artist's conception of physical processes. They are not exact and have no meaningful scale. Green shaded areas represent the cloud of gluons or the gluon field, and red lines the quark paths.



Interaction

Acts on:

Particles experiencing:

Particles mediating:

Strength relative to electromag 10⁻¹⁸ m

for two u quarks at:

for two protons in nucleus

Gravitational

Mass - Energy

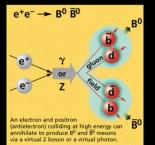
All

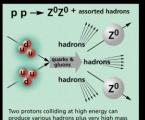
Graviton

10-41

10-41

10-36





particles such as Z bosons. Events such as this one are rare but can yield vital clues to the structure of matter.

		ons are bo about 140			
Symbol	Name	Quark content	Electric charge	Mass GeV/c ²	Spin
π^+	pion	ud	+1	0.140	0
K-	kaon	sū	-1	0.494	0
ρ^+	rho	ud	+1	0.770	1
B ⁰	B-zero	db	0	5.279	0
η	eta-c	cē	0	2 .980	0

The Particle Adventure

Visit the award-winning web feature The Particle Adventure at http://ParticleAdventure.org

This chart has been made possible by the generous support of:

U.S. Department of Energy U.S. National Science Foundation

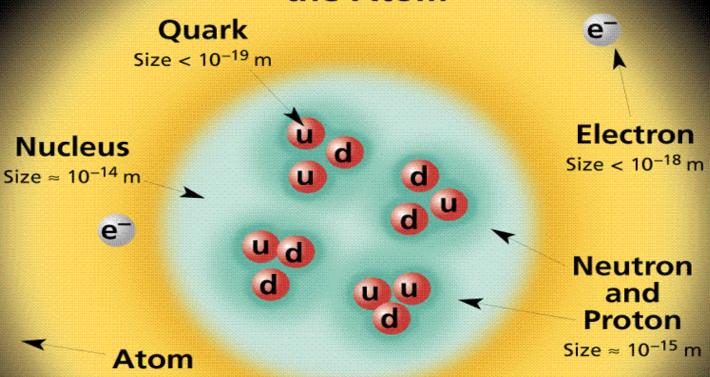
Lawrence Berkeley National Laboratory Stanford Linear Accelerator Center American Physical Society, Division of Particles and Fields

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http://CPEPweb.org

Structure within the Atom



If the protons and neutrons in this picture were 10 cm across, then the quarks and electrons would be less than 0.1 mm in size and the entire atom would be about 10 km across.

Size $\approx 10^{-10}$ m

FERMIONS

matter constituents spin = 1/2, 3/2, 5/2, ...

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Flavor	Mass GeV/c ²	Electric charge	Flavor	Approx. Mass GeV/c ²	Electric charge		
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g gluon	0	0			

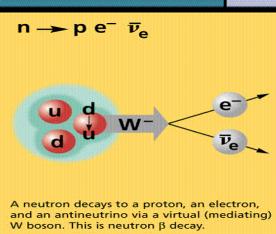
Color Charge

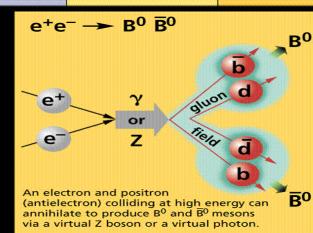
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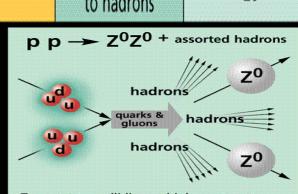
cally-charged particles interact by exchanging photons, in strong interactions color-charged particles interact by exchanging gluons. Leptons, photons, and **W** and **Z** bosons have no strong interactions and hence no color charge.

PROPERTIES OF THE INTERACTIONS

Interaction Property Property		Gravitational	Weak	Electromagnetic	Strong	
Troperty	\	Ciavitational	(Electr	oweak)	Fundamental	Residual
Acts on:		Mass – Energy	Flavor	Electric Charge	Color Charge	See Residual Strong Interaction Note
Particles experiencing:		All	Quarks, Leptons	Electrically charged	Quarks, Gluons	Hadrons
Particles mediating:		Graviton (not yet observed)	W+ W- Z ⁰	γ	Gluons	Mesons
Strength relative to electromag	10 ⁻¹⁸ m	10 ⁻⁴¹	0.8	1	25	Not applicable
for two u quarks at:	3×10 ⁻¹⁷ m	10 ⁻⁴¹	10 ⁻⁴	1	60	to quarks
for two protons in nucleus		10 ⁻³⁶	10 ⁻⁷	1	Not applicable to hadrons	20
$p \rightarrow p = \overline{y}$ $p \rightarrow R^0 \overline{R}^0$ $p \rightarrow 7070 + assorted hadrons$						







Two protons colliding at high energy can produce various hadrons plus very high mass particles such as Z bosons. Events such as this one are rare but can yield vital clues to the structure of matter.

Baryons qqq and Antibaryons qqq

Baryons are fermionic hadrons.

There are about 120 types of baryons.

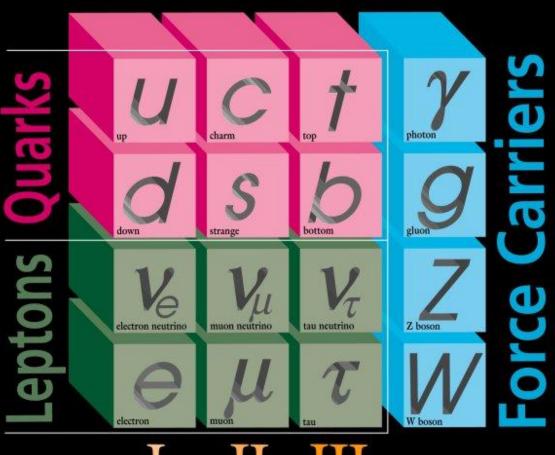
There are about 120 types of baryons.						
Symbol	Name	Quark content	Electric charge	Mass GeV/c ²	Spin	
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n	neutron	udd	0	0.940	1/2	
Λ	lambda	uds	0	1.116	1/2	
Ω -	omega	SSS	٦	1.672	3/2	

Mesons $q\bar{q}$

Mesons are bosonic hadrons.

There are about 140 types of mesons.

Symbol	Name	Quark content	Electric charge	Mass GeV/c ²	Spin
π^{+}	pion	ud	+1	0.140	0
K-	kaon	sū	-1	0.494	0
$ ho^+$	rho	ud	+1	0.770	1
B ⁰	B-zero	db	0	5.279	0
η_{c}	eta-c	ςζ	0	2 .980	0



Three Generations of Matter

Yang, C. N.; Mills, R. (1954). "Conservation of Isotopic Spin and Isotopic Gauge Invariance". Physical Review 96 (1): 191–195

Conservation of Isotopic Spin and Isotopic Gauge Invariance*

C. N. Yang † and R. L. Mills

Brookhaven National Laboratory, Upton, New York

(Received June 28, 1954)

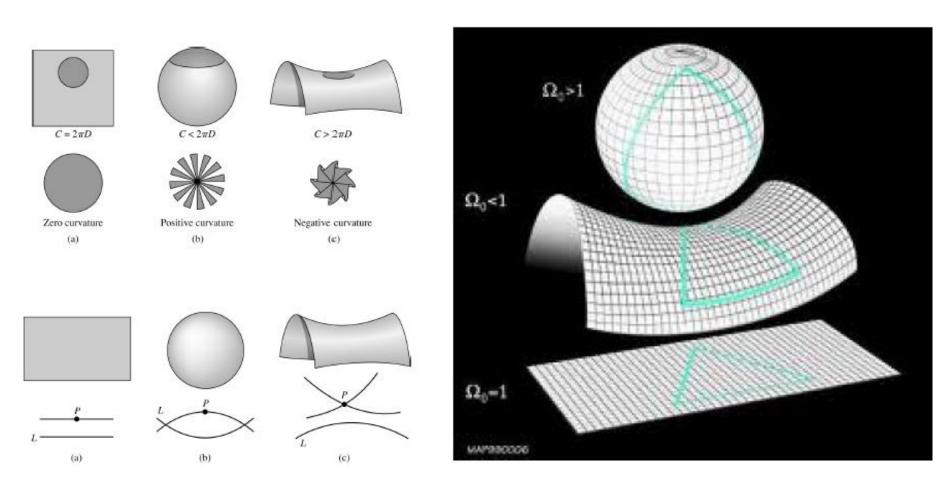
It is pointed out that the usual principle of invariance under isotopic spin rotation is not consistant with the concept of localized fields. The possibility is explored of having invariance under local isotopic spin rotations. This leads to formulating a principle of isotopic gauge invariance and the existence of a \mathbf{b} field which has the same relation to the isotopic spin that the electromagnetic field has to the electric charge. The \mathbf{b} field satisfies nonlinear differential equations. The quanta of the \mathbf{b} field are particles with spin unity, isotopic spin unity, and electric charge $\pm e$ or zero.



C. N. Yang (1922 -) and Robert Mills (1927 - 1999) at Stony Brook in 1999. francisthemulenews.wordpress.com

均匀、無向

Friedmann-Robertson-Walker 空間



http://web.it.nctu.edu.tw/~wfgore/cosmology121.pdf

$$X^{2} + Y^{2} + Z^{2} + W^{2} = A^{2}$$

$$X^{2} + Y^{2} + Z^{2} = B^{2}$$

$$X^{2} + Y^{2} + Z^{2} - W^{2} = A^{2}$$

$$X = A \sin \chi \sin \theta \sin \varphi,$$

$$Y = A \sin \chi \sin \theta \cos \varphi,$$

$$Z = A \sin \chi \cos \theta,$$

$$W = A \cos \chi.$$

$$X = A \sin \chi \sin \theta \sin \varphi,$$

$$Y = A \sin \chi \sin \theta \cos \varphi,$$

$$Z = A \sin \chi \cos \theta,$$

$$W = A \cos \chi.$$

$$dX^{2} + dY^{2} + dZ^{2} + dW^{2}$$

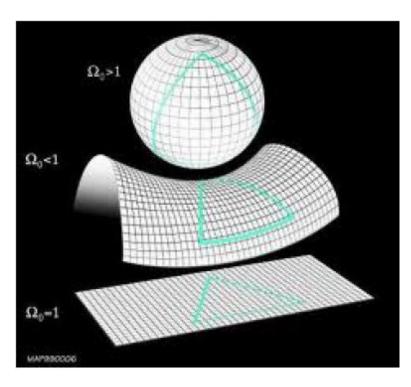
$$= A^{2} \left[d\chi^{2} + \sin^{2} \chi d\Omega \right].$$

