

從平面導體導電之研究 談 靜電學

主講：吳原旭

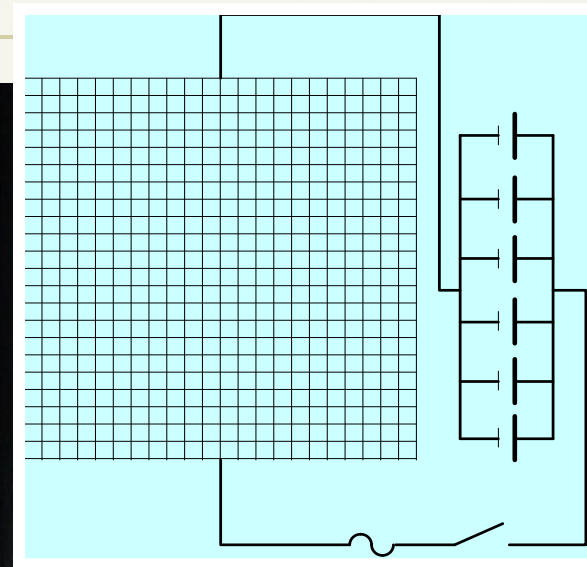
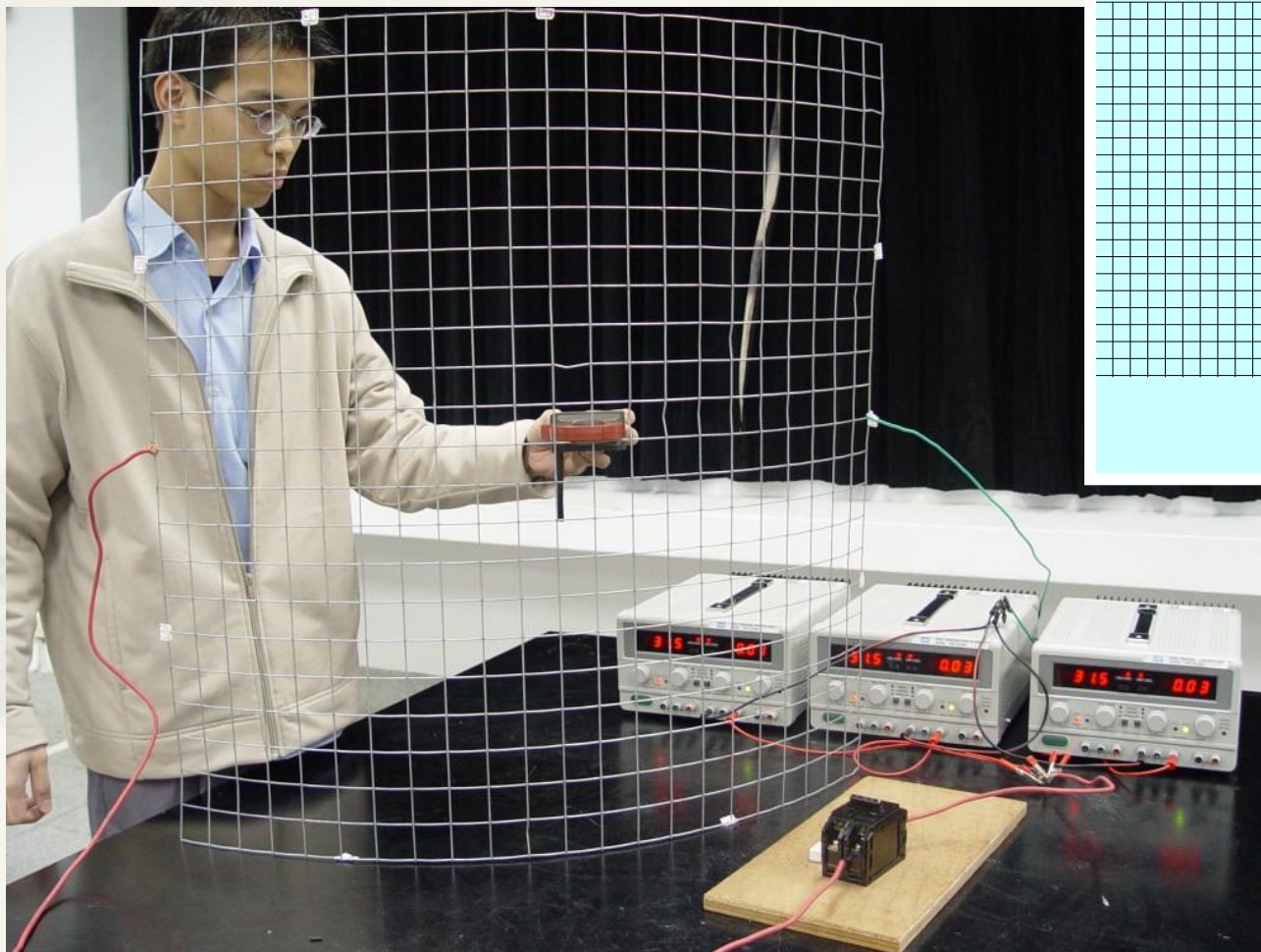
從平面導體導電之研究 談 靜電學

- * 研究如何進行？
- * 電流的強度
- * 克西荷夫結點定則
- * 克西荷夫迴路定則
- * 平方反比定律V.S反比定律
- * 邊界問題
- * 等電位線
- * 等電位線與電(流)場方向關係

網格電路之研究

- * 如何研究平面導體之導電問題？
如何測電流大小與方向
如何測電位(差)

以鉤表測電流



測量範圍及安全評估

- * 測量儀器的解析度？ **0.01A**
- * 通入多大電流才能測出明顯差異？ **37A**
- * 人體通過多少安培電流會致死？ **0.1A**
- * 安全嗎？