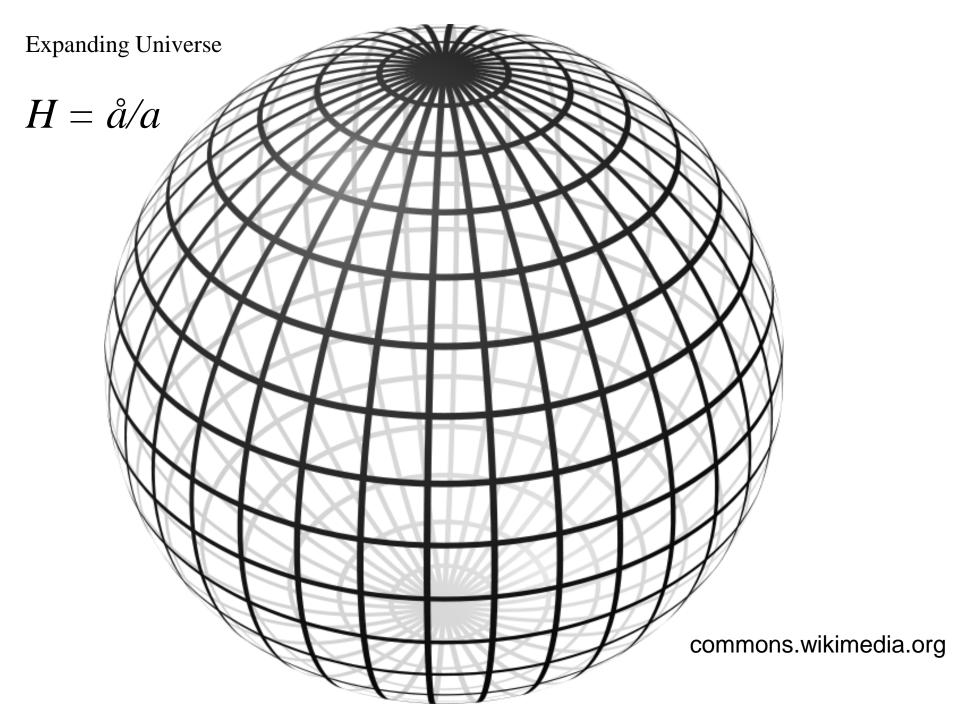
$$r = \sin \chi \qquad dr = \cos \chi d\chi$$
$$dr^2/\cos^2 \chi = d\chi^2 = dr^2/(1 - r^2)$$

$$\left[\frac{dr^2}{1-kr^2} + r^2(d\theta^2 + \sin^2\theta \ d\varphi^2)\right]$$

Similarly for the open space with k=-1 by replacing $\sin \chi$ ($\cos \chi$) with $\sinh \chi$ ($\cosh \chi$).

$$ds^2 = dt^2 - ds_3^2$$
.





$$(T_b^a) = \operatorname{diag}(\rho, -p, -p, -p)$$

$$D_a T_b^a = 0$$

$$\frac{d\rho}{dt} = -3H(t)(\rho + p)$$

能量守恆定律

$$H^2 + \frac{k}{a^2} = \frac{8\pi G}{3}\rho$$

愛因斯坦方程式

$$R_a{}^b - \frac{1}{2} \, \delta_a{}^b R = 8\pi G \, T_a{}^b$$

$$\frac{d\rho}{dt} = -3H(t)(\rho + p)$$
H = å/a

$$d\left(\frac{4\pi}{3}a^3\rho\right) = -p \ 4\pi a^2 da$$

$$dU=-pdV+TdS$$

$$U=\rho V,\ V=4\pi a^3/3,\ S \ \text{the entropy}$$

$$TdS=\bar{d}Q$$

volume of the 3-sphere S^3 is $2\pi^2a^3$ instead of $4\pi a^3/3$.

$$ds^2 = a^2 \left[d\chi^2 + \sin^2 \chi d\Omega \right]$$

$$H^2 + \frac{k}{a^2} = \frac{8\pi G}{3}\rho$$

$$\frac{1}{2}m\dot{a}^2 - mG\left[\frac{\left(\frac{4\pi}{3}a^3\right)\rho}{a}\right] = -m\frac{k}{2}$$

$$E = T + V = -m\frac{k}{2}$$

$$rac{d
ho}{dt} = -3H(t)(
ho+p)$$
 能量守恆定律

the equation of state $p=\omega\rho$ we can write $\rho+p=\gamma\rho$ with the relation $\gamma=1+\omega$

$$\dot{\rho} = -3H\gamma\rho \ ,$$
$$\rho \propto a^{-3\gamma}$$

For matter dominated (MD) universe $\gamma=1(\omega=0)$ $\rho\propto a^{-3}$ For a radiation dominated (RD) universe $\gamma=4/3(\omega=1/3)$ $\rho\propto a^{-4}$

for the case of vacuum dominated (VD) $\gamma = 0$ $\rho = {\rm constant}.$

For matter dominated (MD) universe $\gamma = 1(\omega = 0)$ $\rho \propto a^{-3}$

$$H^2 + \frac{k}{a^2} = \frac{8\pi G}{3} \rho$$
 $H = å/a$

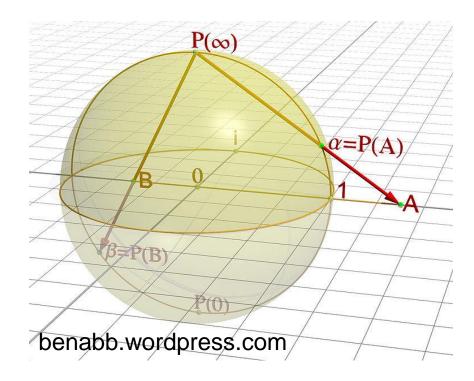
For a flat FRW MD universe, $H^2 = 8\pi G\rho/3$ with $\rho = \rho_0/a^3$. Therefore,

$$\dot{a}^2 = H_0^2 \frac{1}{a}.$$
 $\begin{array}{c}
a \, \text{以} \, a_0 \, \text{為單位} \\
t_0 \, \text{表示現在時間}
\end{array}$
(94)

The age of the universe can be integrated from $\int dt = \int da/\dot{a}$. The result is:

$$t = \frac{2}{3H_0} \ . \qquad \qquad H^2 = H_0^2 \ \frac{1}{a^3}$$

	ho	a
RD	a^{-4}	$(t/t_0)^{1/2}$
MD	a^{-3}	$(t/t_0)^{2/3}$
VD	constant	$\exp[H_0(t-t_0)]$

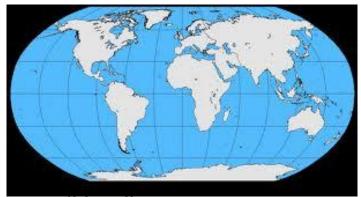


 $S^2 = R^2 + \{P\}$ 原來球面比平面大

manifold 幾河流形 locally Rⁿ



etsy.com



en.wikipedia.org



mappery.com

數學家的宇宙學和高能物理

- 微積分 --- 牛頓重力場
- 黎曼幾何 -- 愛因斯坦重力場
- 纖維束 Fiber Bundle --- 規範場
- Calabi-Yau 流形 ---- Superstring
- Hyperspace 高空間 / 表面宇宙 (Brane Universe)

Riemann, Georg Friedrich Bernhard 黎曼(1826~1866)

- 生於德國漢諾威 (Hanover), 卒於義大利 Selasca。黎曼在分析與幾何上有極廣泛與深入 的貢獻, 其空間觀念與方法, 影響及於現代理 論物理, 尤其是廣義相對論。
- 25歲得到哥廷根的博士學位,兩年後提出論文 〈On the representation of a function by means of a trigonometrical series〉申請哥廷根的(無給)講師職位,1854年在偉大的高斯面前發 表就職演說〈On the Hypothesis that forms the foundation of Geometry〉。在 這篇演說中,黎曼為此後一百五十年的微分幾 何大業指出了方向,立下了基礎,論文的本身 不僅是個數學史上的一篇傑作,並且在表達上 也是一個典範。



統一場論

- 重力
 - 牛頓重力 F= GMm / r²
- 電磁力 SU(1)
 - 庫倫定律 F= kQq / r²

1950-

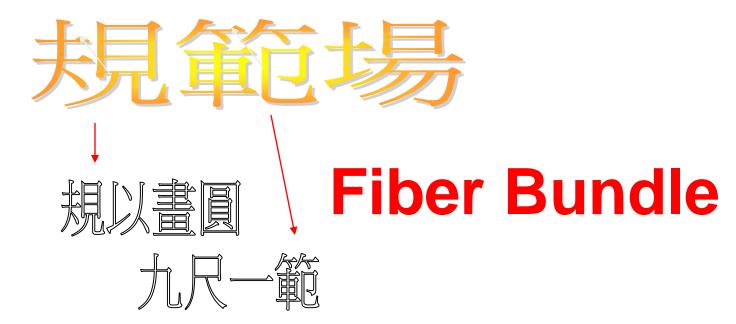
- 弱交互作用力 SU(2)
- 強交互作用力 SU(3)

Hermann Klaus Hugo Weyl [1885-1955]

 1918 He produced the first guage theory in which the Maxwell electromagnetic field and the gravitational field appear as geometrical properties of space-time.



Gauge/Scale symmetry



規範場 Let there be light!

```
d\{\Psi'(x)\}=d\{\exp[i\theta(x)]\Psi(x)\}=
           \exp [i\theta(x)] \{i[d\theta(x)] \Psi(x)\}
           + \exp \left[ i \theta (x) \right] \left\{ d \Psi(x) \right\}
(d+A') \{\Psi'(x)\} = (d+\underline{A'}) \{\exp [i\theta(x)] \Psi(x)\}
            = (d + \underline{A - i \ d \theta}) \{ \exp [i \theta (x)] \Psi(x) \}
           = \exp [i \theta (x)] \{i [d \theta(x)] \Psi(x)\}
               + \exp [i \theta (x)] \{d \Psi(x)\}
              -\exp[i\theta(x)]\{i[d\theta(x)]\Psi(x)\}
= \exp [i \theta (x)] (d+A) \{ \Psi(x) \}
```

Theodor Franz Eduard Kaluza [1885-1954]

- Kaluza in 1919, sent a paper to Albert <u>Einstein</u> proposing a unification of gravity with <u>Maxwell</u>'s theory of light
- This paper was communicated by <u>Einstein</u> himself on 8 December 1921 for publishing

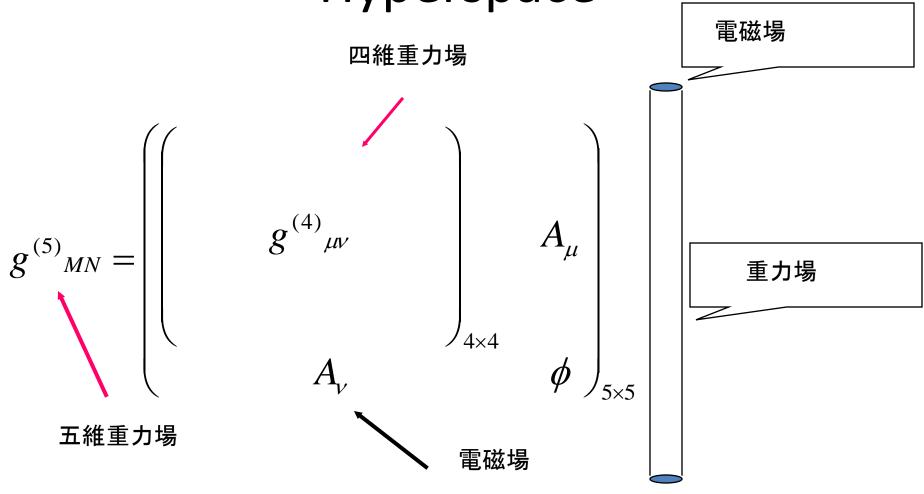


Oskar Klein [1894-1977]

- Klein assumed the fifth dimension to be periodic with a period I = c(2k)^{1/2}/e where e was the charge of the electron and k was Einstein's constant of gravitation. The dimension was on the order of the Planck length.
- Klein's results were published in *Nature* in the autumn of 1926.

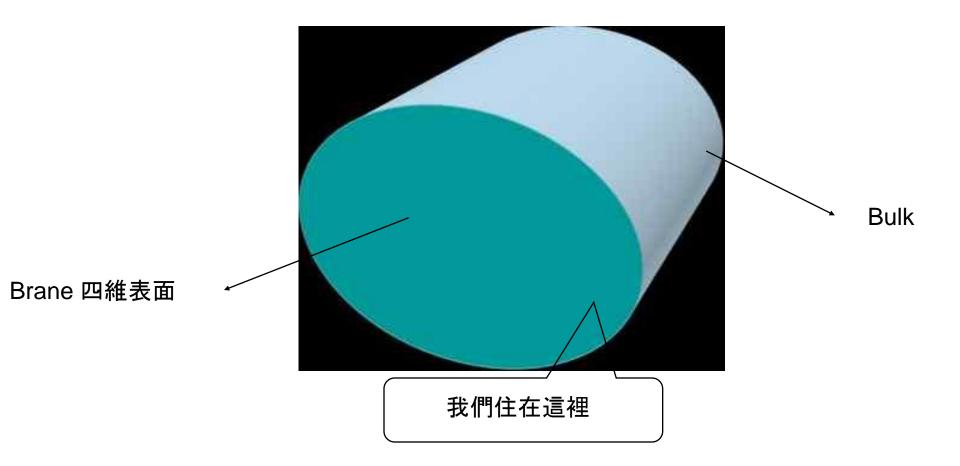


Kaluza-Klein Theory of Hyperspace



Randall-Sundrum 1999 高空間表面物理Brane (hypersurface) Physics

Extra dimension 第五維



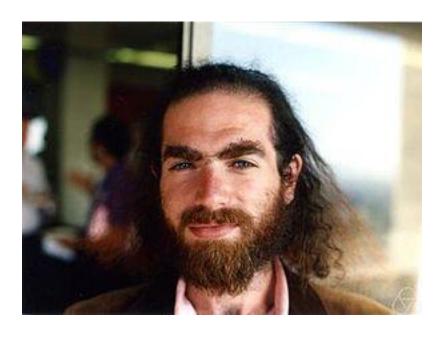
$$\mathcal{L}_{gf} = -\frac{1}{4} \text{Tr}(F^2) = -\frac{1}{4} F^{\mu\nu a} F_{\mu\nu}{}^a \quad F_{\mu\nu} = T_a F_{\mu\nu}{}^a$$
$$[T_a, T_b] = i f^{abc} T_c \qquad D_{\mu} = I \partial_{\mu} - i g T_a A_{\mu}{}^a$$
$$F_{\mu\nu}{}^a = \partial_{\mu} A_{\nu}{}^a - \partial_{\nu} A_{\mu}{}^a + g f^a{}_{bc} A_{\mu}{}^b A_{\nu}{}^c$$

$$[D_{\mu}, D_{\nu}] = -igT_a F_{\mu\nu}{}^a.$$

$$\partial^{\mu} F_{\mu\nu}{}^{a} + g f^{a}{}_{bc} A^{\mu b} F_{\mu\nu}{}^{c} = 0.$$

$$(D^{\mu}F_{\mu\nu})^a = 0.$$

數學家也瘋狂



Grigori Perelman in 1993

Born Grigori Yakovlevich Perelman

13 June 1966 (age 45) Leningrad, Soviet Union

Residence Saint Petersberg, Russia

Citizenship Russia Nationality Russian Fields Mathematics

Alma mater Leningrad State University Doctoral advisor Aleksandr Aleksandrov

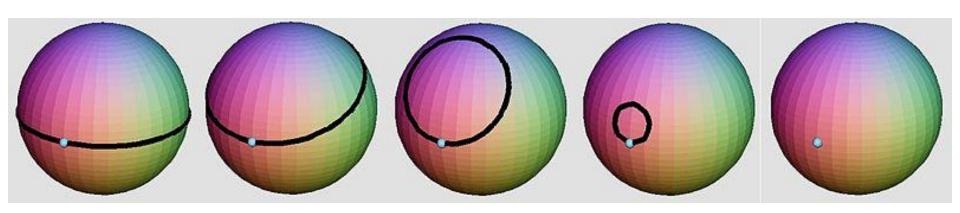
Yuri Burago

Known for Riemannian geometry

Geometric topology

Proof of the Poincare Conjecture

Notable awards Saint Petersburg Mathematical Society Prize (1991), accepted EMS Prize (1996), declined Fields Medal (2006), declined Millennium Prize (2010), declined



For compact 2-dimensional surfaces without boundary, if every loop can be continuously tightened to a point, then the surface is topologically homeomorphic to a 2-sphere (usually just called a sphere). The Poincaré conjecture asserts that the same is true for 3-dimensional spaces.

The Fields Medal and Millennium Prize

In May 2006, a committee of nine mathematicians voted to award Perelman a Fields Medal for his work on the Poincaré conjecture.[14] The Fields Medal is the highest award in mathematics: [citation needed] two to four medals are awarded every four years. However, Perelman declined to accept the prize. Sir John Ball, president of the International Mathematical Union, approached Perelman in Saint Petersburg in June 2006 to persuade him to accept the prize. After 10 hours of persuasion over two days, Ball gave up. Two weeks later, Perelman summed up the conversation as follows: "He proposed to me three alternatives: accept and come; accept and don't come, and we will send you the medal later; third, I don't accept the prize. From the very beginning, I told him I have chosen the third one... [the prize] was completely irrelevant for me. Everybody understood that if the proof is correct, then no other recognition is needed."[14] "I'm not interested in money or fame,' he is quoted to have said at the time. 'I don't want to be on display like an animal in a zoo. I'm not a hero of mathematics. I'm not even that successful; that is why I don't want to have everybody looking at me."[23] Nevertheless, on 22 August 2006, Perelman was publicly offered the medal at the International Congress of Mathematicians in Madrid "for his contributions to geometry and his revolutionary insights into the analytical and geometric structure of the Ricci flow."[24] He did not attend the ceremony, and declined to accept the medal, making him the first person to decline this prestigious prize.[25][26] He had previously turned down a prestigious prize from the European Mathematical Society, [26] allegedly saying that he felt the prize committee was unqualified to assess his work, even positively.[27] On 18 March 2010, Perelman was awarded a Millennium Prize for solving the problem. [28] On June 8, 2010, he did not attend a ceremony in his honor at the Institut Océanographique, Paris to accept his \$1 million prize.[29] According to Interfax, Perelman refused to accept the Millennium prize in July 2010. He considered the decision of Clay Institute unfair for not sharing the prize with Richard Hamilton, [5] and stated that "the main reason is my disagreement with the organized mathematical community. I don't like their decisions, I consider them unjust."[6]

Perelman's proof was rated one of the top cited articles in Math-Physics in 2008.[30]

Possible withdrawal from mathematics
As of the spring of 2003, Perelman no longer worked at the Steklov Institute.[31] His friends are said to have stated that he currently finds mathematics a painful topic to

discuss; some even say that he has abandoned mathematics entirely.[32] According to a 2006 interview, Perelman was then unemployed, living with his mother in Saint Petersburg.[31]

Perelman is quoted in an article in The New Yorker saying that he is disappointed with the ethical standards of the field of mathematics. The article implies that Perelman refers particularly to the efforts of Fields medalist Shing-Tung Yau to downplay Perelman's role in the proof and play up the work of Cao and Zhu. Perelman added, "I can't say I'm outraged. Other people do worse. Of course, there are many mathematicians who are more or less honest. But almost all of them are conformists. They are more or less honest, but they tolerate those who are not honest."[14] He has also said that "It is not people who break ethical standards who are regarded as aliens. It is people like me who are isolated."[14]

has said that "As long as I was not conspicuous, I had a choice. Either to make some ugly thing or, if I didn't do this kind of thing, to be treated as a pet. Now, when I become a very conspicuous person, I cannot stay a pet and say nothing. That is why I had to quit." (The New Yorker authors explained Perelman's reference to "some ugly thing" as "a fuss" on Perelman's part about the ethical breaches he perceived).[33] It is uncertain whether his resignation from Steklov and subsequent seclusion mean that he has ceased to practice mathematics. Fellow countryman and mathematician Yakov Eliashberg said that, in 2007, Perelman confided to him that he was working on other things but it was too premature to talk about it. He is said to have been interested in the past in the Navier—Stokes equations and the set of problems related to them that also constitutes a Millennium Prize, and there has been speculation that he may be working on them now.[34]

This, combined with the possibility of being awarded a Fields medal, led him to guit professional mathematics. He

Ed. Witten [1951-] 通識教育 Fields Medal, 1990 讓歷史系學生換跑道

布蘭代斯大學 (Brandeis) B.A. 1971 歷史系

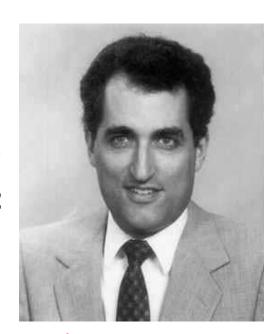
Princeton M.A. 1974 / Ph.D. in 1976

Harvard 博士後 1976-77; Junior Fellow 1977-80

Princeton 物理教授 1980 MacArthur Fellowship 1982

高等研究院(Institute for Advanced Study)

Professor in the School of Natural Sciences 1982

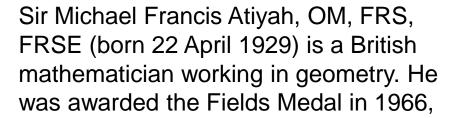


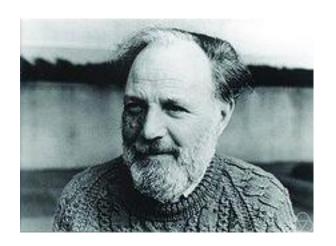
數學是科學之母 物理是科學之父

Atiyah: 雖然他顯然是物理學家(從他的著作可知),然而他主導數學的能力顯然少有數學家可以出其右,他以數學描述物理觀念的能力也是近乎唯一. 其完美地運用物理直觀,開創新而深入的數學的能力,

一再令數學界嘆為觀止....