安全嗎？

爆火花的強電流

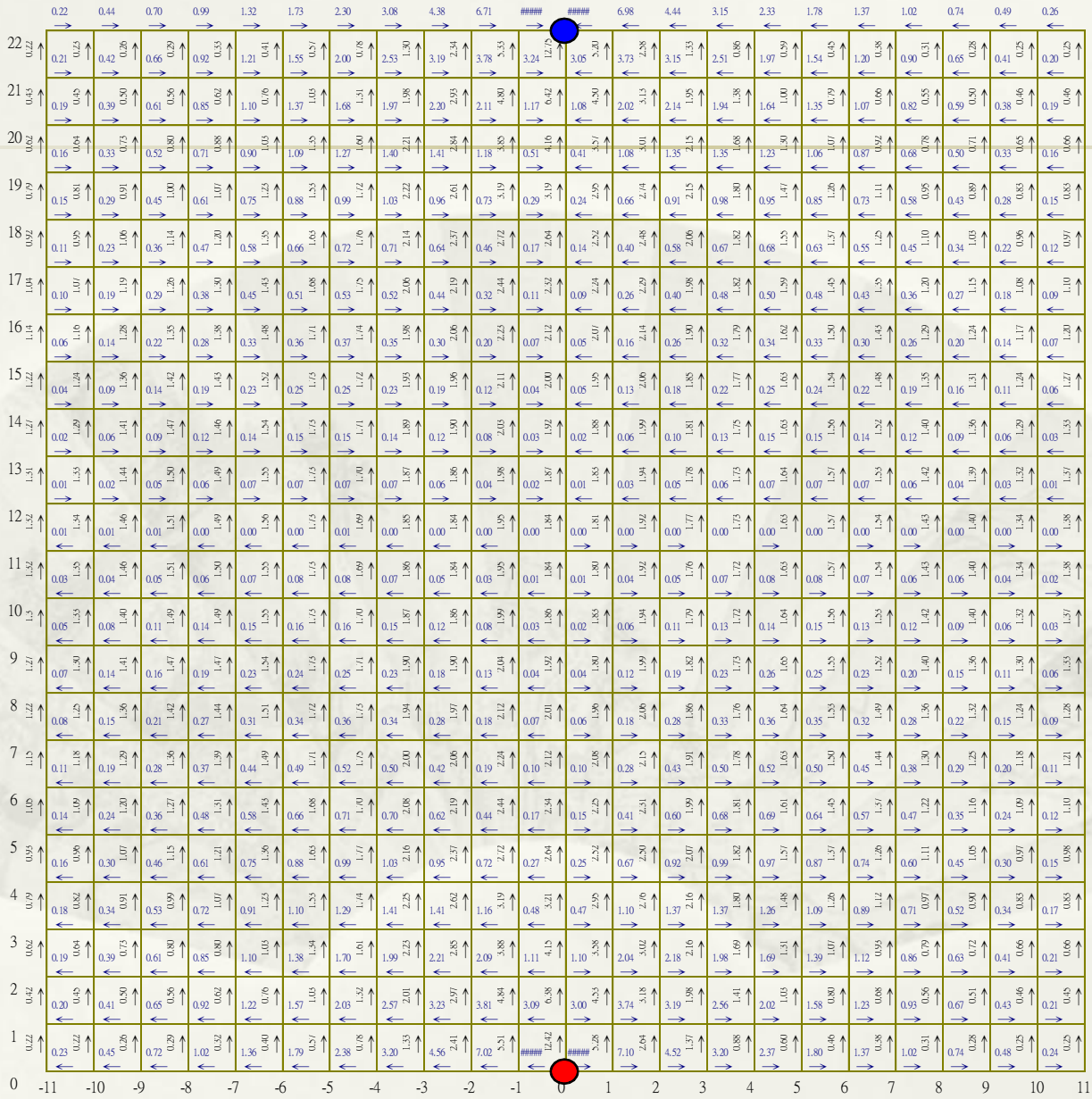
* 簡單的原理

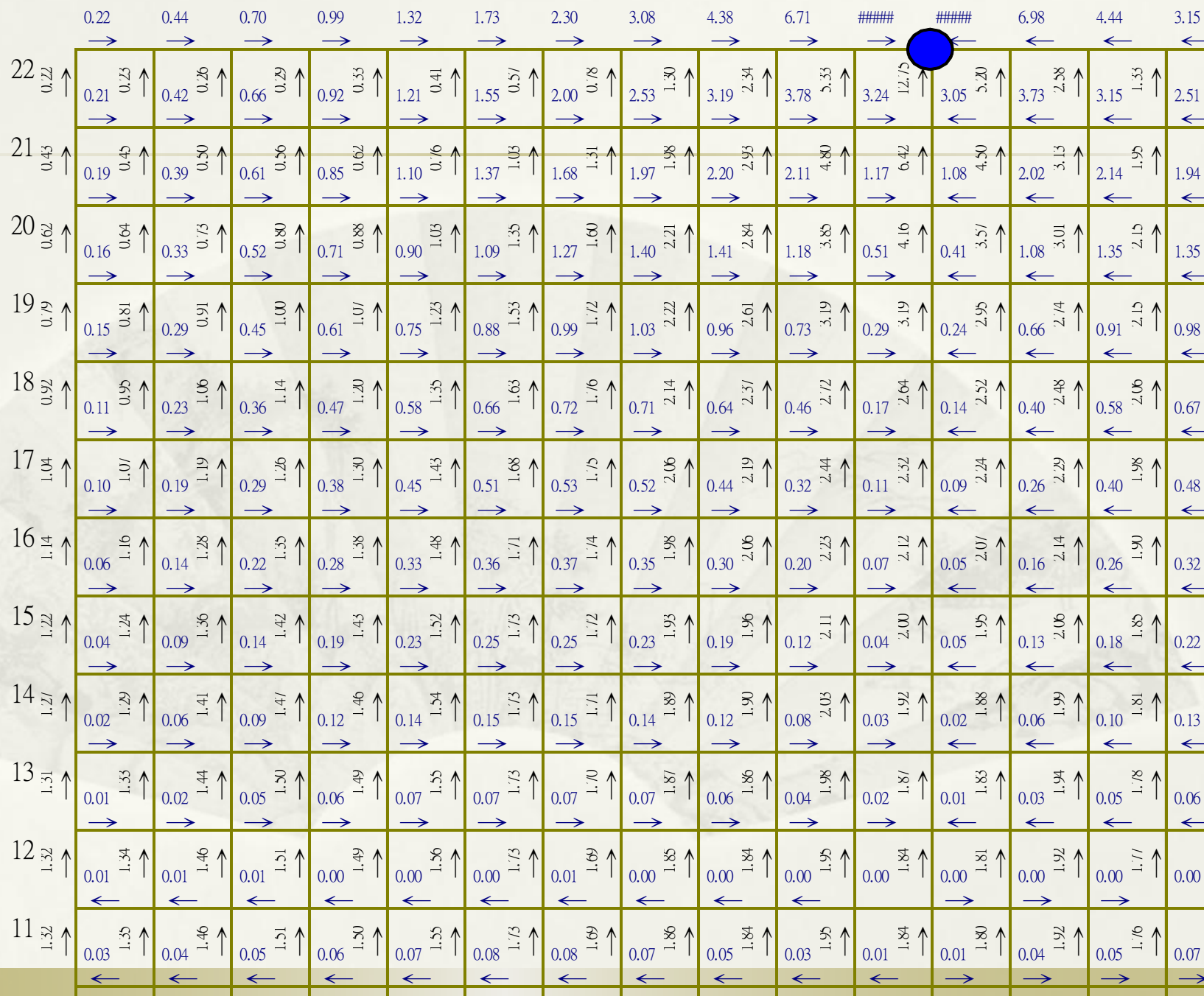
$$V=IR$$

V固定時 I與R成反比

鐵絲網電阻很小，只需 2V 電壓就能通過37A 電流。

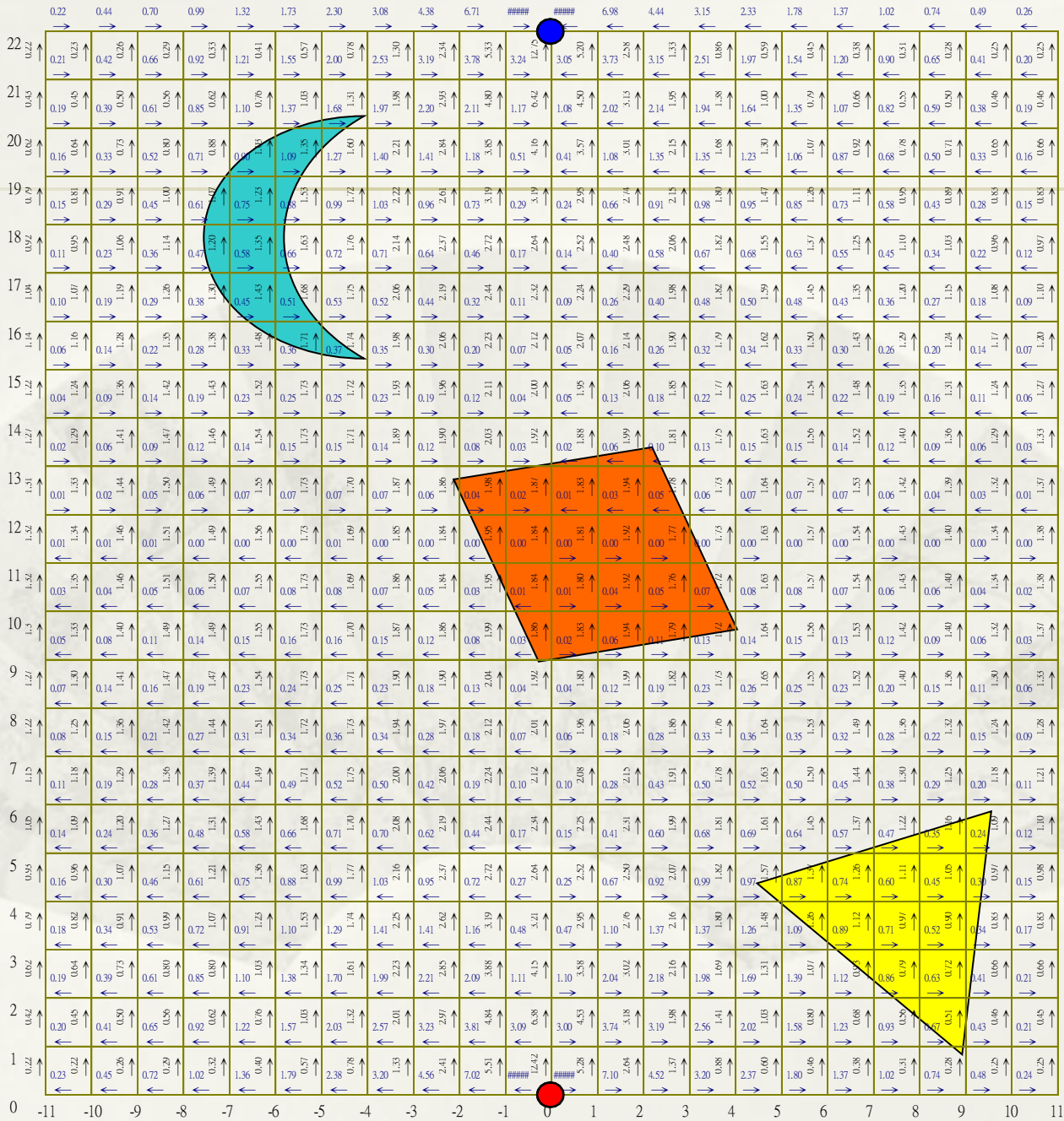
人體的電阻至少數萬歐姆，通過的電流極小。





同一結點的總進出電流淨值為零

		0.22	0.44	0.70	0.99	1.32	1.73	2.30	3.08
		→	→	→	→	→	→	→	→
22	0.22 ↑	0.21 → 0.23 ↑	0.42 → 0.26 ↑	0.66 → 0.29 ↑	0.92 → 0.33 ↑	1.21 → 0.41 ↑	1.55 → 0.51 ↑	2.00 → 0.78 ↑	2.53 → 1.30 ↑
21	0.43 ↑	0.19 → 0.45 ↑	0.39 → 0.50 ↑	0.61 → 0.56 ↑	0.85 → 0.62 ↑	1.10 → 0.76 ↑	1.37 → 1.03 ↑	1.68 → 1.31 ↑	1.97 → 1.98 ↑
20	0.62 ↑	0.16 → 0.64 ↑	0.33 → 0.73 ↑	0.52 → 0.80 ↑	0.71 → 0.88 ↑	0.90 → 1.03 ↑	1.09 → 1.35 ↑	1.27 → 1.60 ↑	1.40 → 2.21 ↑
19	0.79 ↑	0.15 → 0.81 ↑	0.29 → 0.91 ↑	0.45 → 1.00 ↑	0.61 → 1.07 ↑	0.75 → 1.23 ↑	0.88 → 1.53 ↑	0.99 → 1.72 ↑	1.03 → 2.22 ↑
18	0.92 ↑	0.11 → 0.95 ↑	0.23 → 1.06 ↑	0.36 → 1.14 ↑	0.47 → 1.20 ↑	0.58 → 1.35 ↑	0.66 → 1.63 ↑	0.72 → 1.76 ↑	0.71 → 2.14 ↑
17	1.04 ↑	0.10 → 1.07 ↑	0.19 → 1.19 ↑	0.29 → 1.26 ↑	0.38 → 1.30 ↑	0.45 → 1.43 ↑	0.51 → 1.68 ↑	0.53 → 1.75 ↑	0.52 → 2.06 ↑



克西荷夫結點定則

同一區塊的總進出電流淨值為零

$$\sum_i I_i = 0$$

克西荷夫迴路定則

任一迴路，沿途電位的總變化量等於0

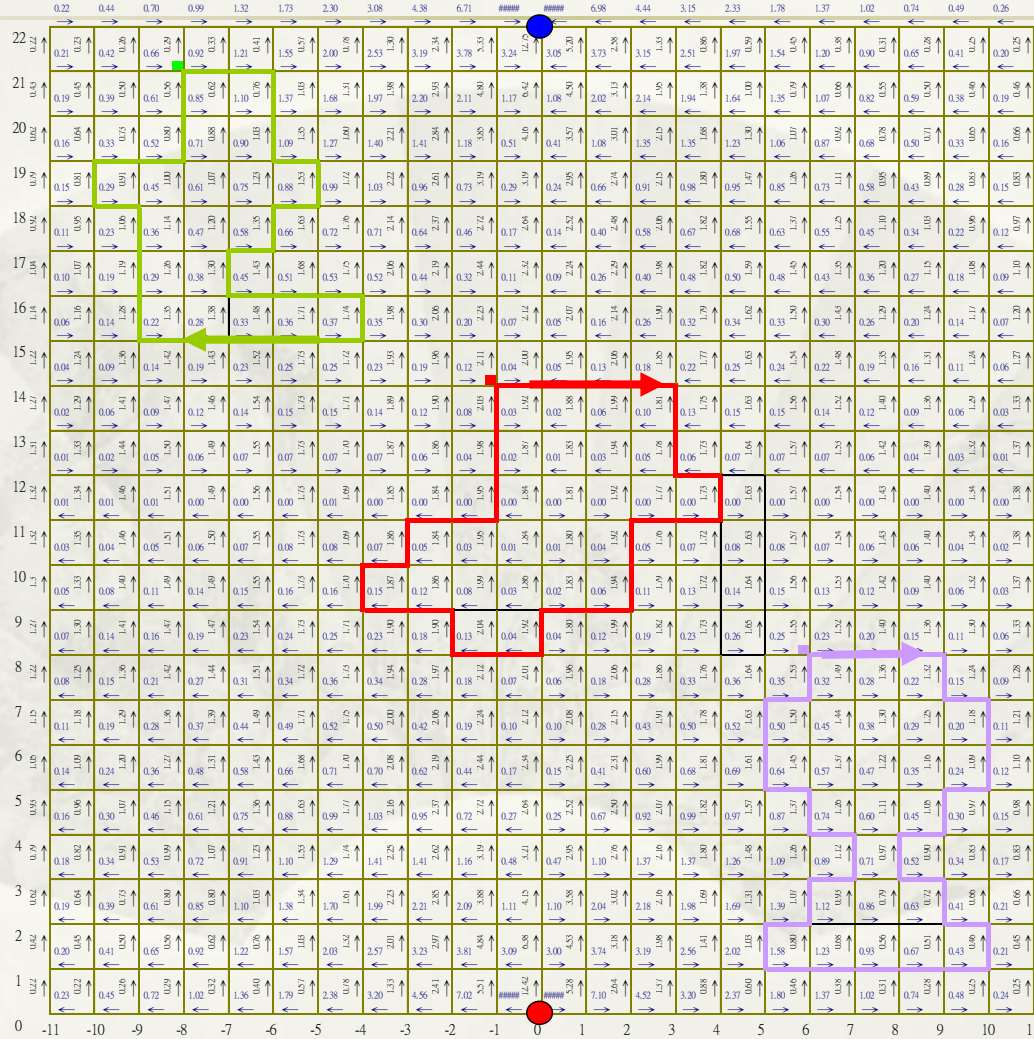
$$\sum_i \Delta V_i = 0$$

每一段導線兩端電位差 $\Delta V_i = I_i \times R_i$

假設每一小段鐵絲長度、粗細、材質均相同且焊接點之電阻可忽略，因此設每一小段電阻均為R。

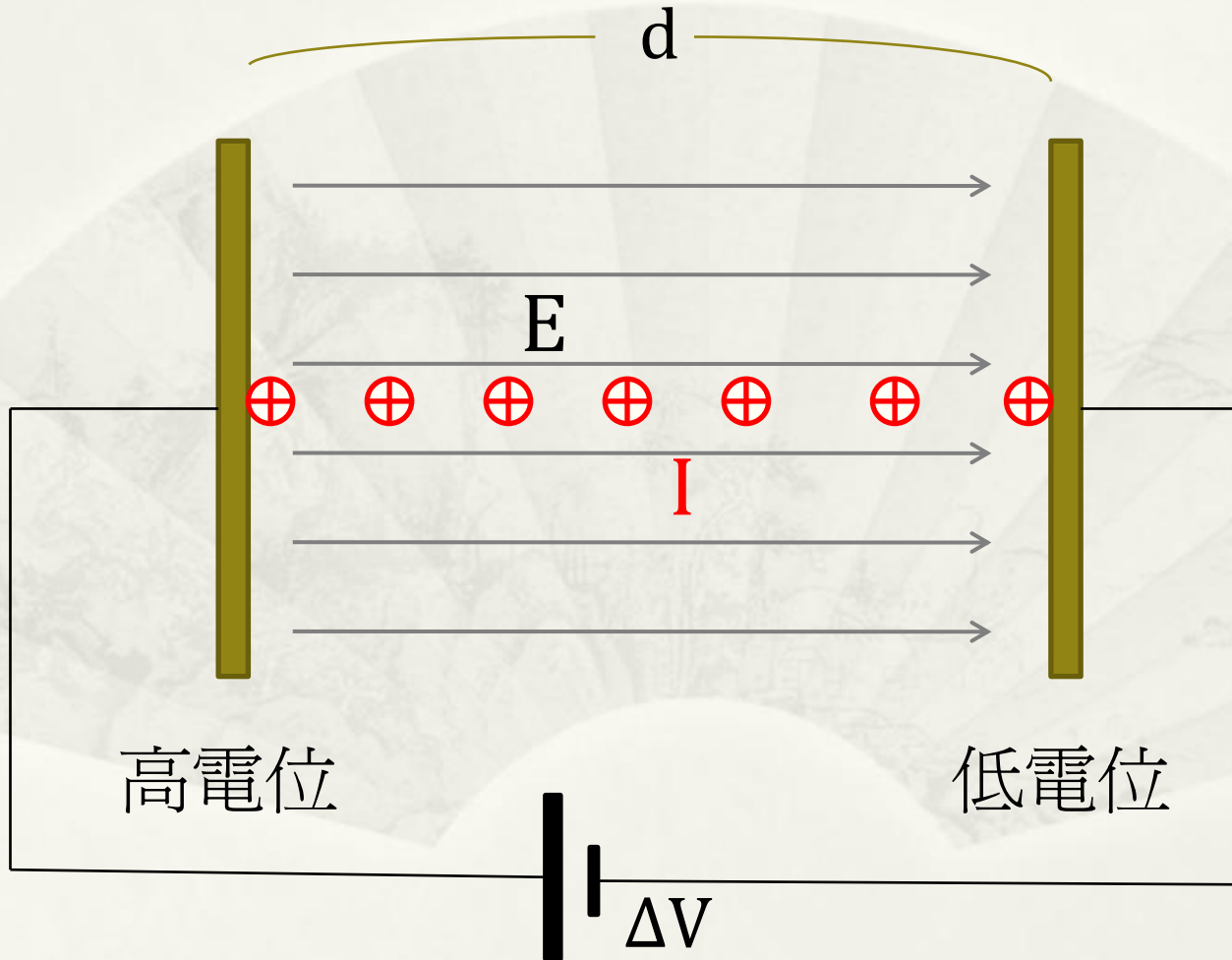
$$\begin{aligned} \sum_i (I_i \times R_i) &= 0 \\ \Rightarrow \sum_i (I_i \times R) &= 0 \Rightarrow R \times \sum_i I_i = 0 \\ \therefore \sum_i I_i &= 0 \end{aligned}$$