Isadore Manuel Singer (in 1977), who worked with Atiyah on index theory

(born April 24, 1924)

In 1966, when he was 36 years old, he was awarded the Fields Medal, for his work in developing K-theory, a generalized Lefschetz fixed-point theorem and the Atiyah–Singer theorem, for which he also won the Abel Prize jointly with Isadore Singer in 2004.[107]



丘成桐(Shing-Tung Yau, 1949年4月4日一), 美國人, 原籍廣東省梅州蕉嶺縣, 客家人, 生於汕頭, 長於香港。 著名數學家。數學界最高榮譽菲爾茲獎及沃爾夫數學獎 得主之一。

1982, Fields Medal, for his contributions to partial differential equations, to the Calabi conjecture in algebraic geometry, to the positive mass conjecture of general relativity theory, and to real and complex Monge-Ampère equations.

1997年,他受台灣新竹清華大學校長<u>劉炯朗</u>邀請,作為講席教授訪問一年。若干年後,他建議已是台灣國家科學委員會主席的劉炯朗,建立理論科學中心。正式成立是在1998年。他擔任理論科學中心顧問委員會主任直到2005年。

學測新方向

THE RECORD-BREAKING BESTSELLER NOW IN PAPERBACK

ABRIEF HISTORY OF TIME

From the Big Bang to Black Holes

'This book marries a child's wonder to a genius's intellect. We journey into Hawking's universe, while marvelling at his mind' Sunday Times



Introduction by Carl Sagan

STEPHEN HAWKING

Stephen William Hawking was born on 8 January 1942 (300 years after the death of Galileo) in Oxford, England.

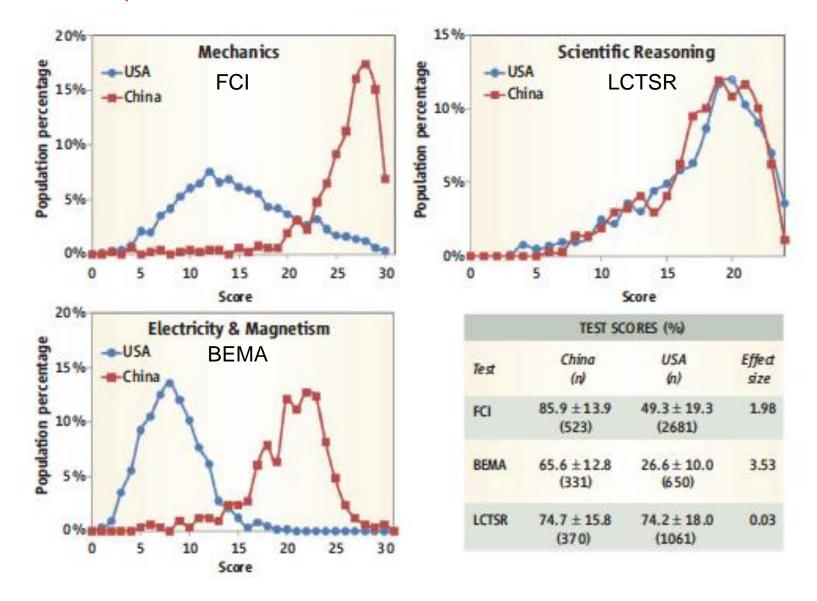
物理是不老仙丹

他是如何計算的?

Learning and Scientific Reasoning

Lei Bao, Tianfan Cai, Kathy Koenig, Kai Fang, Jing Han, Jing Wang, Qing Liu, Lin Ding, Lili Cui, Ying Luo, Yufeng Wang, Lieming Li, and Nianle Wu

Science 30 January 2009: 586-587.



U1 is a large research-1 state university, U.S. ranking top 60, acceptance rate 59%. U2 is a large research-1 state university, U.S. ranking top 60, acceptance rate 60%. U3 is a large tier-4 state university with an acceptance rate of 84%. U4 is a large tier-3 state university with an acceptance rate of 69%.

The three Chinese universities are labeled with C1, C2, and C3.

Their national rankings are also given below (based on 2007 ranking from Sina Educatoin News, http://edu.sina.com.cn).

(A national university is one that is under direct control of the department of education.)

C1 is a top 30 national university.

C2 is a top 60 national university.
C3 is a top 130 national university.

清華大學都會、非都會高中學業成績表現

入學方式	年度	畢業高中	名次百分比平均%	人數
繁星	96	都會	20.97%	30
	99	非都會	40.22%	428
推薦	88	都會	35.43%	544
	99	非都會	42.69%	573
申請	88	都會	41.89%	2044
	99	非都會	46.06%	1175
指考	92 99 [≀]	都會	52.99%	3455
		非都會	54.04%	2592

非都會高中資優生的表現並不輸都會高中一般學生不是都會明星高中才能培養優秀的學生

(都會高中為17所"都市明星高中")

清華大學繁星學生各縣市分佈情形

縣市	人數	繁星人數百分比	縣市人數百分比
		(縣市人數/總人數)	(縣市人口/台灣人口)
台北市	76人	17.16%	11.38%
新北市	57人	12.97%	16.86%
桃園縣	25人	5.64%	8.67%
新竹縣市	19人	4.29%	4.03%
苗栗縣	7人	1.58%	2.42%
台中市	54人	12.19%	11.47%
彰化縣	14人	3.16%	5.62%
南投縣	9人	2.03%	2.26%
嘉義縣	20人	4.52%	3.49%
雲林縣	15人	/3.39%	3.08%
台南市	34人	7.68%	\ 8.09% /
高雄市	63人	14.22%	11.95%
屏東縣	11人	2.48%	3.73%
台東縣	5人	1.13%	0.99%
花蓮縣	10人	2.26%	1.45%
宜蘭縣	21人	4.74%	/ 3.62%
外島	3人	0.68%	0.90%
總計	443人	100%	100%

繁星管道有較佳的地域分布性

頂大第一屆繁星錄取學生97上成績排名(百分比)

							分位值		
分發學校	人數	平均數	中位數	標準差	最小値	最大値	25	50	75
國立中央大學	16	37.21	24.41	31.94	2.04	100.00	11.15	24.41	61.72
國立台灣科技大 學	53	50.92	51.00	29.1	2.00	100.00	25.50	51.00	76.00
國立中興大學	39	28.60	28.60	25.16	1.60	89.80	6.80	20.50	45.50
國立中山大學	33	41.22	41.22	28.2	2.00	94.00	17.25	37.00	65.00
長庚大學	28	41.33	41.33	29.01	4.00	98.00	14.00	37.00	69.00
國立台灣大學	26	28.04	28.04	21.23	2.00	68.00	10.00	22.50	45.25
國立陽明大學	4	52.50	28.04	30.35	18.00	86.00	23.00	53.00	81.50
元智大學	25	37.96	52.50	32.55	2.00	100.00	12.25	26.00	66.00
國立政治大學	40	27.98	37.96	23.62	2.00	88.00	9.00	21.00	39.75
國立成功大學	30	27.47	27.98	22.34	1.32	86.67	10.11	19.14	41.74
國立交通大學	84	42.96	42.96	25.63	0.88	100.00	22.36	40.73	60.75
國立清華大學	134	40.87	40.87	26.81	1.45	100.00	16.59	36.55	59.65

各高中均有能力培養出有競爭力的學生,明星高中不應該是頂大的唯一選擇。

學測新方向與 高中生的夢靨

- 10. 太多必修課、學生沒有時間消化、吸收
- 沒有配套 變成填鴨教學
 - 製造許多不懂就背下來的學生

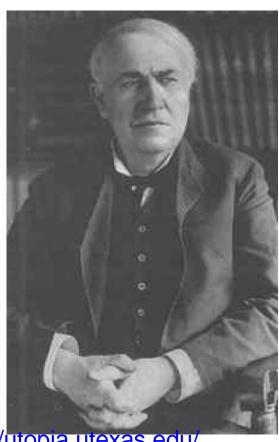
妥協下、可能必須暫時接受的的配套

- 數理課要把學生當文組教
- 社會課要把學生當理組教
 - •目的:給學生有一點點時間,停下來、想一想

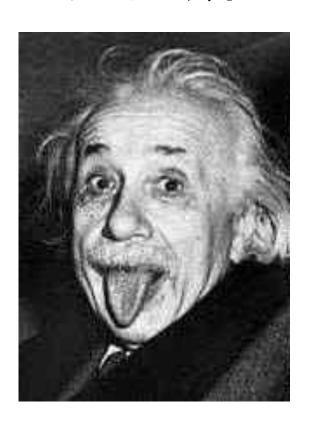
物理像宗教? 真理是?

愛因斯坦

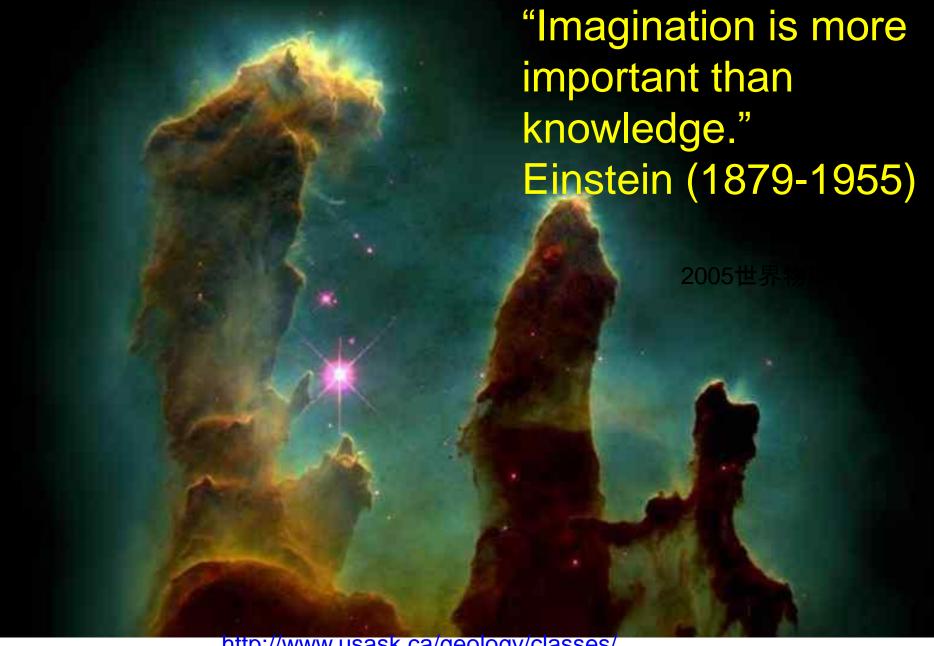
愛迪生



http://utopia.utexas.edu/ project/portraits/edison.jpg 與



http://www.cec.mtu.edu/csa/pegasus/einstein.jpg



http://www.usask.ca/geology/classes/

geol109and122/109_122_A/Eagle_nebula.jpg

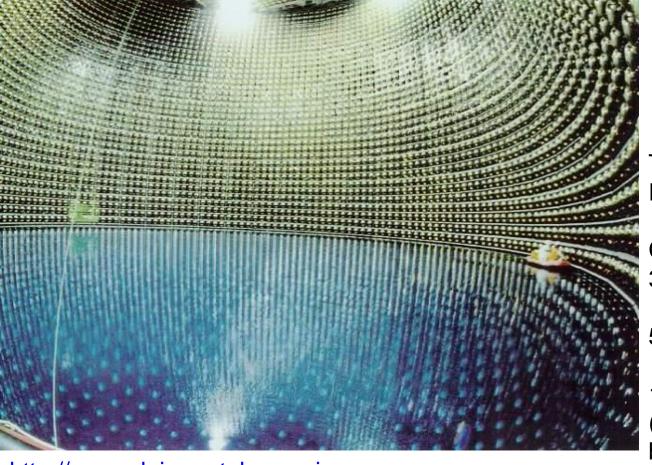
Everything is physics 舉目所見皆是物理 J. Schwinger

- •Matter Physics 物質物理
 - •Bio-Physics生命物理
 - •Social Physics社會物理

•[孔德 Auguste Comte, 1798-1857]

Auguste Comte: Weathering a Storm of Change Social Physics

What sort of person would invent sociology? Certainly someone living in times of momentous change. Comte (1798-1857) grew up in the wake of the French Revolution, which brought a sweeping transformation to his country. And if that wasn't sufficient, another revolution was under way as factories were sprouting up across continental Europe, recasting the lives of the entire population. Just as people enduring a storm cannot help but think of the weather, so those living during Comte's turbulent era became keenly aware of the state of society. Drawn from his small hometown by the bustle of Paris, Comte was soon deeply involved in the exciting events of his time. More than anything else, he wanted to understand the human drama that was unfolding all around him. Once equipped with knowledge about how society operates, Comte believed, people would be able to build for themselves a better future. He divided his new discipline into two parts: how society is held together (which he called social statics) and how society changes social dynamics) From the Greek and Latin words meaning "the study of society," Comte came to describe his work as sociology.



http://www-sk.icrr.u-tokyo.ac.jp/sk/photo/sk_build44.jpg

The 2002 Nobel Prize in Physics

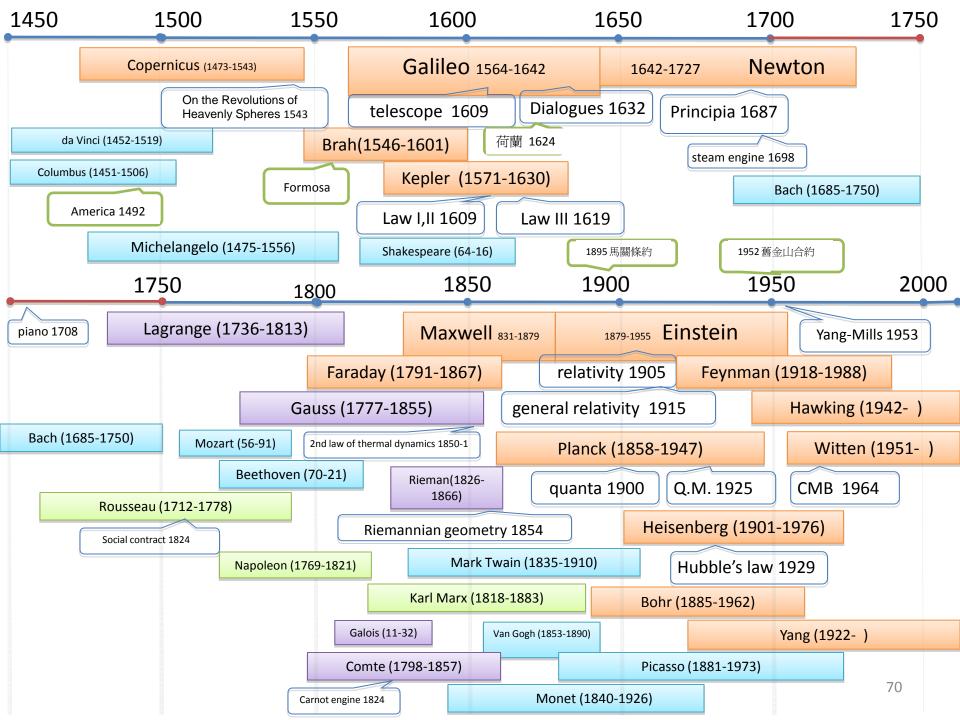
Cylinder of 41.4m (Height) x 39.3m (Diameter)

50,000 tons of pure water

11,200 photomultiplier tubes (50cm each in diameter -the biggest size in the world)

岐阜県吉城郡神岡町(神岡宇 鉱業 茂住坑 地下1,000m)

所有大型實驗原始目的皆未達成,但是,都找到更好的。



造物主早就告訴我們生存知道







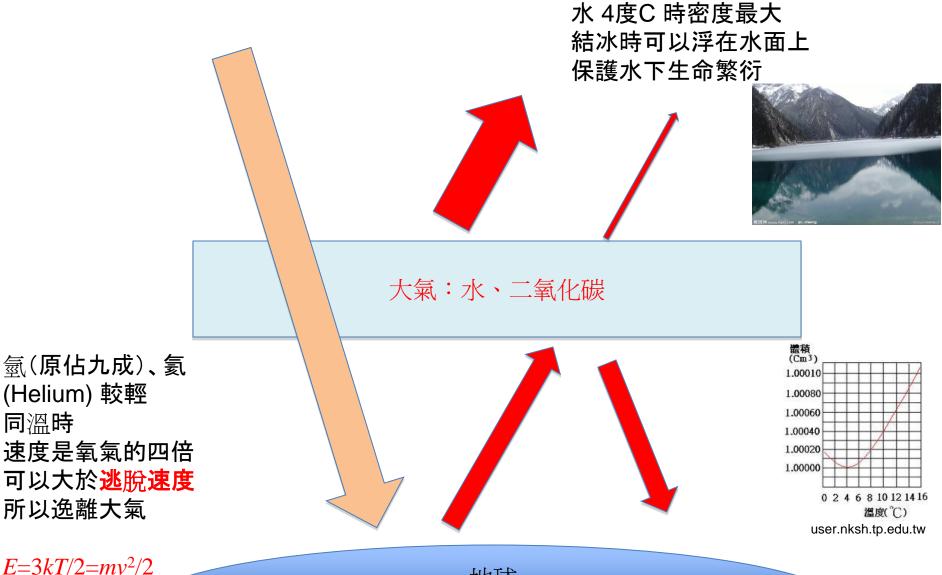
真理無所不在

能源小常識: 各盡所能 各取所需

地球受日照功率約為 1 GW/平方公里

約爲現有核電廠一個機組功率~1 GW

每平方公里太陽能~核電廠功率 Muller: physics for future presidents

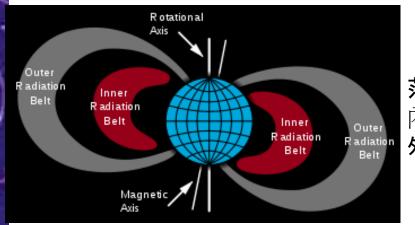


 $E=3kT/2=mv^2/2$ = GmM/r

所以逸離大氣

(Helium) 較輕

同溫時



禁衛軍

范艾倫輻射帶

內:100~1萬公里

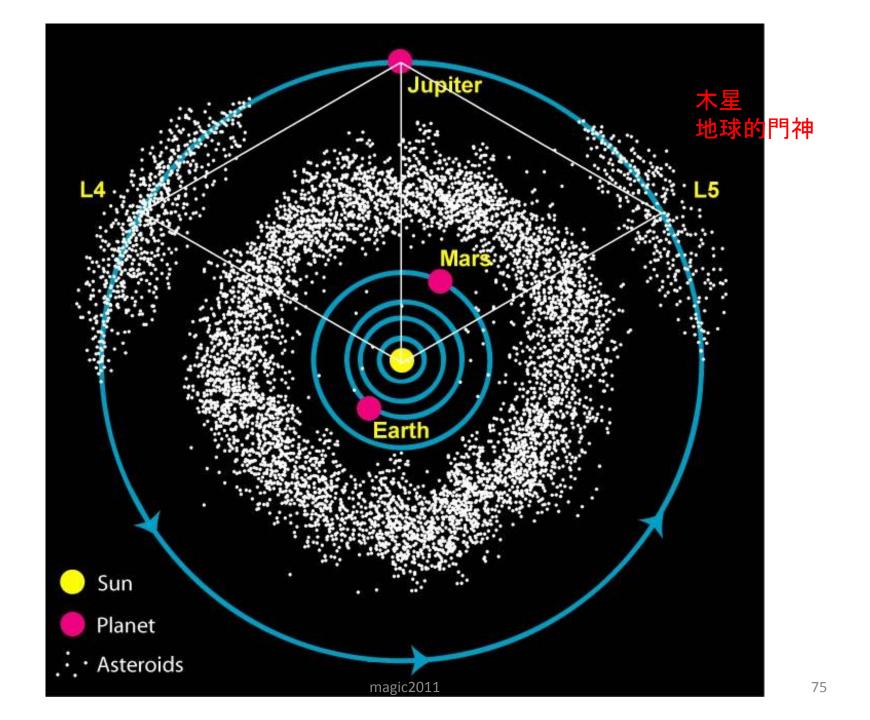
外:1.3萬~6萬公里

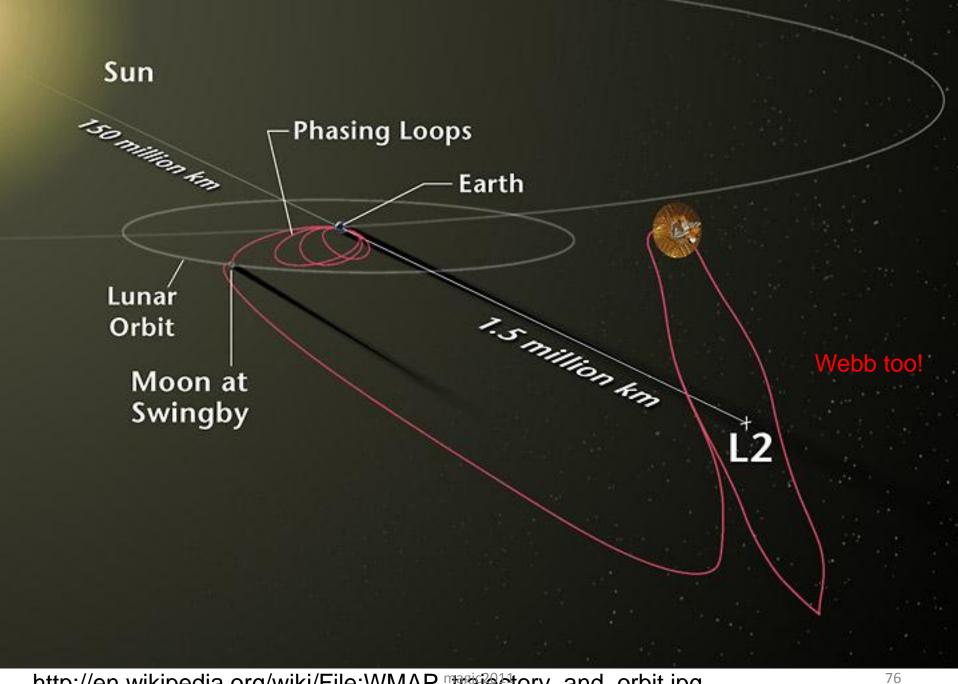


人造磁場~10^{6~7}高斯 中子星磁場~10^{12~13}高斯 地表磁場~0.5高斯

地球大氣層外的磁層示意圖

太陽風(是一大群時速達4~500 Km/hr的電漿)