任一迴路，電流的總變化量等於0



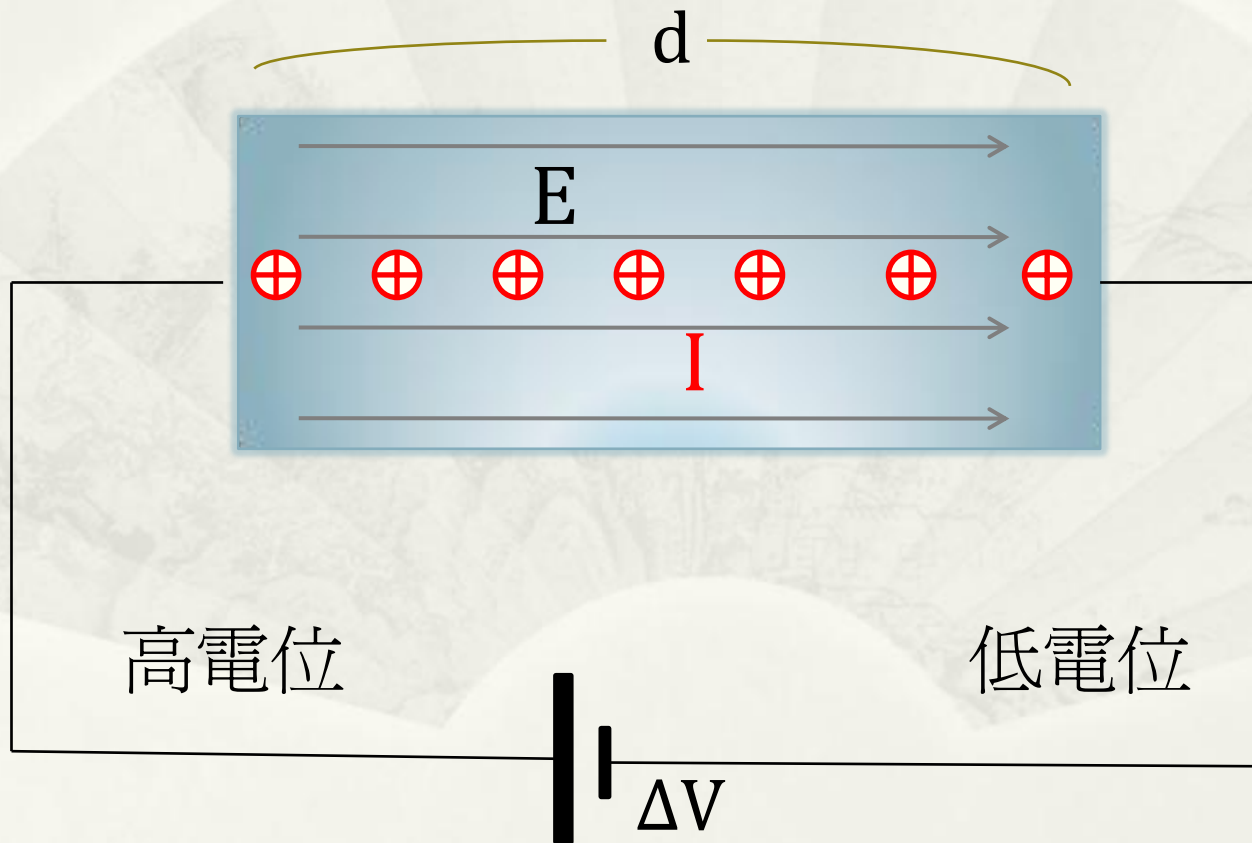


$$E \cdot d = \Delta V = I \cdot R$$



$$E \cdot d = \Delta V = I \cdot R$$

以金屬為介質，情形都一樣



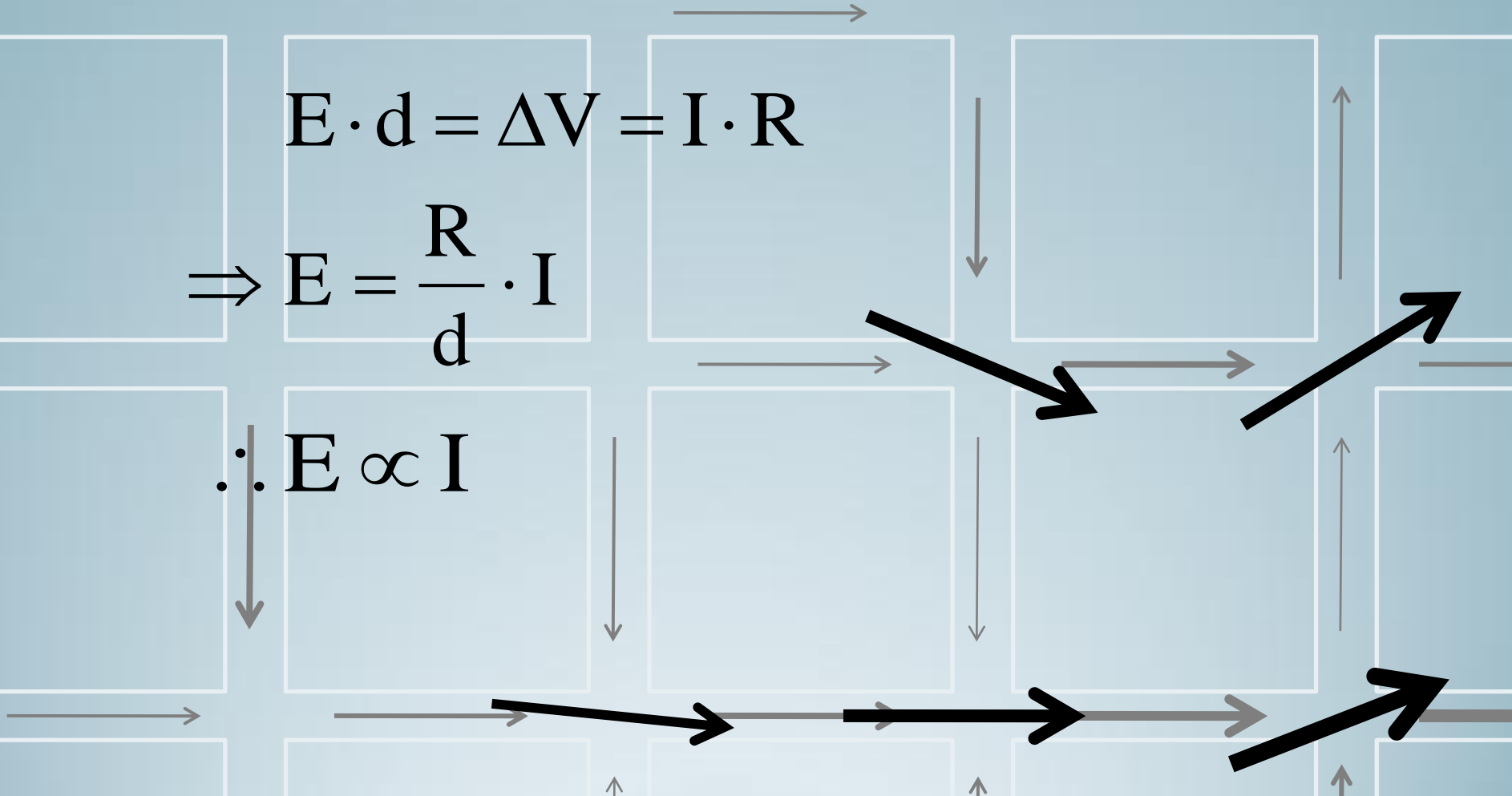
探討網格電路上的電流向量場

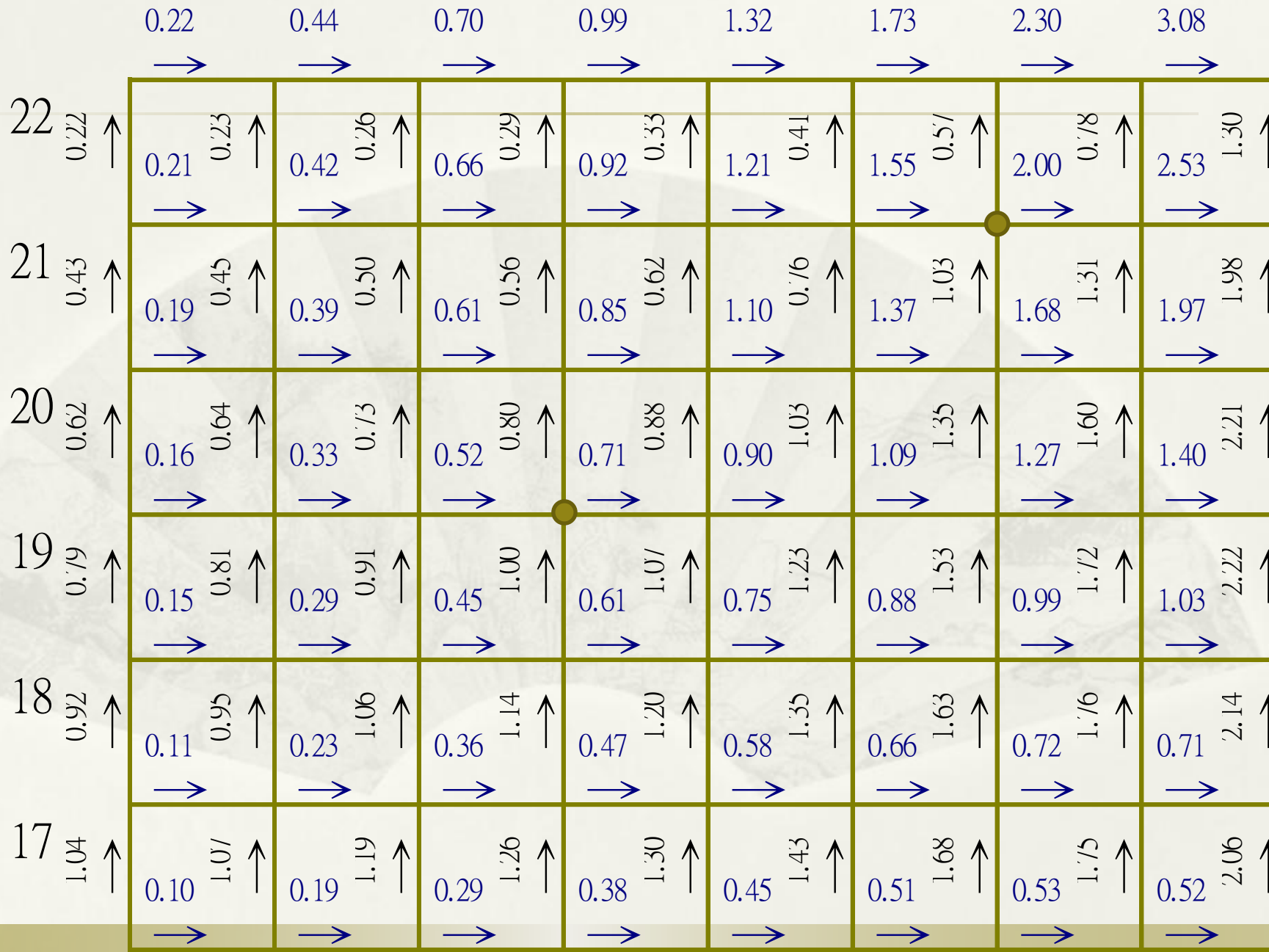
將每一小段鐵絲視為均勻導體

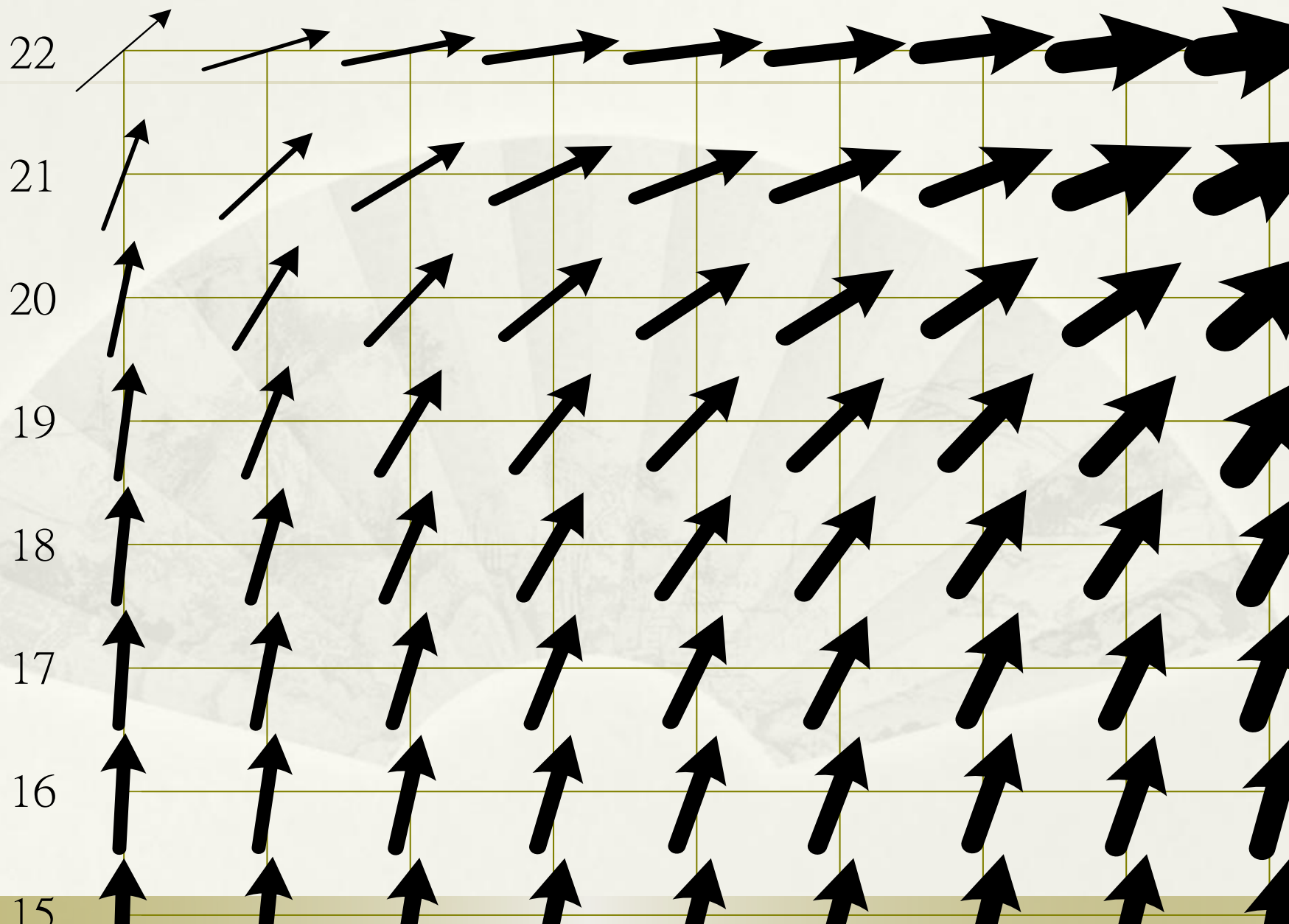
$$E \cdot d = \Delta V = I \cdot R$$

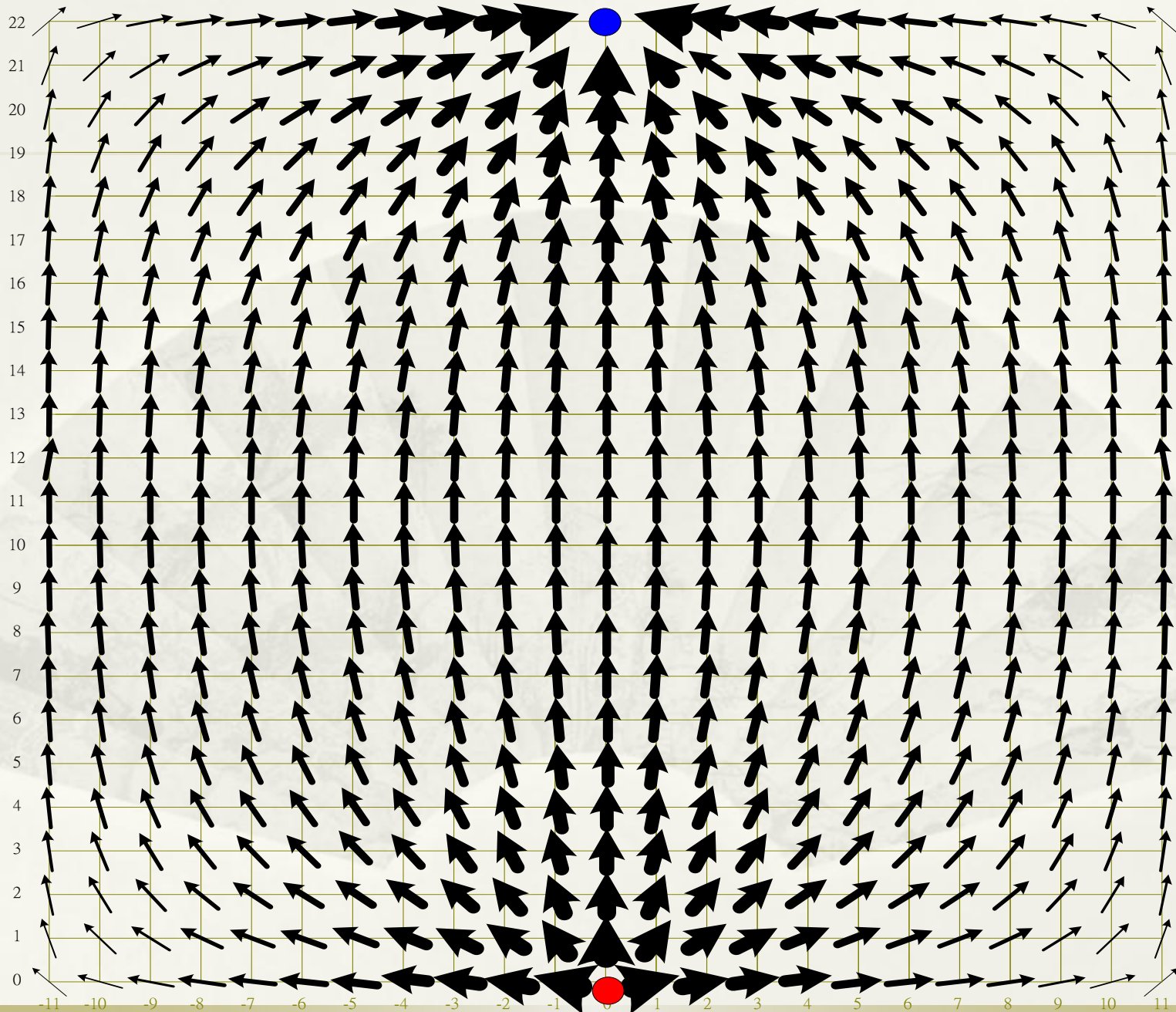
$$\Rightarrow E = \frac{R}{d} \cdot I$$

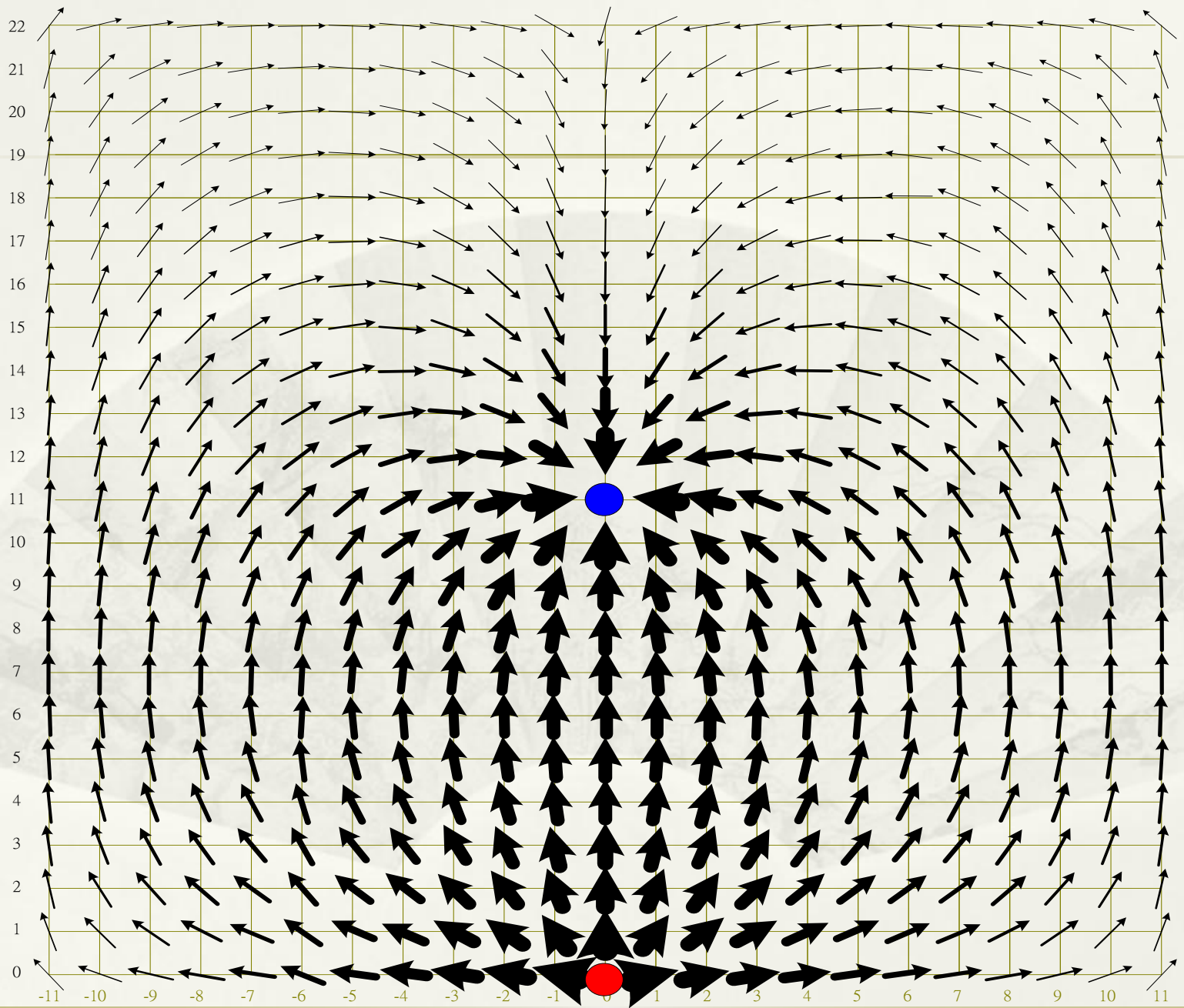
$$\therefore E \propto I$$

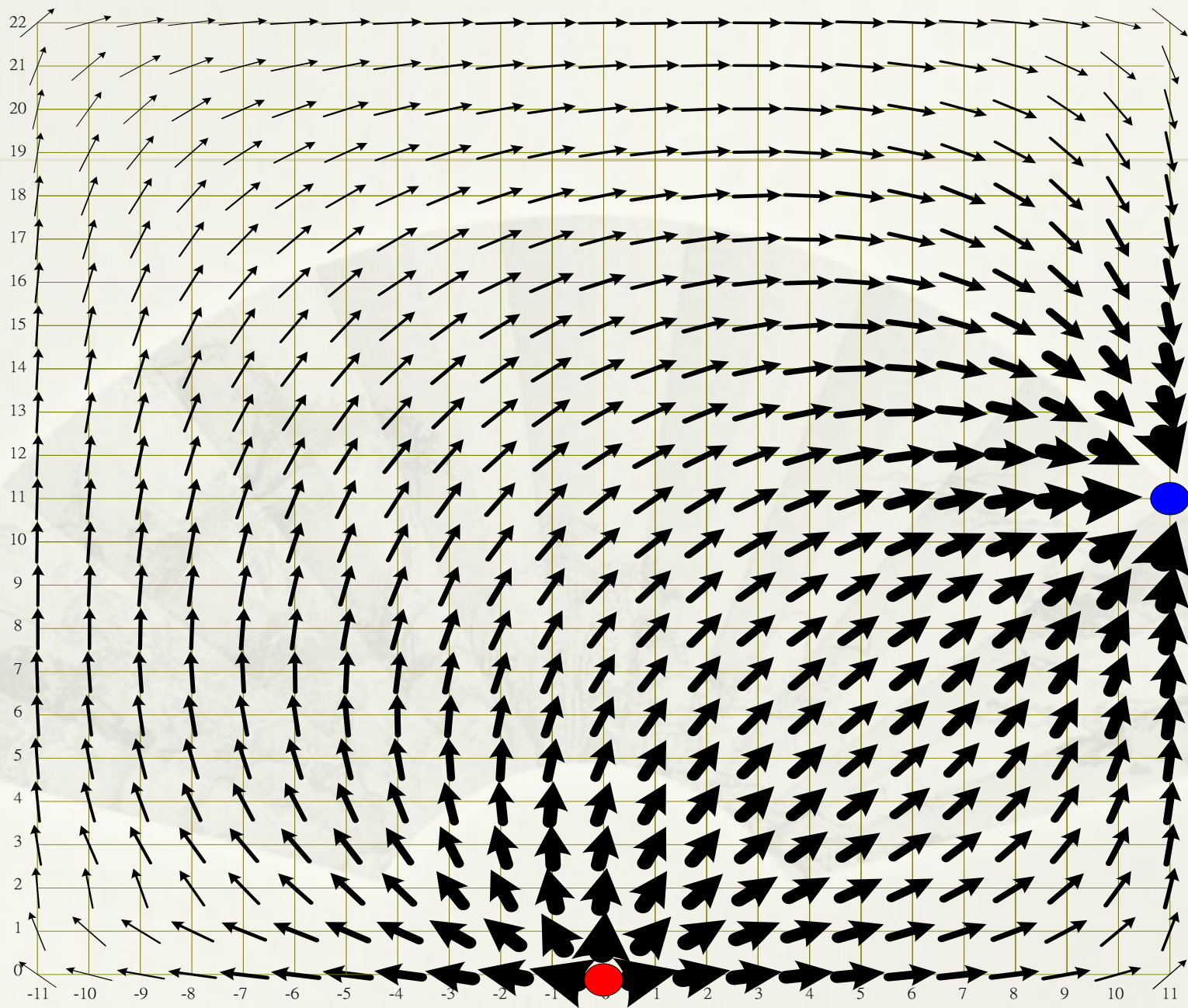


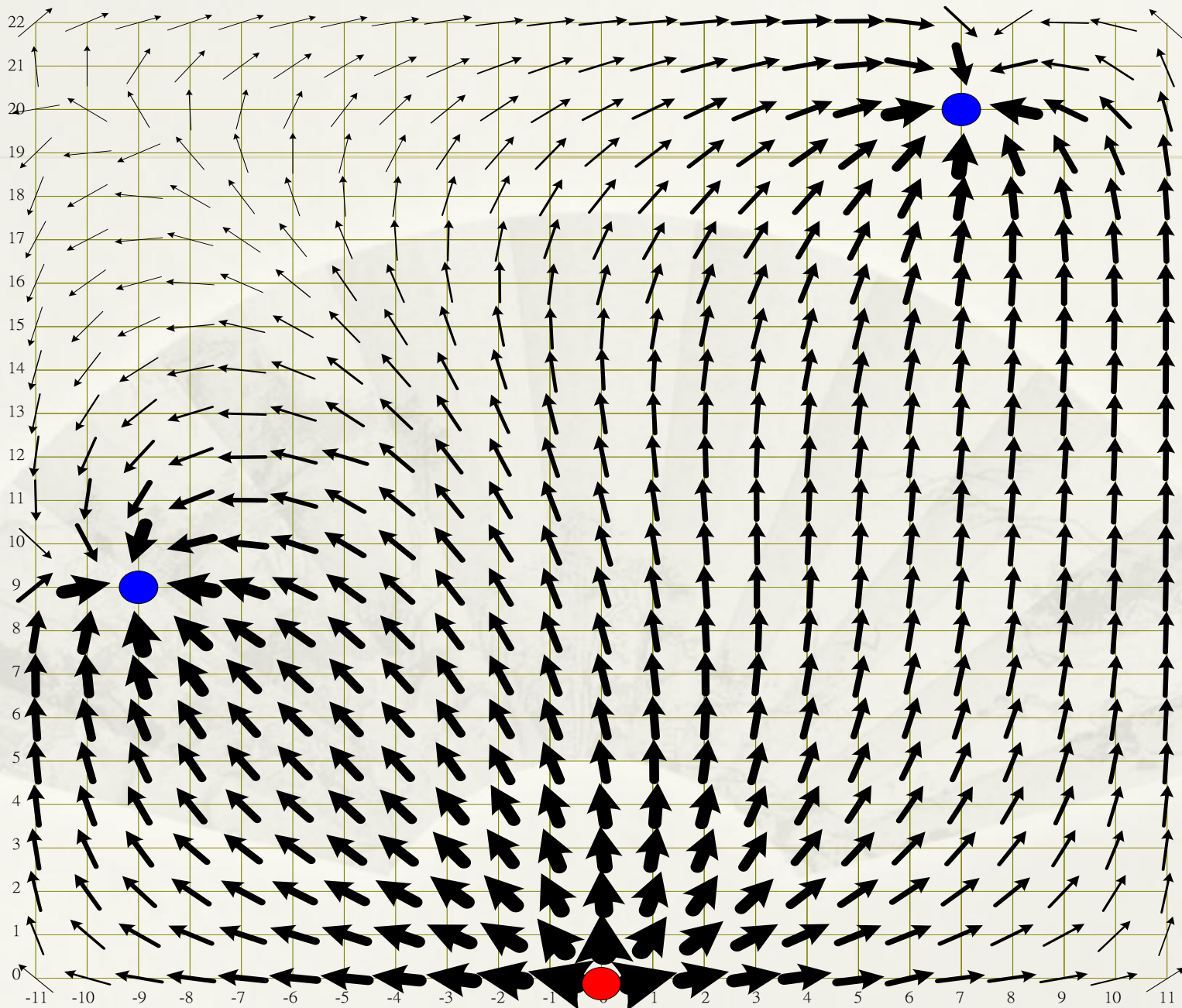




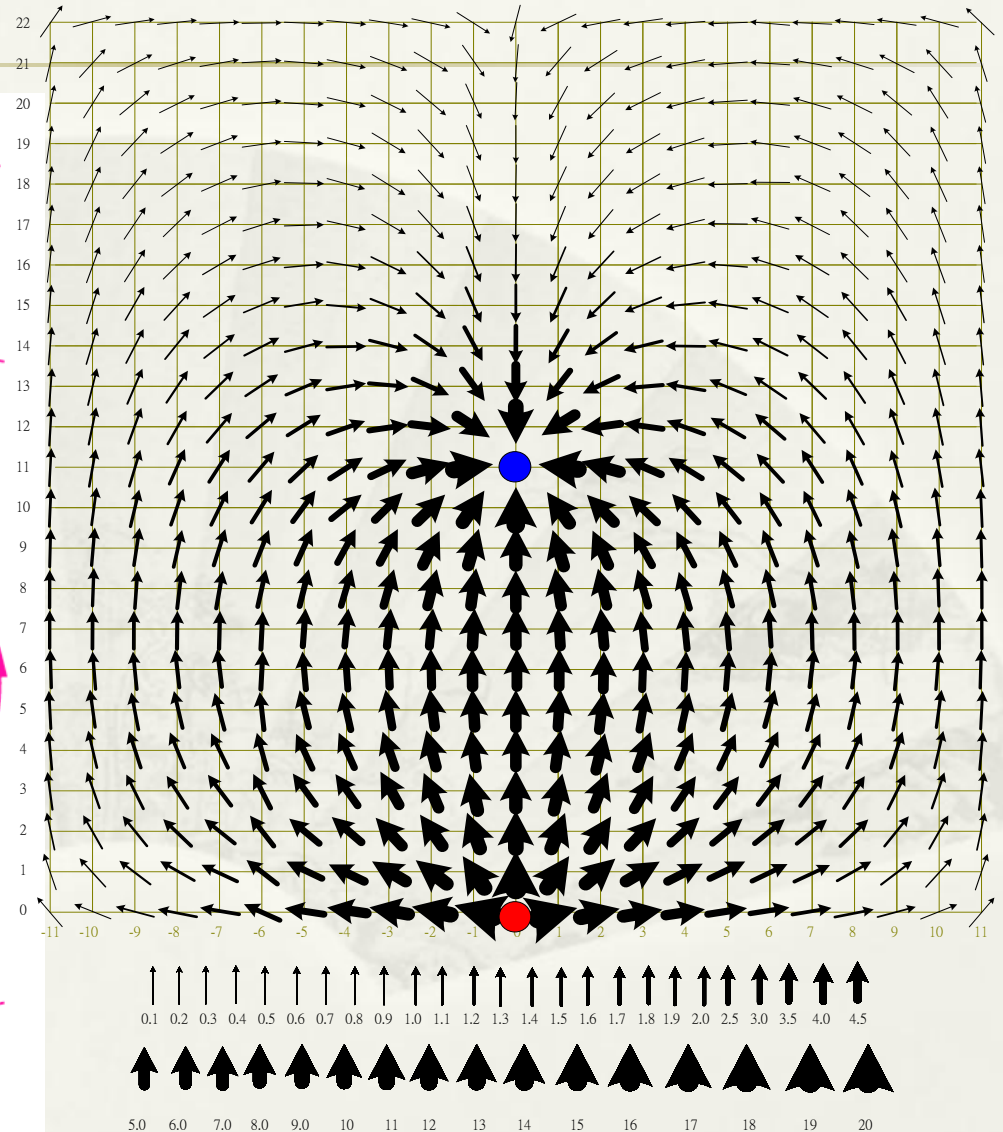
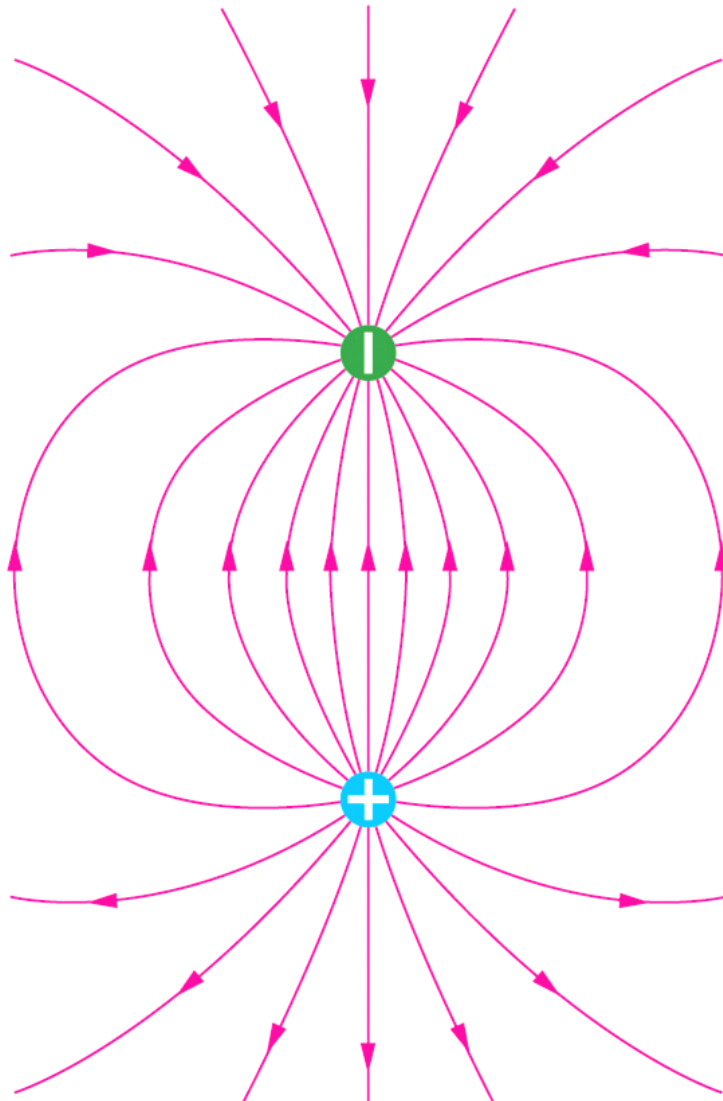