如何儲藏能源 上帝的秘方

巧克力~8黃色炸藥~5大卡/克

汽油 ~15黃色炸藥

氫氣 ~40黃色炸藥

~2.6汽油/g

~0.18汽油/cc

燃料	1KWh 的價格	轉換成 1kWh電力
煤	0.4¢	1.2¢
天然氣	0.9¢	2.7¢
汽油	7¢	21¢
電力	10¢	10¢
車用電池	21¢	21¢
Pc電池	\$4	\$4
AAA電池	\$1000	\$1000

波音瓦=747 W~1馬力 (3600J=)1Wh~1大卡 (=4200J) 不休息的鴿子 反應速度的極限

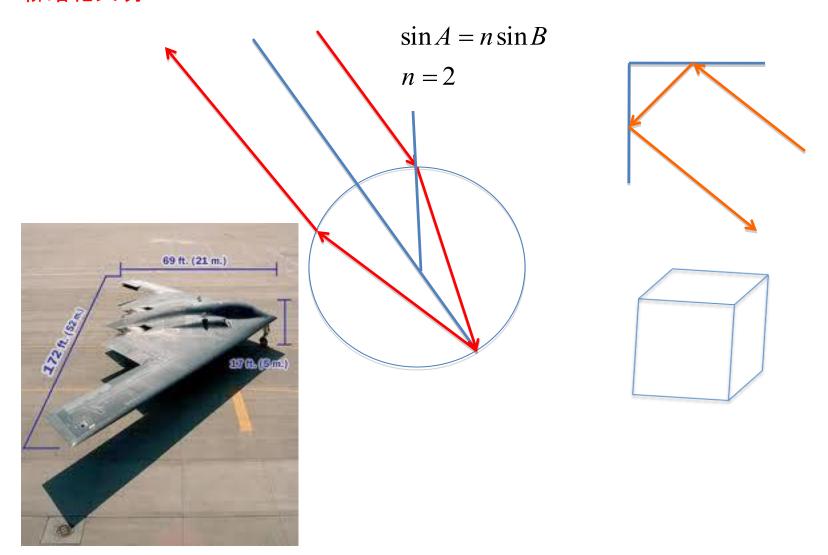


kenming.idv.tw

tieba.baidu.com

#至Moobol.com 已基本版权

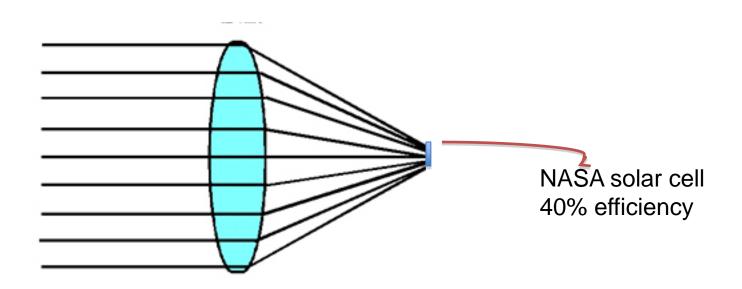
腦筋轉一轉 柳暗花又明



science.howstuffworks.com



gropius-passagen.de



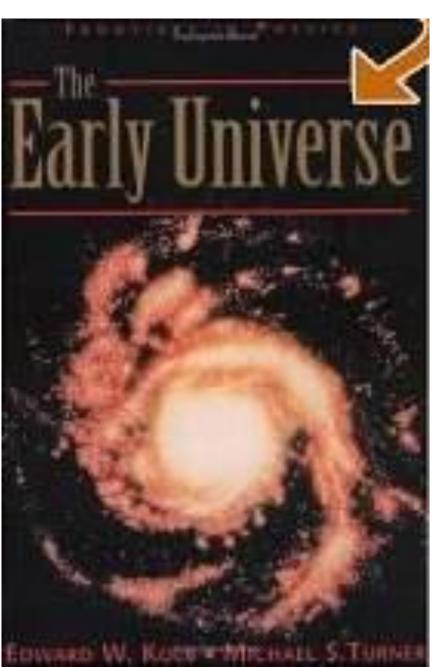
STEVEN WEINBERG

Winner of the 1979 Nobel Prize for Physics

A Modern View of the Origin of the Universe http://www.th.physik.uni-frankfurt.de/

~jr/gif/phys/weinberg.jpg

The Early Universe (Frontiers in Physics)

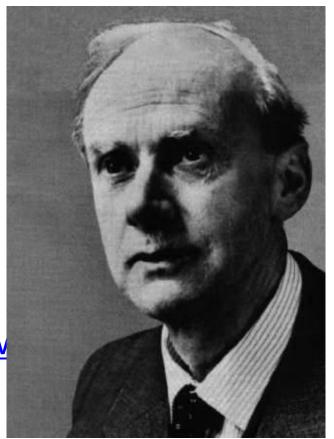


Turner "Our current understanding of the evolution of the Universe is based upon the Friedmann-Robertson-Walker (FRW) cosmological model, or the hot big bang model as it..." (more)

General Theory of Relativity yes, no, not-a-question

by <u>Paul Adrien Maurice Dirac</u>
 "For the space-time of physics we need four coordinates, the time t and three space coordinates x, y, z..." (<u>more</u>)

• <u>廣義相對論</u> 講義
http://www.cc.nctu.edu.tw/~wgore/apple2.htm



一棵開花的樹/席慕容

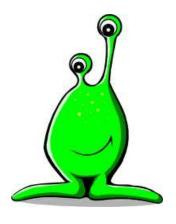
如何讓你遇見我 在這最美麗的時刻 為這 我已在佛前 求了五百年 求祂讓我們結一段塵緣

佛於是把我化作一棵樹 長在你必經的路旁 陽光下慎重地開滿了花 朵朵都是我前世的盼望 Feynman 說教書 會讓自己覺得自己是有用的人 所以先謝謝大家搭乘企業號 讓我有機會變成有用的人

當你走近 請你細聽 那顫抖的葉是我等待的熱情 而當你終於無視地走過 在你身後落了一地的 朋友啊 那不是花瓣 是我凋零的心



ladyous.blogspot.com

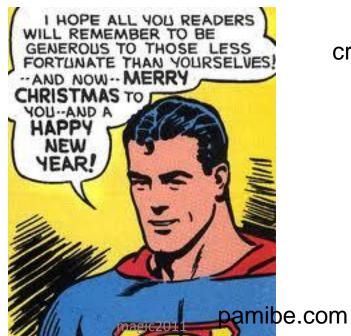


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forum.mymaji.com



cryptomundo.com

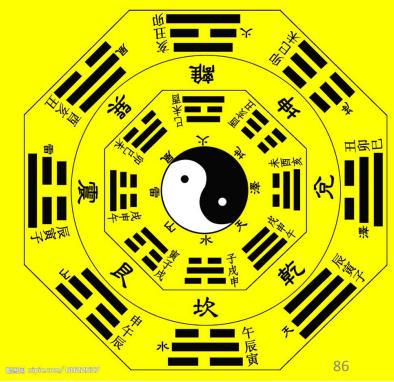


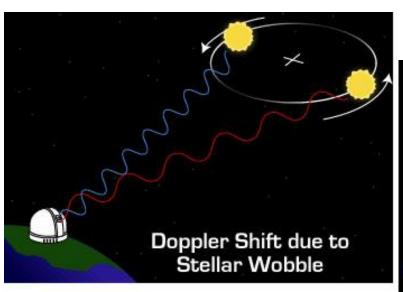


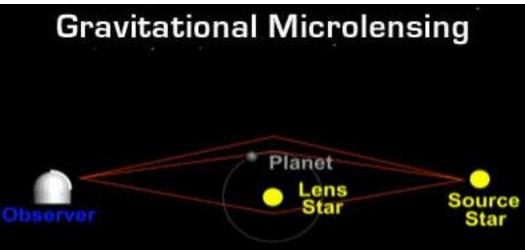
http://tw.myblog.yahoo.com/jw!y7hFqz.RGhjUF9c.EIA8ztQ-/article?mid=977&prev=978&next=976



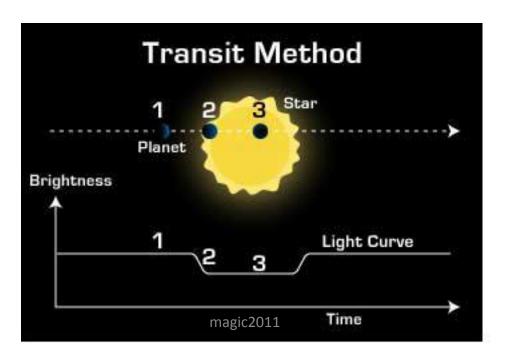
http://egland.com/viewthread.php?tid=2727 捷哀2011



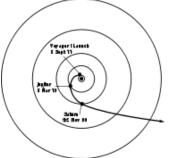




http://planetquest.jpl.nasa.gov/science/finding _planets.cfm



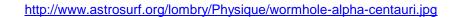




As of April 21, 2011, Voyager 1 was about 116.825 AU, or about 0.00183 light-year from the Sun.