正、負兩點電荷所建立的靜電場



以距離平方反比關係 分析

$$E = E_x + E_y$$

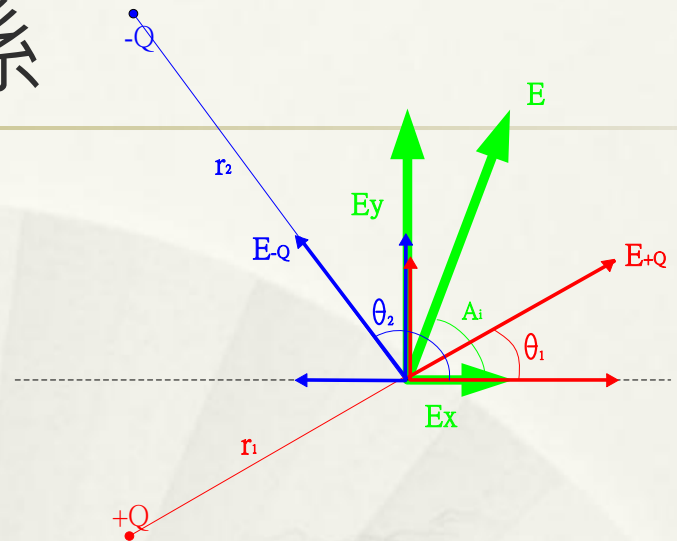
$$\text{其中 } E_x = E_{+Q} \cos \theta_1 + E_{-Q} \cos \theta_2$$

$$E_y = E_{+Q} \sin \theta_1 + E_{-Q} \sin \theta_2$$

$$\text{設 } +Q \text{ 點電荷在空間中建立的電場爲 } E_{+Q} = +\frac{kQ}{r^2} = +\frac{C}{r^2} \quad (C \text{ 爲一常數})$$

$$-Q \text{ 點電荷在空間中建立的電場爲 } E_{-Q} = -\frac{kQ}{r^2} = -\frac{C}{r^2}$$

$$\text{而電場 } E \text{ 與 } X \text{ 軸之水平夾角 } A_i = \tan^{-1} \frac{E_y}{E_x}$$

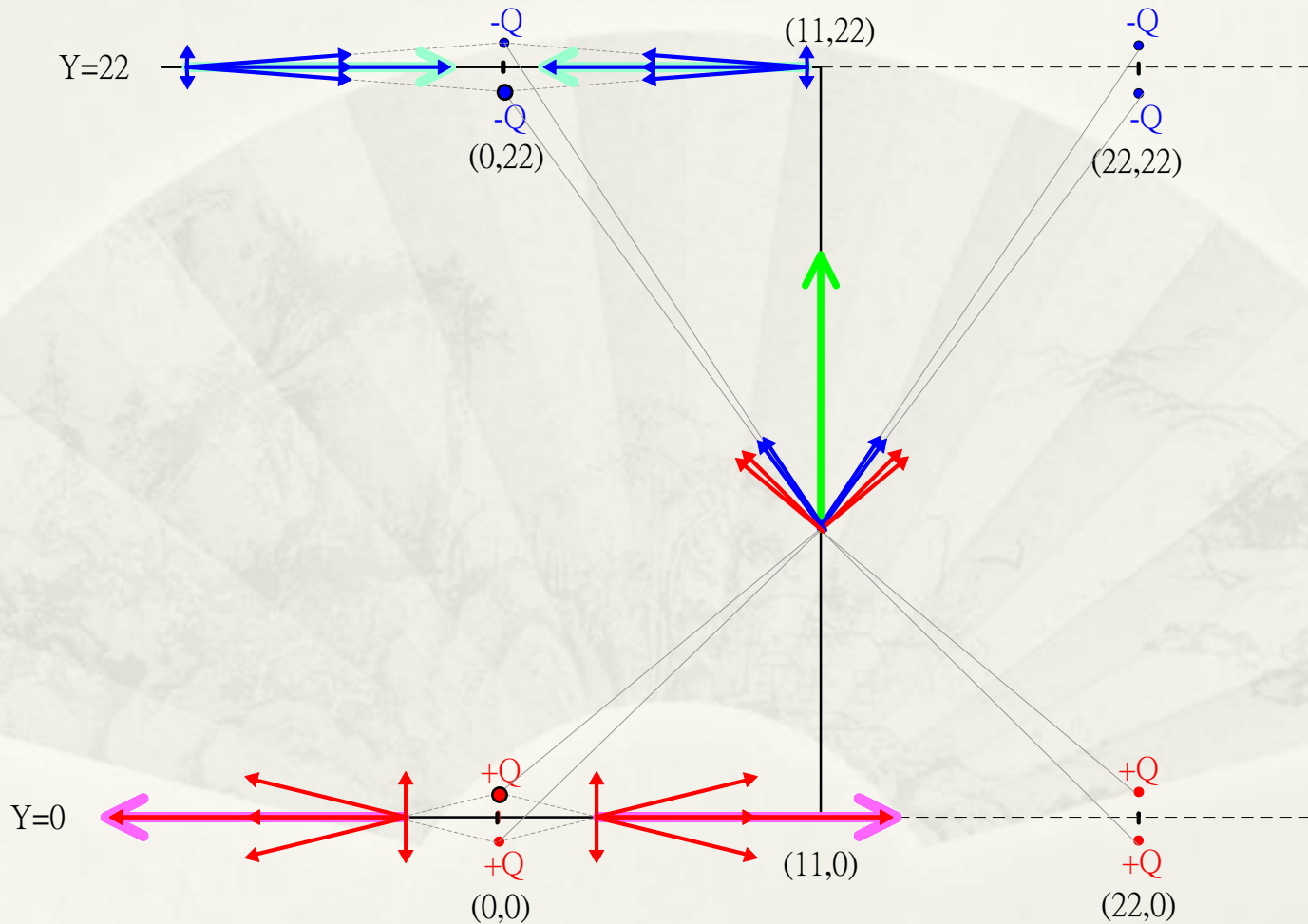


電場方向理論值與電流場方向比對

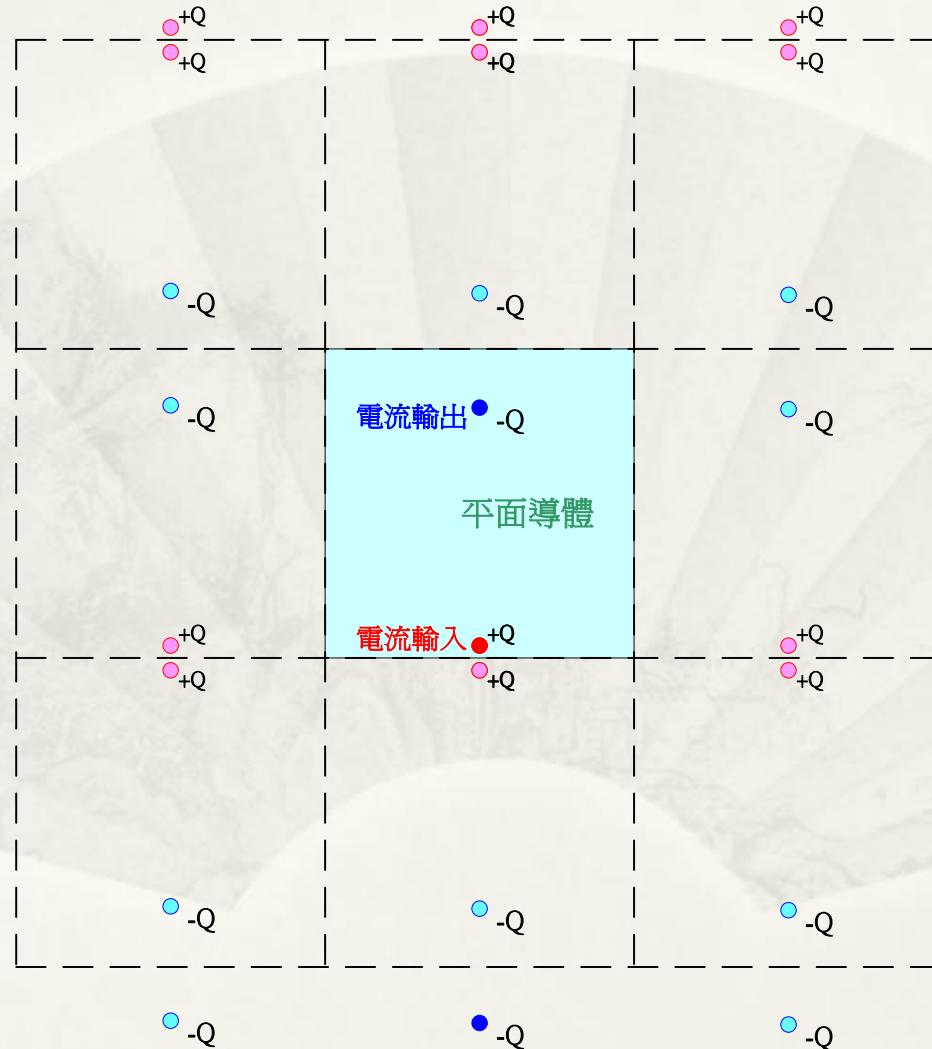
Xi	Yi	電場 Ei	夾角 Ai	電流 向量	夾角 (度)	電流 電場	角度差		Xi	Yi	電場 Ei	夾角 Ai	電流 向量	夾角 (度)	電流 電場	角度差	
-11	0	1.23	168.9	0.32	136.3	0.26	-32.6	***	-9	0	0.13	172.0	1.20	167.5	9.50	-4.5	
-11	1	1.23	162.5	0.67	107.4	0.54	-55.1	****	-9	1	0.13	164.7	1.30	144.4	10.35	-20.3	**
-11	2	1.22	155.9	1.06	100.4	0.87	-55.5	****	-9	2	0.12	157.3	1.59	129.1	12.86	-28.2	**
-11	3	1.19	149.1	1.42	97.3	1.19	-51.8	****	-9	3	0.12	149.9	1.86	117.9	15.67	-31.9	***
-11	4	1.15	142.2	1.73	95.3	1.50	-46.9	****	-9	4	0.11	142.4	2.12	111.0	18.89	-31.4	***
-11	5	1.11	135.2	1.98	94.0	1.79	-41.1	****	-9	5	0.11	135.0	2.35	104.8	22.24	-30.2	***
-11	6	1.06	128.0	2.20	92.9	2.07	-35.1	***	-9	6	0.10	127.7	2.53	100.7	25.58	-27.0	**
-11	7	1.02	120.7	2.37	91.9	2.32	-28.7	**	-9	7	0.09	120.3	2.67	97.7	28.69	-22.5	**
-11	8	0.99	113.2	2.49	91.6	2.53	-21.6	**	-9	8	0.09	112.8	2.79	96.2	31.51	-16.6	*
-11	9	0.96	105.5	2.57	91.1	2.68	-14.4	*	-9	9	0.08	105.3	2.82	93.9	33.18	-11.4	*
-11	10	0.94	97.8	2.62	90.7	2.79	-7.1		-9	10	0.08	97.7	2.86	91.8	34.59	-5.8	
-11	11	0.94	90.0	2.64	90.3	2.82	0.3		-9	11	0.08	90.0	2.92	90.3	35.61	0.3	
-11	12	0.94	82.2	2.63	89.8	2.80	7.6		-9	12	0.08	82.3	2.90	88.6	35.07	6.3	
-11	13	0.96	74.5	2.58	89.6	2.69	15.1	*	-9	13	0.08	74.7	2.85	87.0	33.62	12.2	*
-11	14	0.99	66.8	2.49	89.1	2.53	22.3	**	-9	14	0.09	67.2	2.78	85.3	31.43	18.1	*
-11	15	1.02	59.3	2.36	88.5	2.31	29.2	**	-9	15	0.09	59.7	2.66	82.2	28.58	22.5	**
-11	16	1.06	52.0	2.18	87.4	2.05	35.4	***	-9	16	0.10	52.3	2.52	79.0	25.40	26.7	**
-11	17	1.11	44.8	1.96	86.8	1.77	42.0	****	-9	17	0.11	45.0	2.33	75.3	22.03	30.4	***
-11	18	1.15	37.8	1.72	85.0	1.49	47.2	****	-9	18	0.11	37.6	2.10	69.4	18.75	31.9	***
-11	19	1.19	30.9	1.42	83.5	1.19	52.6	****	-9	19	0.12	30.1	1.85	62.6	15.60	32.5	***
-11	20	1.22	24.1	1.07	79.7	0.88	55.6	****	-9	20	0.12	22.7	1.59	50.9	12.86	28.2	**
-11	21	1.23	17.5	0.68	72.1	0.55	54.6	****	-9	21	0.13	15.3	1.32	35.1	10.47	19.8	*
-11	22	1.23	11.1	0.31	45.0	0.25	33.9	***	-9	22	0.13	8.0	1.17	12.8	9.27	4.9	
-10	0	1.51	170.5	0.71	162.1	0.47	-8.4		-8	0	0.16	173.5	1.76	170.5	10.92	-2.9	
-10	1	1.51	163.7	0.91	132.3	0.60	-31.4	***	-8	1	0.16	165.5	1.79	151.6	11.10	-14.0	*
-10	2	1.49	156.7	1.23	118.0	0.83	-38.7	***	-8	2	0.16	157.5	2.00	137.0	12.80	-20.5	**
-10	3	1.44	149.6	1.55	109.6	1.07	-40.0	****	-8	3	0.15	149.6	2.18	124.9	14.78	-24.7	**
-10	4	1.38	142.5	1.84	104.5	1.33	-38.0	***	-8	4	0.14	141.9	2.39	116.6	17.36	-25.3	**
-10	5	1.32	135.3	2.08	100.5	1.58	-34.8	***	-8	5	0.13	134.3	2.56	109.1	20.10	-25.2	**
-10	6	1.25	128.0	2.29	97.5	1.83	-30.5	***	-8	6	0.12	126.9	2.71	103.9	23.02	-23.0	**
-10	7	1.19	120.6	2.44	95.4	2.05	-25.2	**	-8	7	0.11	119.5	2.82	99.8	25.83	-19.7	*
-10	8	1.14	113.1	2.56	94.7	2.24	-18.4	*	-8	8	0.10	112.2	2.91	96.9	28.42	-15.3	*
-10	9	1.10	105.5	2.63	92.8	2.39	-12.7	*	-8	9	0.10	104.8	2.97	94.8	30.46	-10.0	*
-10	10	1.08	97.8	2.68	91.5	2.48	-6.3		-8	10	0.09	97.4	3.00	92.1	31.75	-5.3	
-10	11	1.07	90.0	2.69	90.5	2.51	0.5		-8	11	0.09	90.0	3.02	90.2	32.28	0.2	
-10	12	1.08	82.2	2.67	89.4	2.47	7.1		-8	12	0.09	82.6	3.01	87.9	31.86	5.3	
-10	13	1.10	74.5	2.62	88.3	2.38	13.7	*	-8	13	0.10	75.2	2.98	86.0	30.53	10.8	*
-10	14	1.14	66.9	2.53	87.1	2.22	20.2	**	-8	14	0.10	67.8	2.91	83.5	28.40	15.7	*
-10	15	1.19	59.4	2.41	85.2	2.02	25.8	**	-8	15	0.11	60.5	2.81	79.8	25.77	19.3	*
-10	16	1.25	52.0	2.25	82.6	1.80	30.6	***	-8	16	0.12	53.1	2.69	75.6	22.90	22.5	**
-10	17	1.32	44.7	2.05	80.4	1.55	35.7	***	-8	17	0.13	45.7	2.54	70.9	19.93	25.3	**
-10	18	1.38	37.5	1.81	76.0	1.31	38.5	***	-8	18	0.14	38.1	2.39	63.6	17.33	25.6	**
-10	19	1.44	30.4	1.53	71.3	1.06	41.0	****	-8	19	0.15	30.4	2.18	55.7	14.76	25.3	**
-10	20	1.49	23.3	1.23	62.0	0.83	38.7	***	-8	20	0.16	22.5	2.00	43.0	12.80	20.5	**
-10	21	1.51	16.3	0.93	47.2	0.61	30.9	***	-8	21	0.16	14.5	1.79	28.3	11.15	13.8	*
-10	22	1.51	9.5	0.70	19.2	0.46	9.7		-8	22	0.16	6.5	1.71	9.7	10.61	3.2	

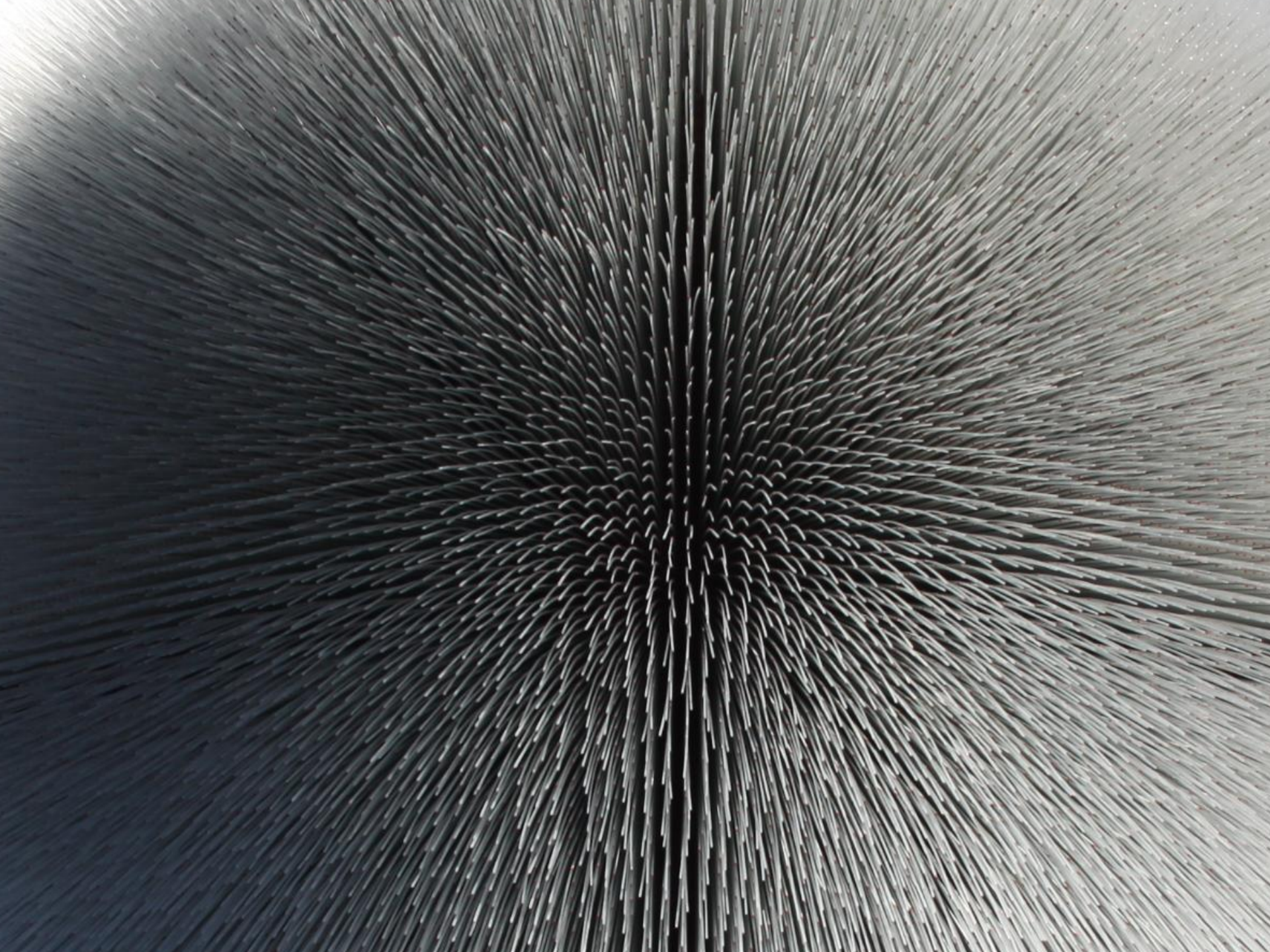
誤差很大，尤其邊界附近角度差很大

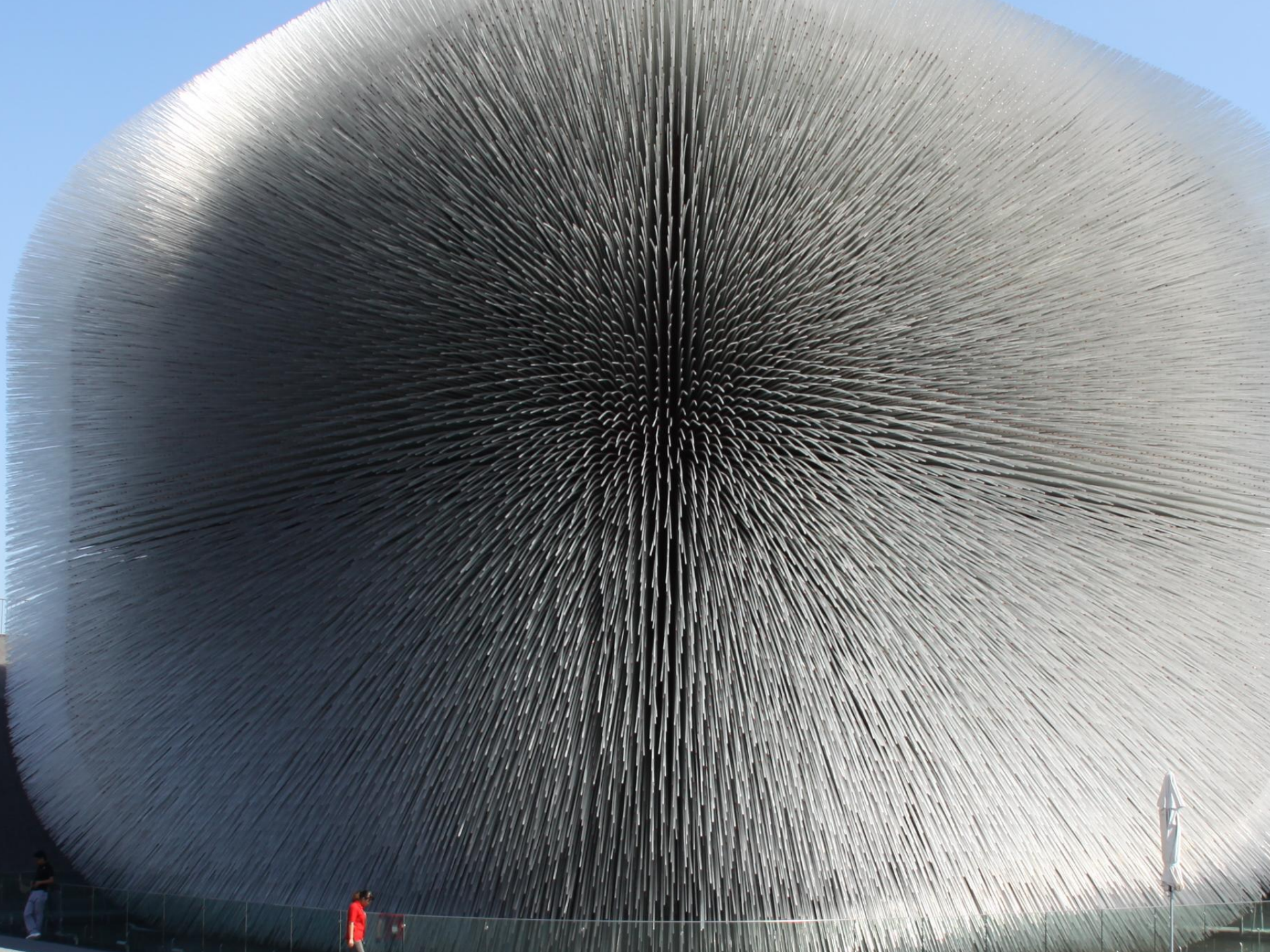
利用類似『鏡面』效果來滿足邊界 電流場的方向問題

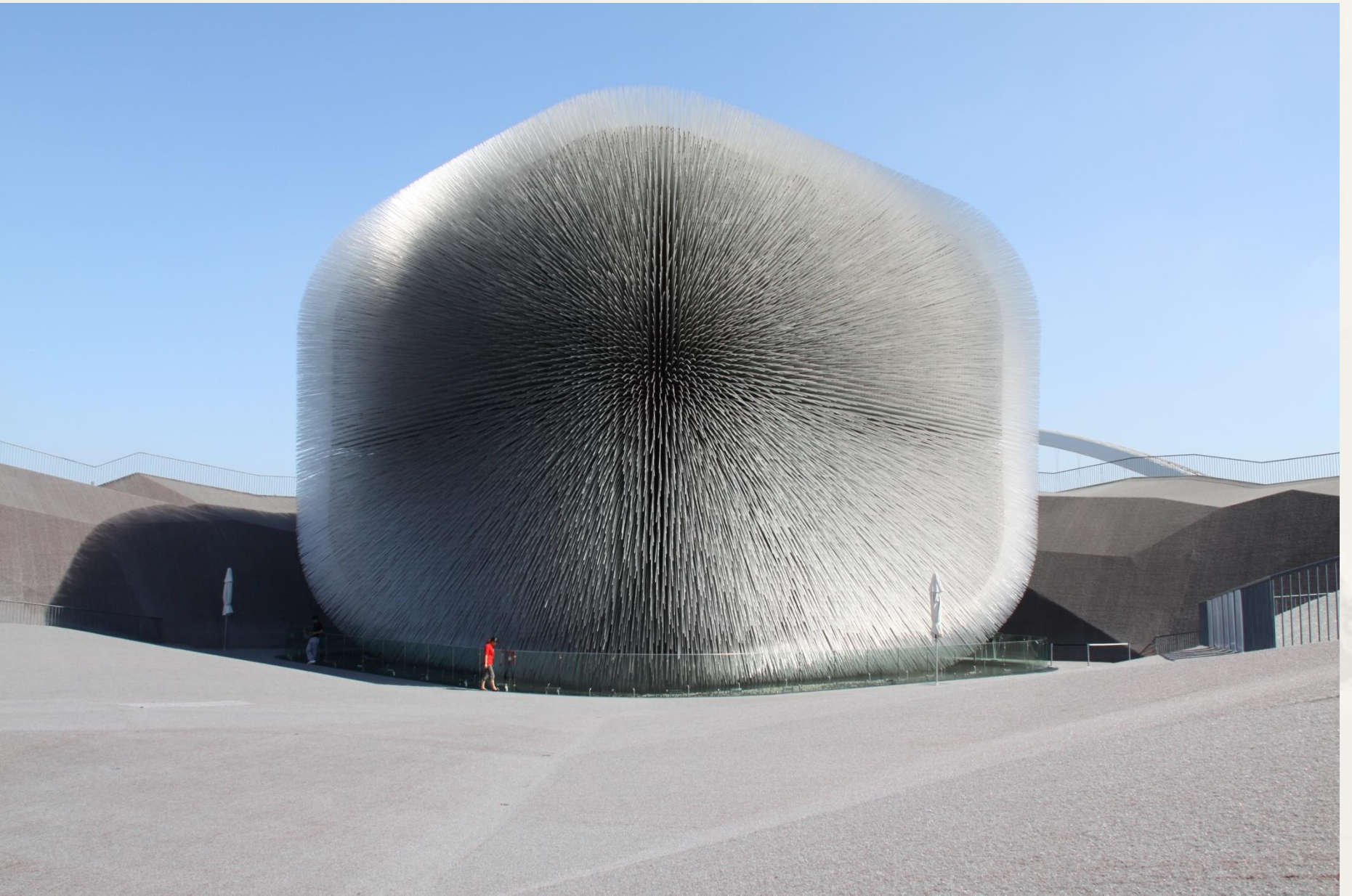


利用類似『鏡面』效果來滿足邊界 電流場的方向問題



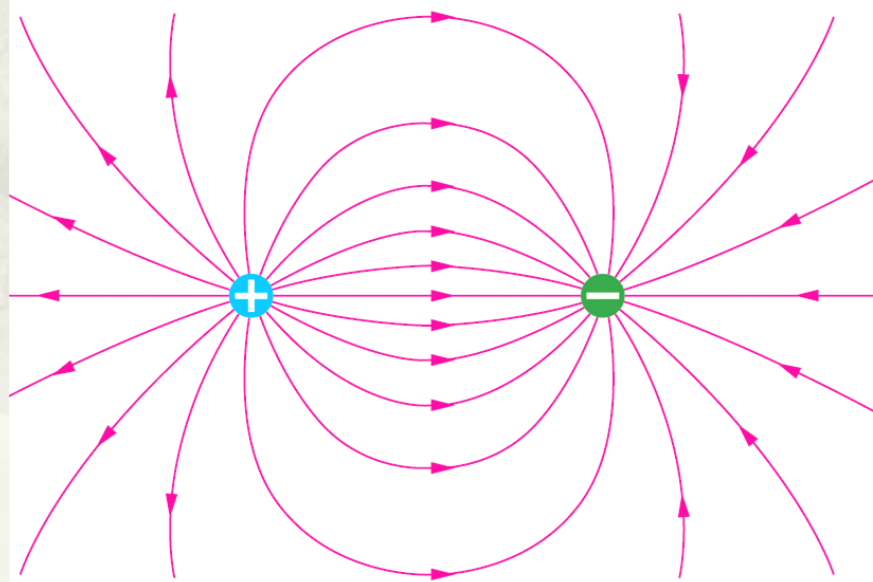
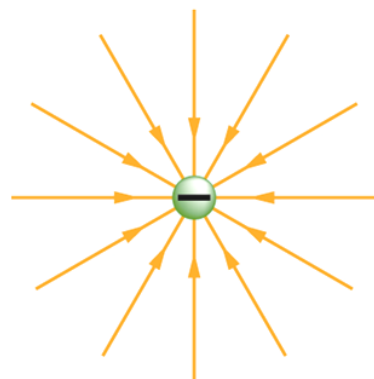
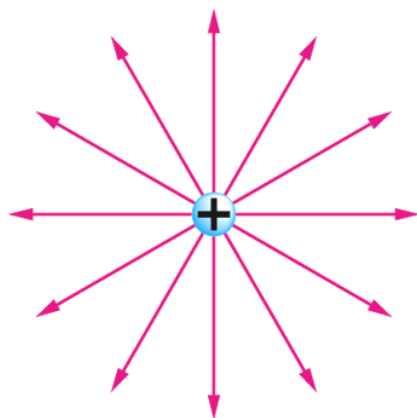






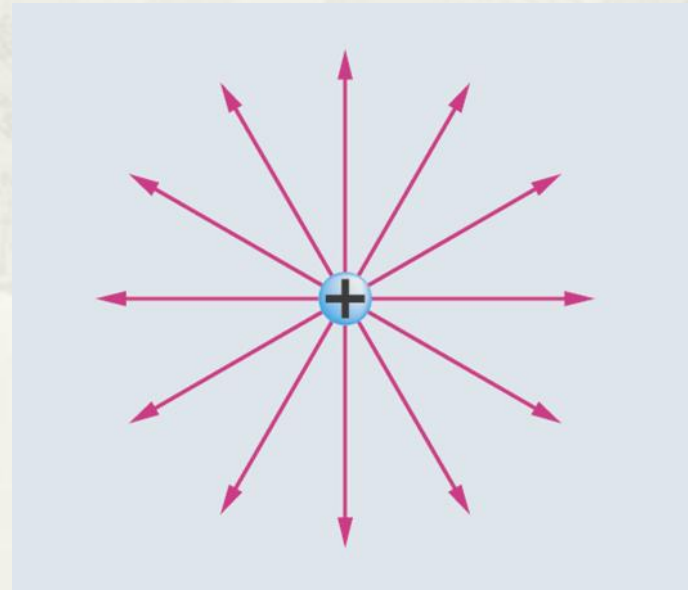
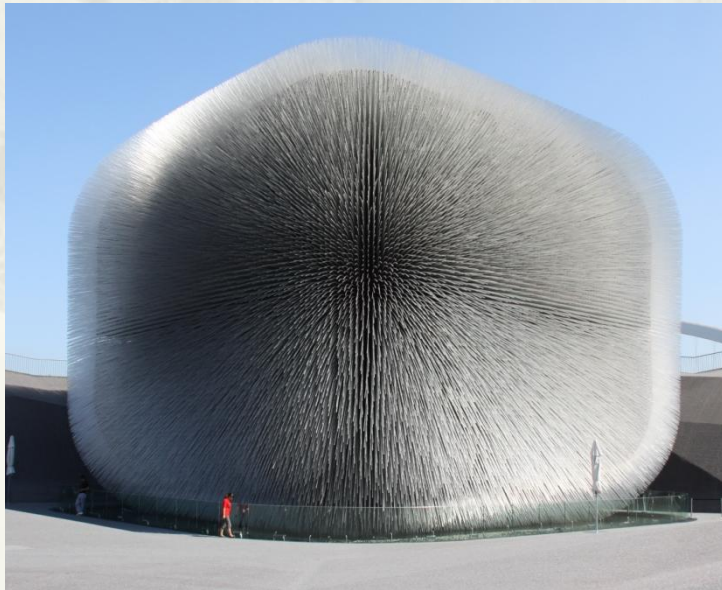