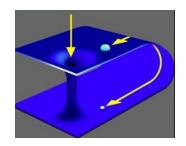
magic2011

m http://en.wikipedia.org/wiki/File:Voyager.jpg The Voyager 1 spacecraft is a 722kilogram (1,592-lb) robotic American space probe launched by NASA on September 5, 1977, to study the outer Solar System and eventually interstellar space. Operating for 33 years, 7 months, and 28 days, the spacecraft receives routine commands and transmits data back to the Deep Space Network. It is the first probe to leave the Solar System and is the

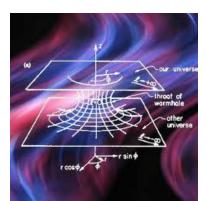




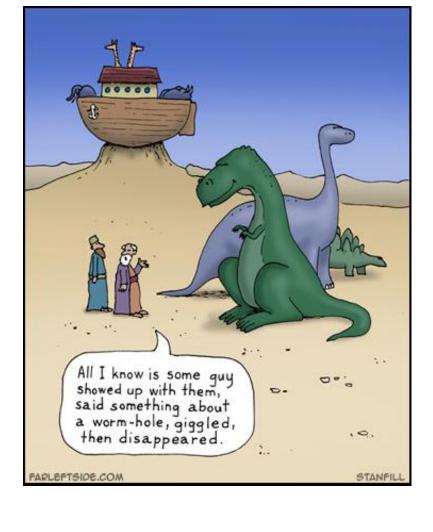
time-travel.over-blog.com



tribalwar.com

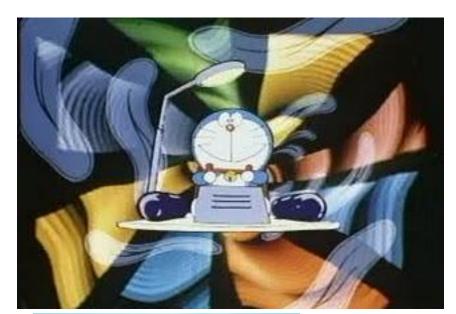


paranormalspy.com







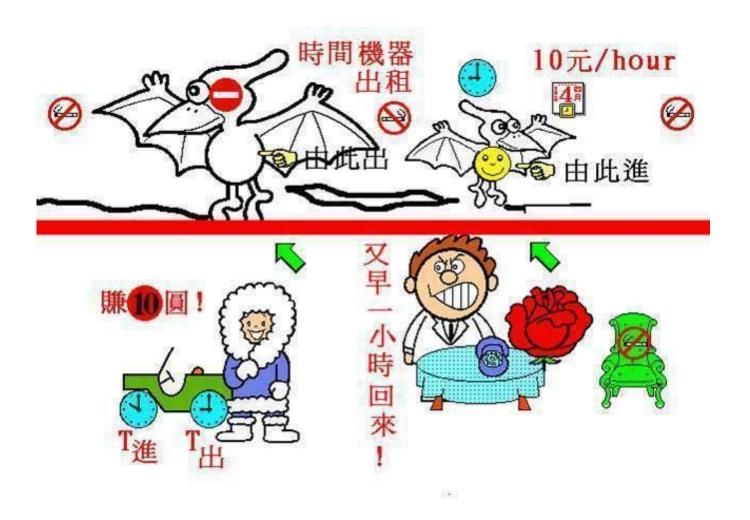




http://idiothink.blogspot.com/2009/09/dorae mon-d.html



台北八景



一棵開花的樹/席慕容

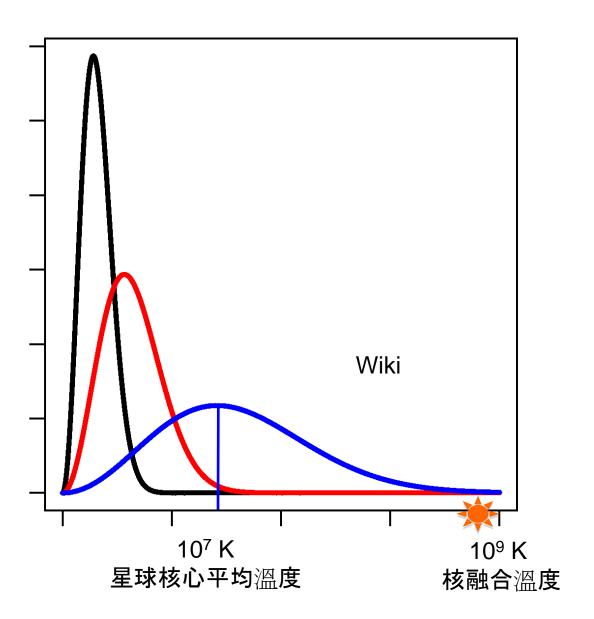
如何讓你遇見我 在這最美麗的時刻 為這 我已在佛前 求了五百年 求祂讓我們結一段塵緣

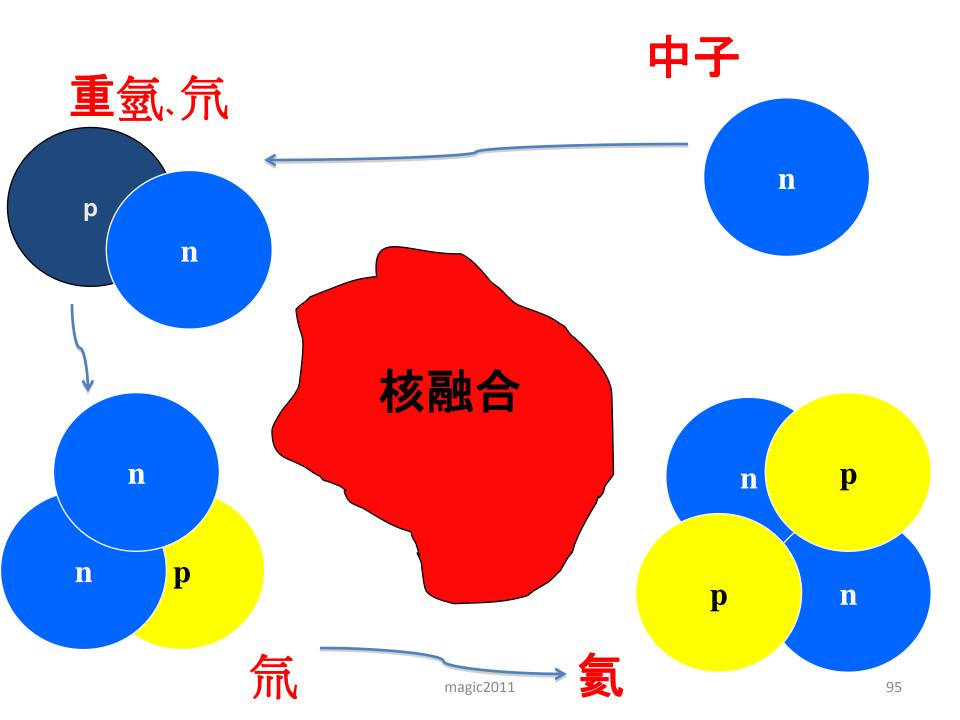
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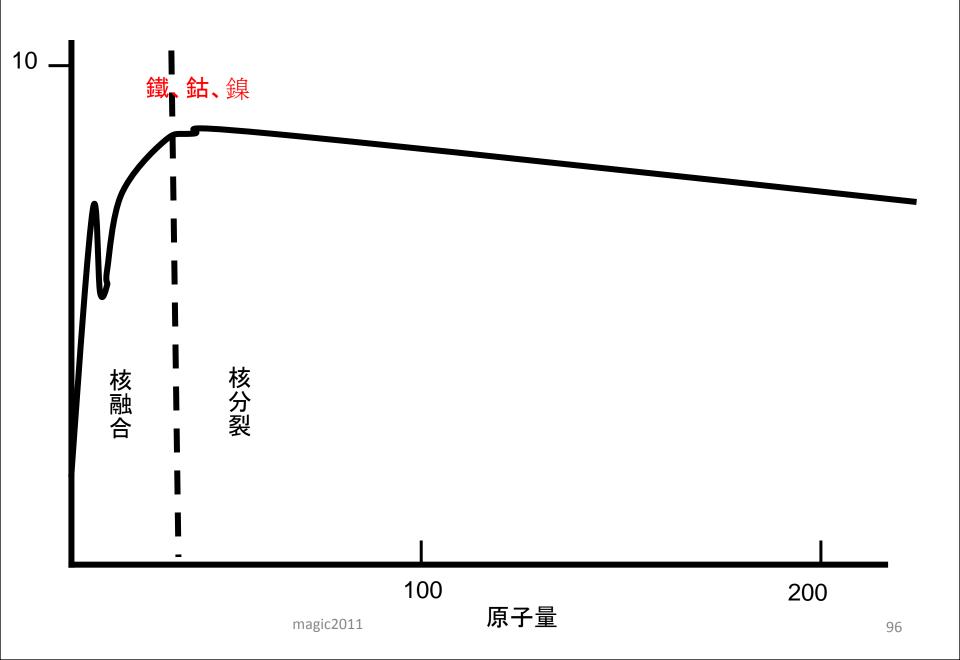
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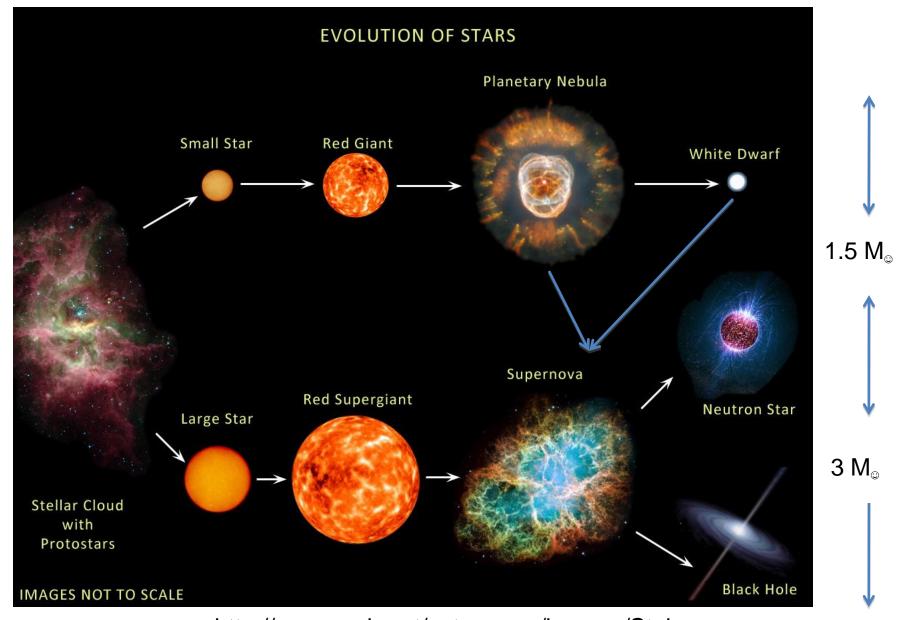