正、負兩點電荷所建立的靜電場




修正平面電場

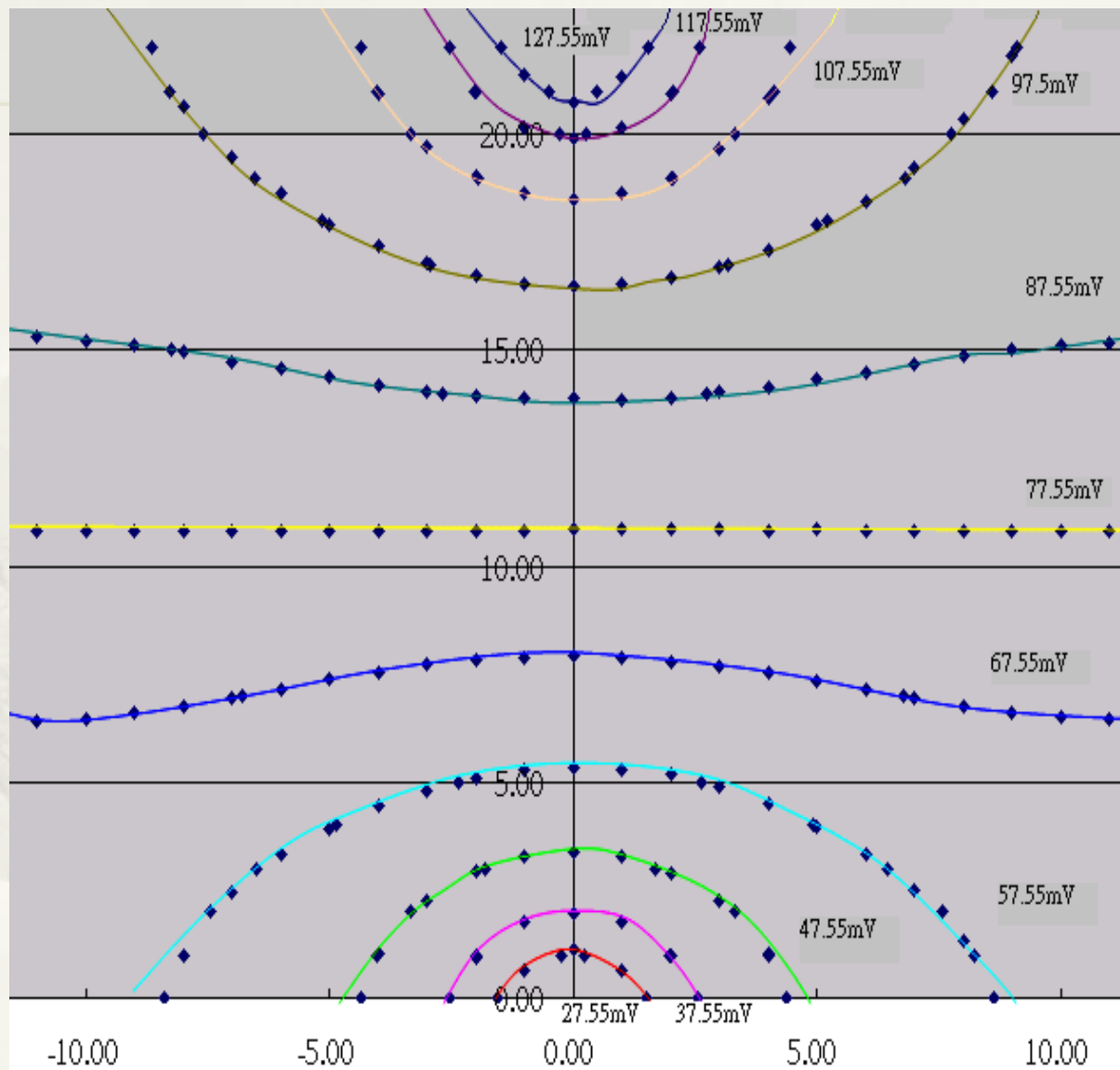
- * 將電場修正為與距離一次方成反比帶入比對。
- * 結果，電場方向與電流場方向幾乎一致，且電流強度與電場強度比值幾乎為一定值。