$$f(v) = \exp\left[-\frac{mv^2/2}{kT}\right]$$









http://essayweb.net/astronomy/images/Stellar_Evolution_large.jpg

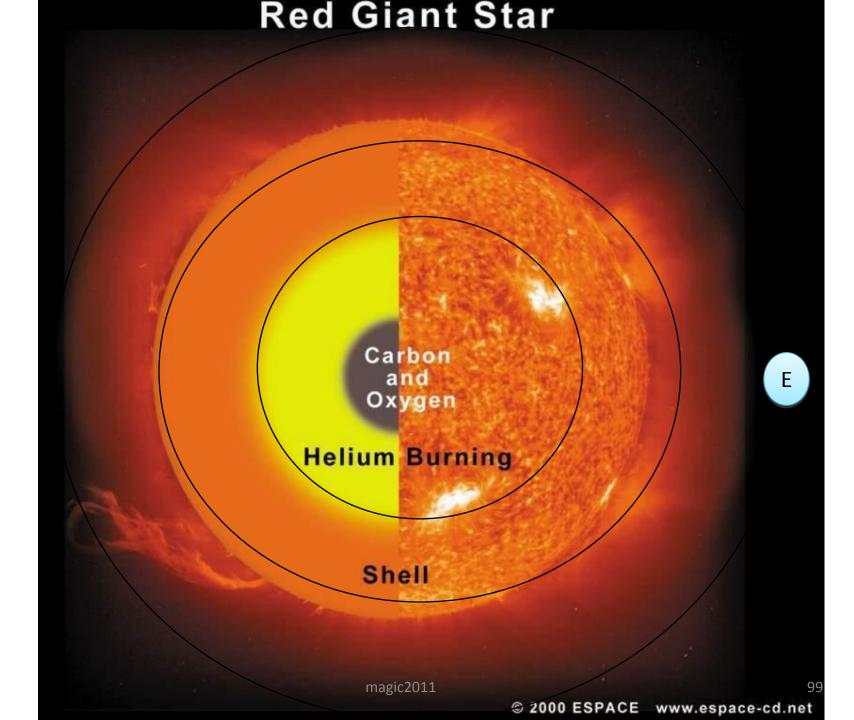


■包利 (Pauli)作用力或稱簡併力: 兩個費米子(fermion)無法處於同 一個量子態

Compton Wavelength 康卜吞波長

電子 electron $\lambda_e = h/m_e c$ ~2.426 × 10⁻¹² m

中子 neutron λ_p =h/m_nc ~1/2000 λ_e ~ 1.319 × 10⁻¹⁵ m





星雲中心的熾熱天體就是白矮星行星狀星雲通常在數千年後就會消散掉留下一顆暗、冷的白矮星



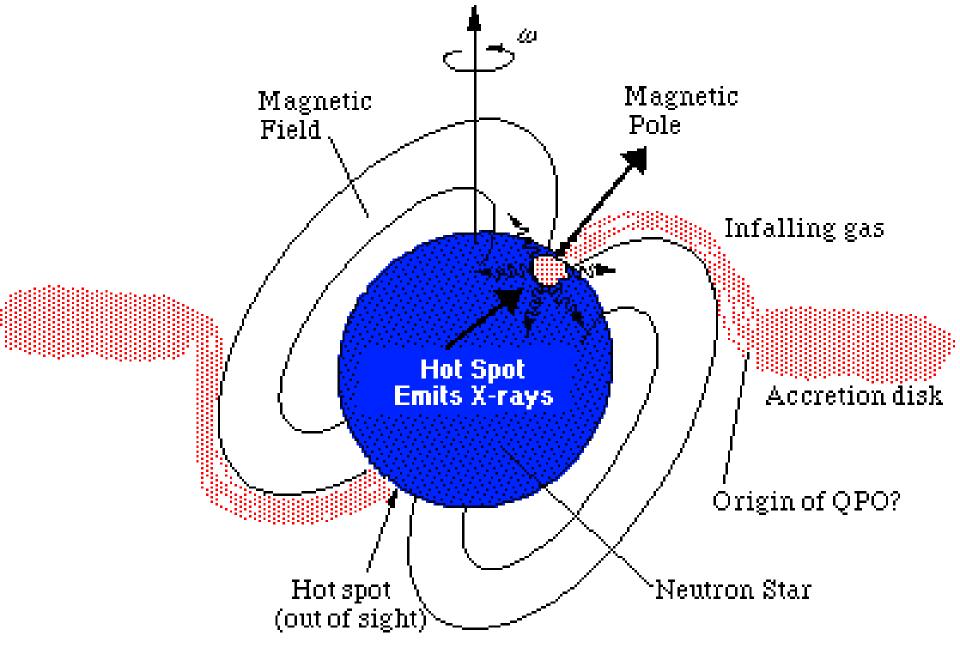
(HST/NASA)

太陽若形成。。。其半徑約為

• 白矮星 地球大小

中子星 6公里

• 黑 洞 3公里





he Nobel award to Ryle and Hewish without the inclusion of Bell as a co-recipient was controversial, and was roundly condemned by Hewish's fellow astronomer Fred Hoyle. Others, however, have noted that the prize was given to Ryle and Hewish for their work across the field of radio-astronomy as a whole, with particular mention of Ryle's work on aperture-synthesis, and Hewish's on pulsars.

http://www.lbl.gov/Science-Articles/ Archive/sb/Nov-2004/03-Bell_radiot elescope.jpg

Jocelyn Bell Burnell

Antony Hewish

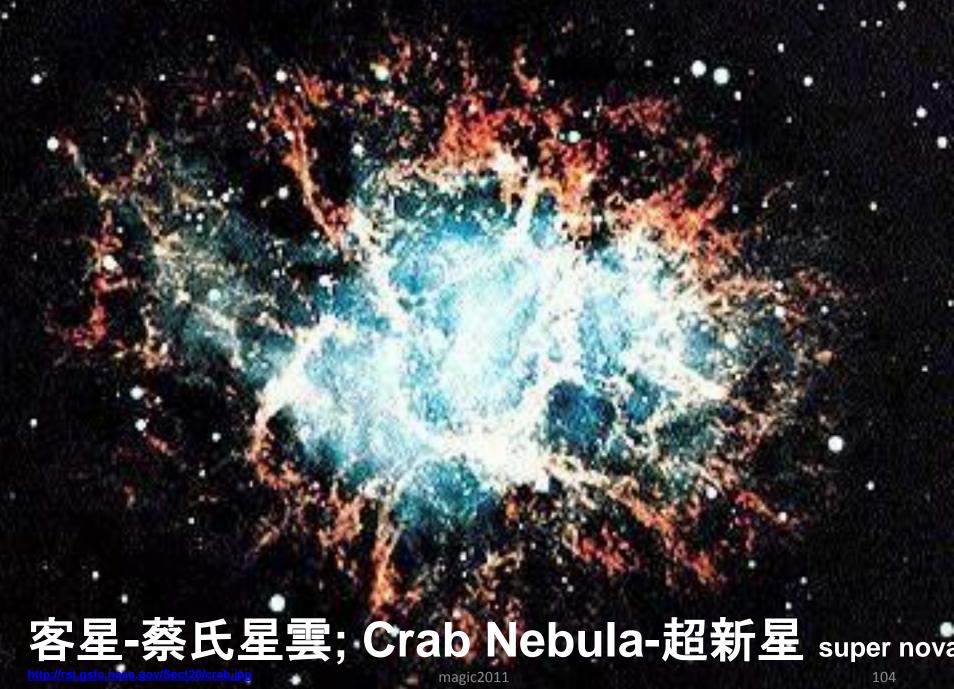
Nobel Prize for Physics (1974)





tagsup.com

wiki



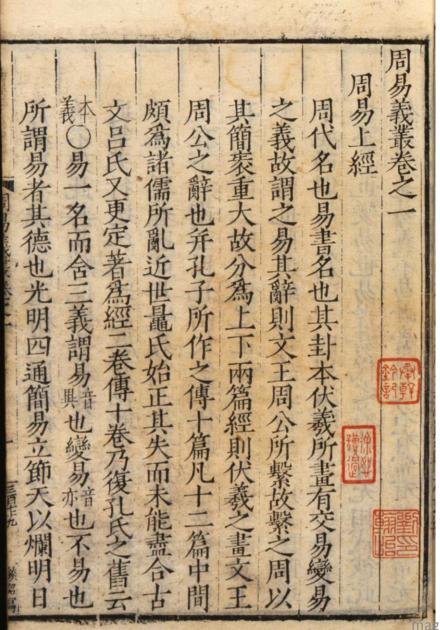


http://aeea.nmns.edu.tw/ geo home/geo 93/126.jpg http://hanyu.icib a.com/wiki/445 62.shtml

司天監言自至和元年五月客星晨出東方空

西元1054年 宋史

客星 至和元年五月已丑, 出天關東南, 可數寸, 歲餘稍沒



西元1054年 宋至和 元年五月已丑

・宋史

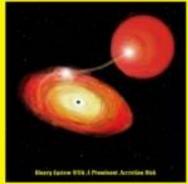
客星出天關東南, 可數寸, 歲餘稍沒

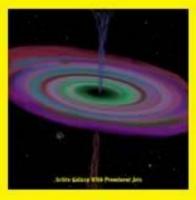


HST/NASA http://rst.gisfc.nasa.gov/Sect20/sn87ba.jpg

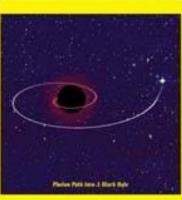
STARCHILD presents...











Continued Presented Stell of A Mark Sale











Paycheck 記憶裂痕

預知未來,就不會有未來 預知戰爭,想阻止戰爭,就會引發戰爭 預知疾病,集中管理,最後引發瘟疫失控

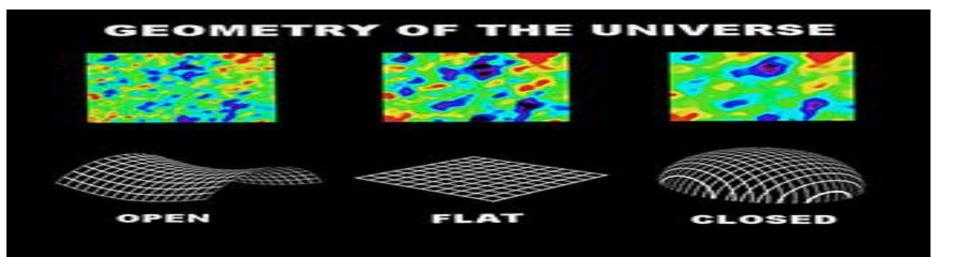
物理最美好的一面, 就是無法 確定預知未來 最美好的記憶, 就是自己的缺點



長度/Mikowski vs Friedmann-Robertson-Walker Spacetime

$$ds^{2} = -c^{2}dt^{2} + dx^{2} + dy^{2} + dz^{2} = -dt^{2} + dr^{2} + r^{2}d\theta^{2} + r^{2}\sin^{2}\theta d\varphi^{2}$$

$$= -dt^{2} + a^{2}(t) \left(\frac{dr^{2}}{1 - kr^{2}} + r^{2}d\theta^{2} + r^{2}\sin^{2}\theta d\varphi^{2} \right)$$



宇宙加速膨脹挑戰科學對時空的認識