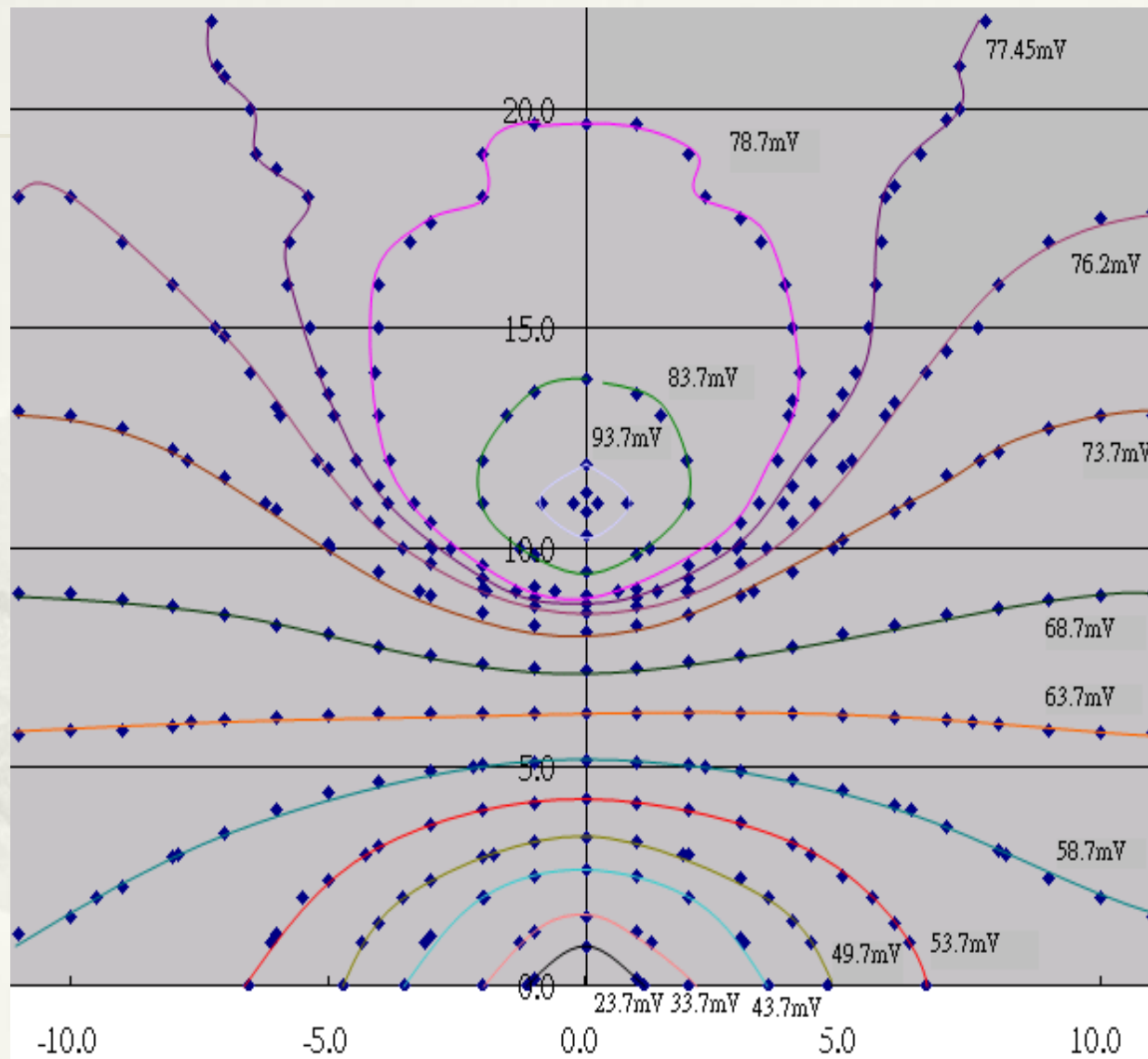


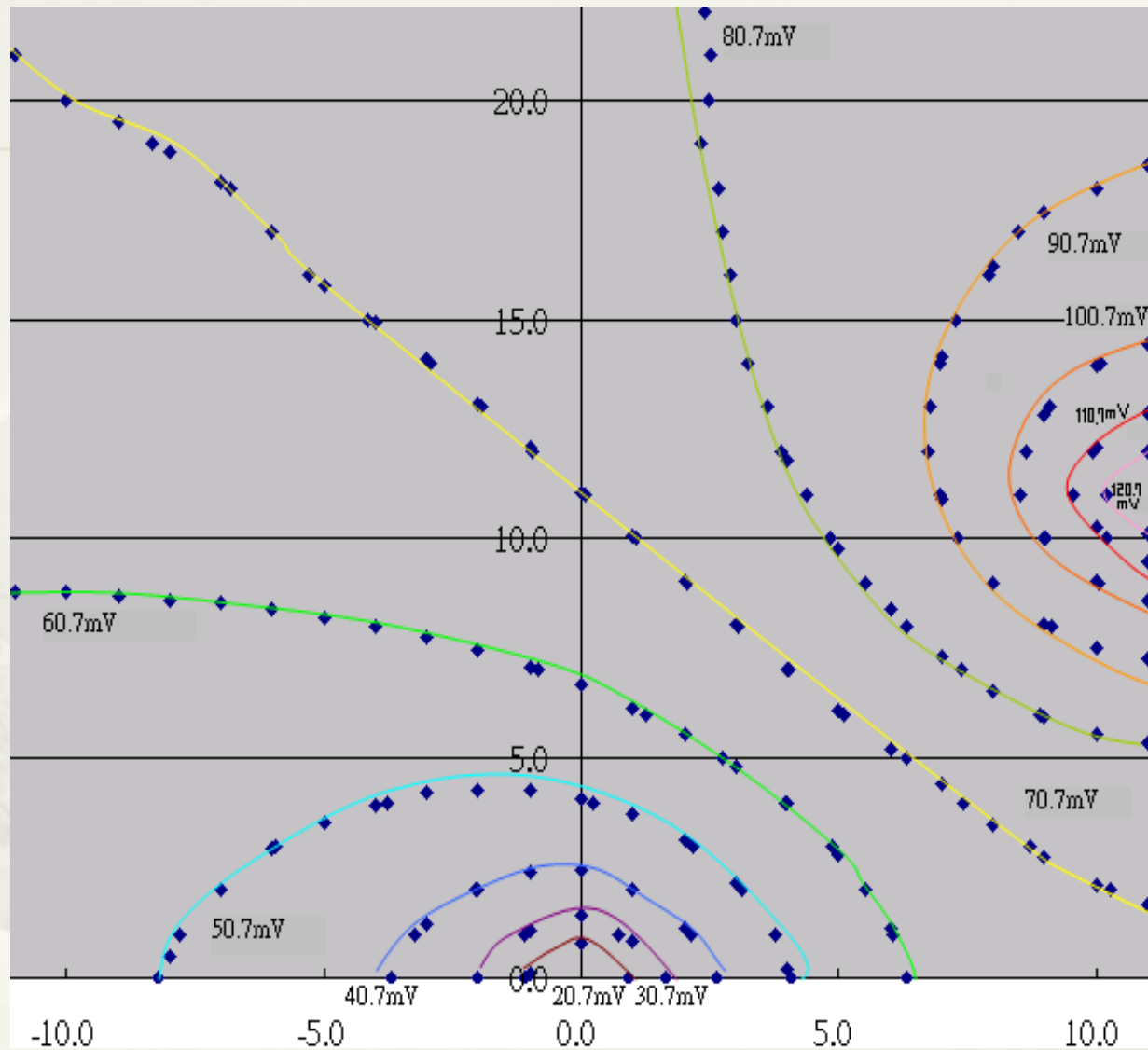
高中物理等電位線實驗

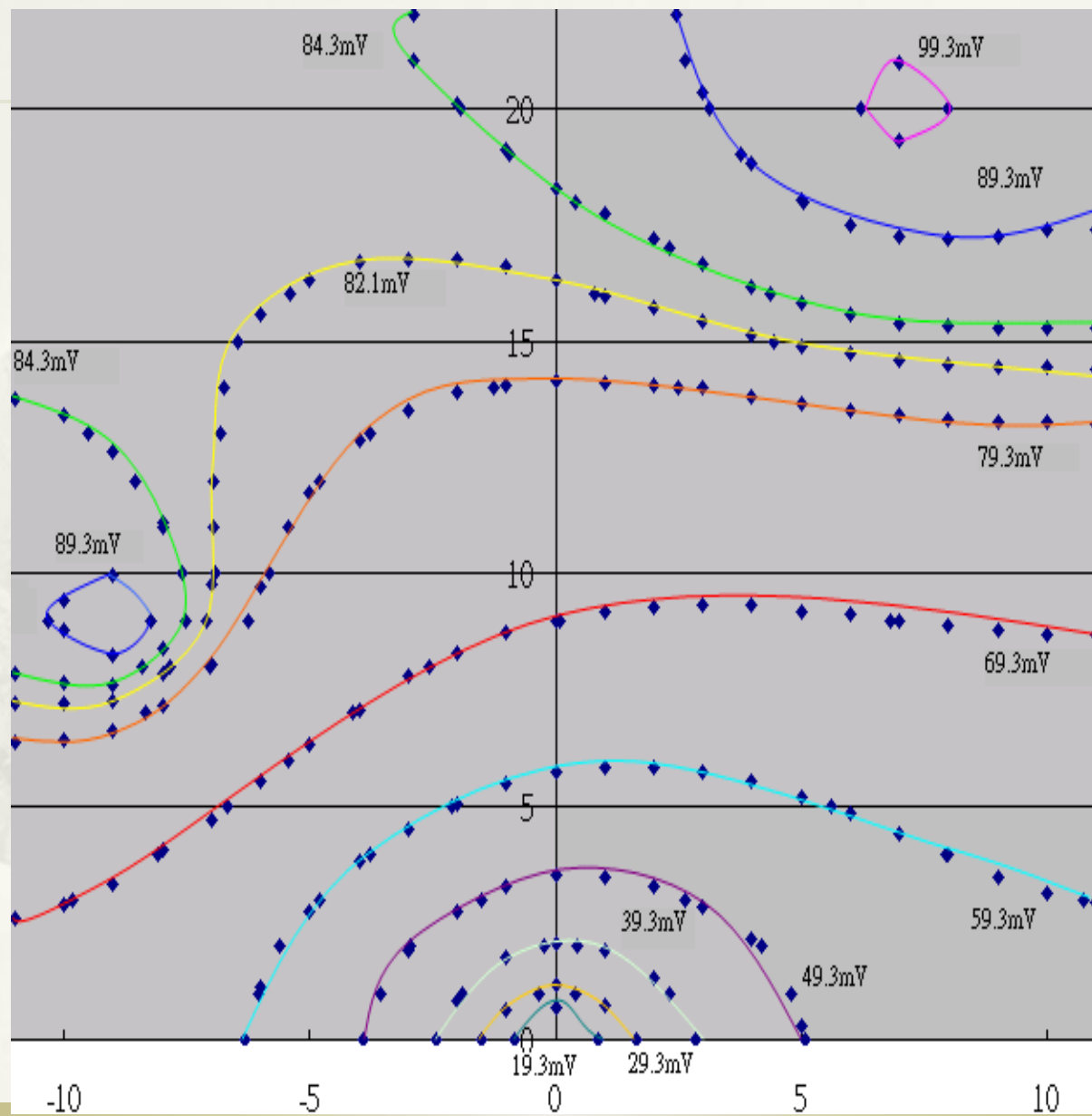
實驗做了嗎？

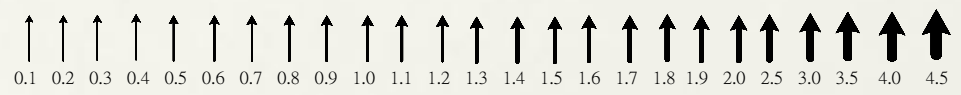
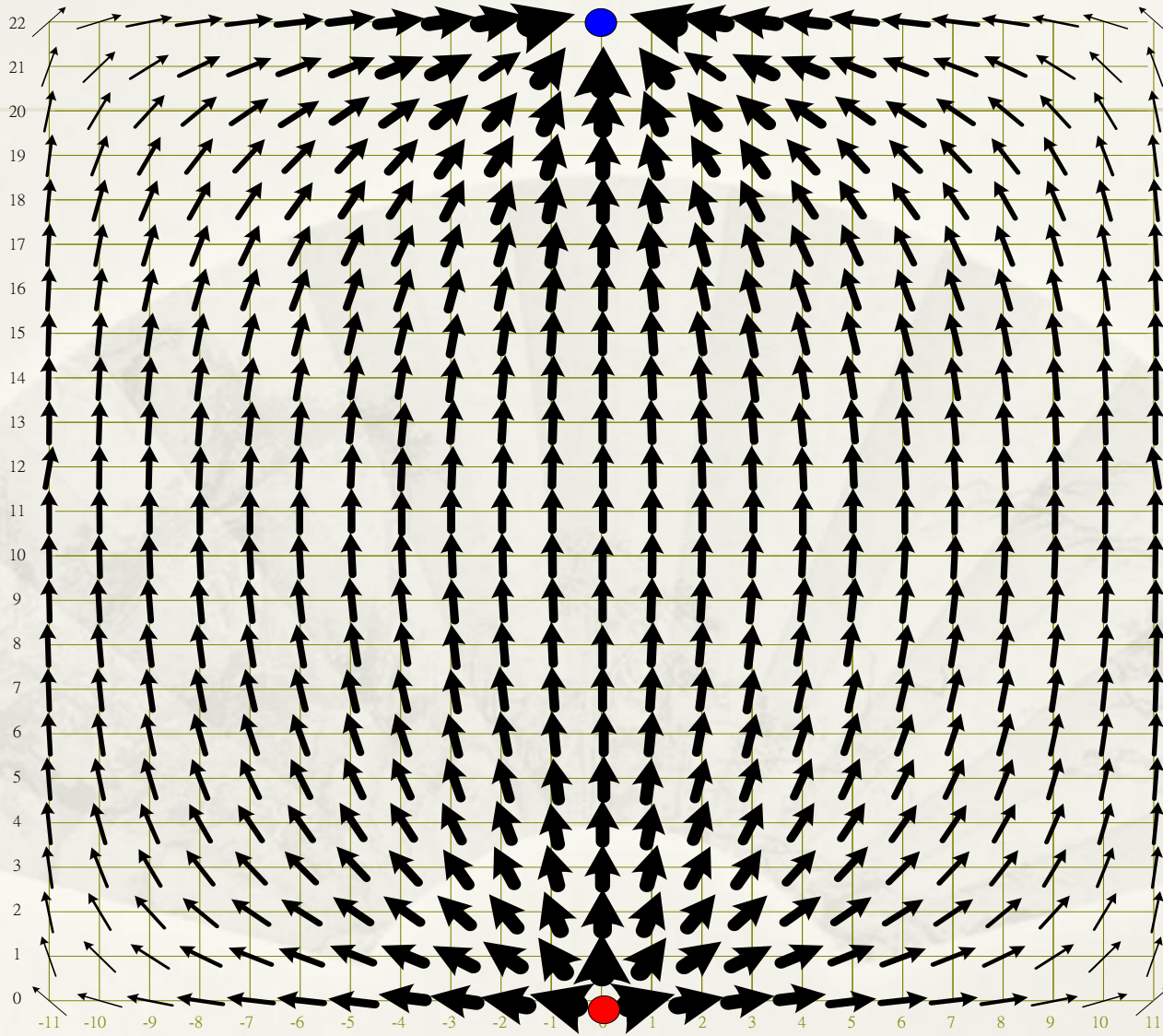


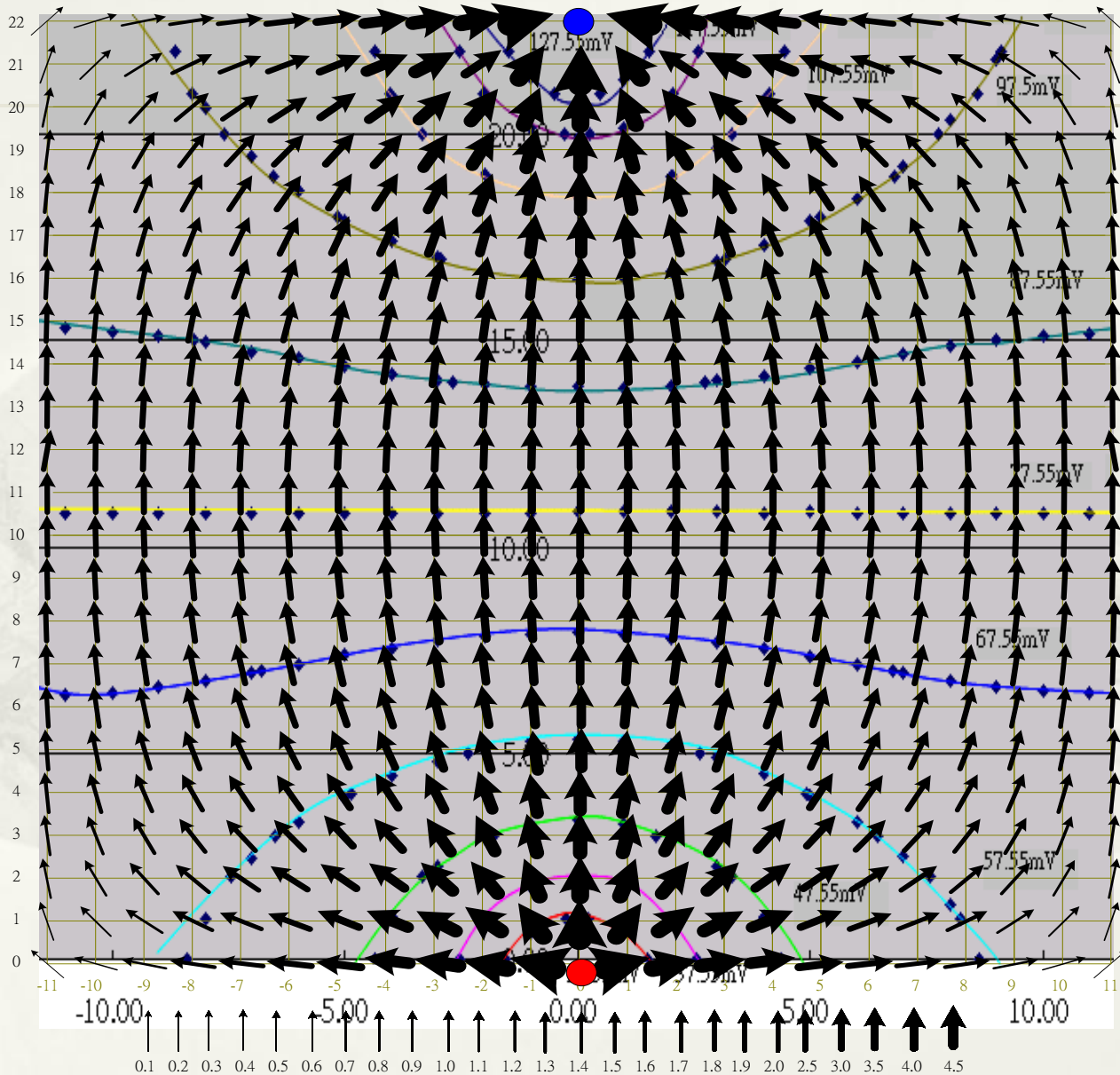


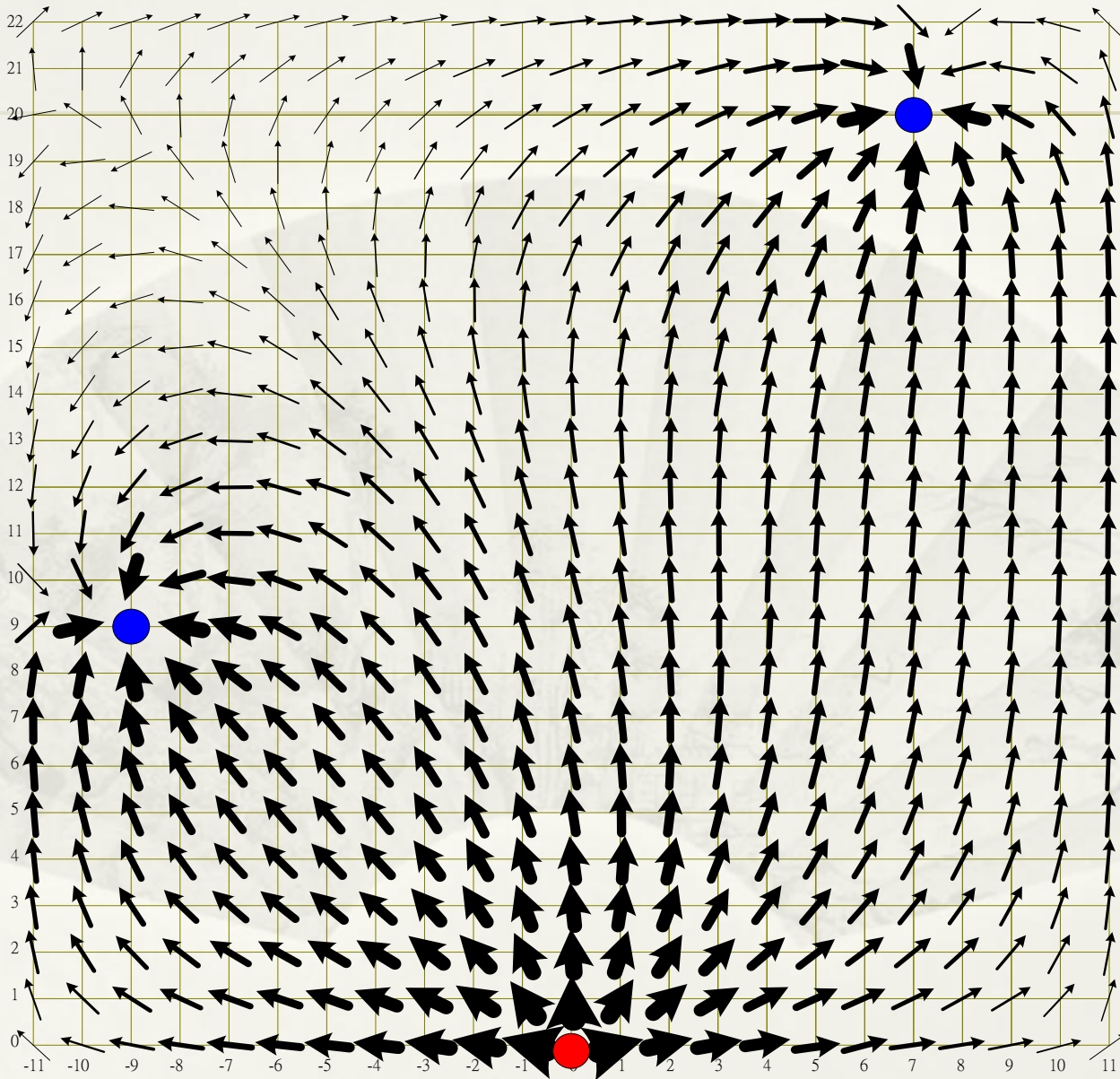


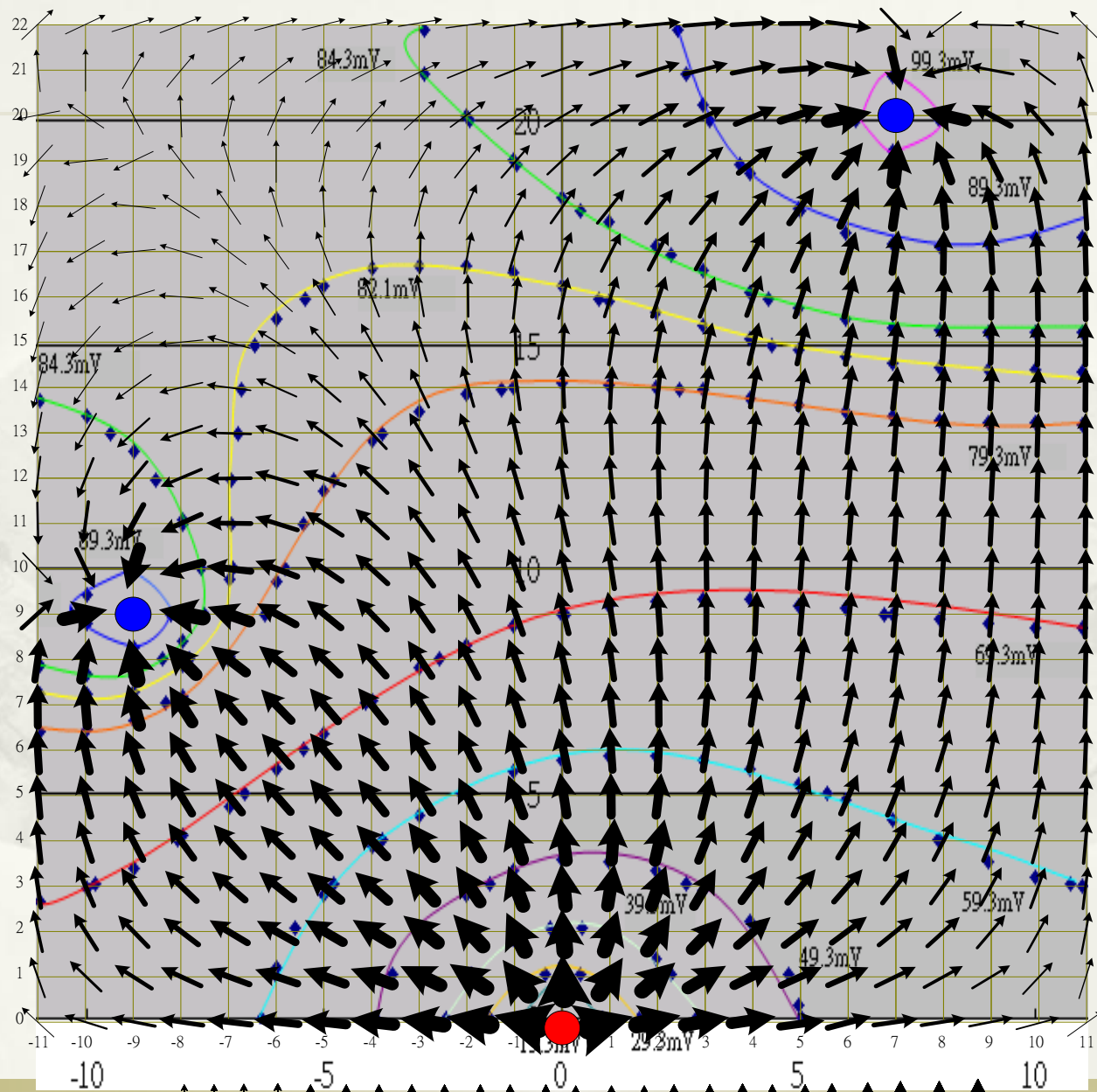






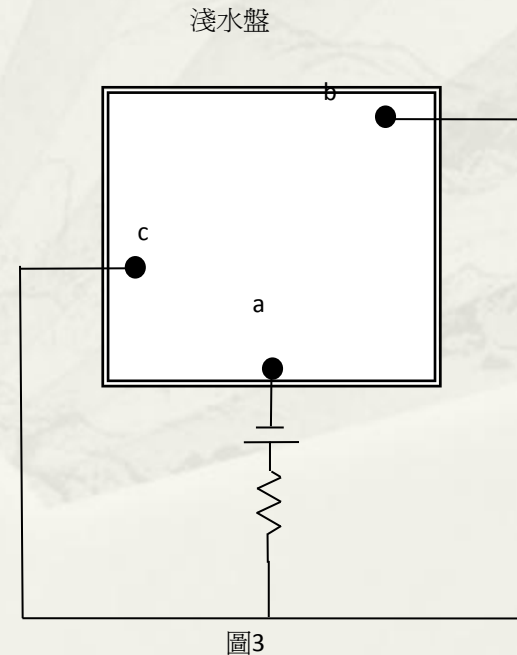






3-4 為題組

在「等電位線與電場」實驗中，筱雯使用的電路接法如圖3所示，其中a、b、c為電極。筱雯以三用電表來測量電位，先將負極探針固定插在a電極上，再以正極探針插入淺水盤中，尋找相同電位差的點，將這些點連成線便可得到一條等電位線，依此方法她繪出數條等電位線，如圖4中之細實線所示。回答3-4題。



3. 圖4中，甲~戊五條粗黑實線，哪一條描繪出最接近正確的電力線？(A) 甲 (B) 乙 (C) 丙 (D) 丁 (E) 戊

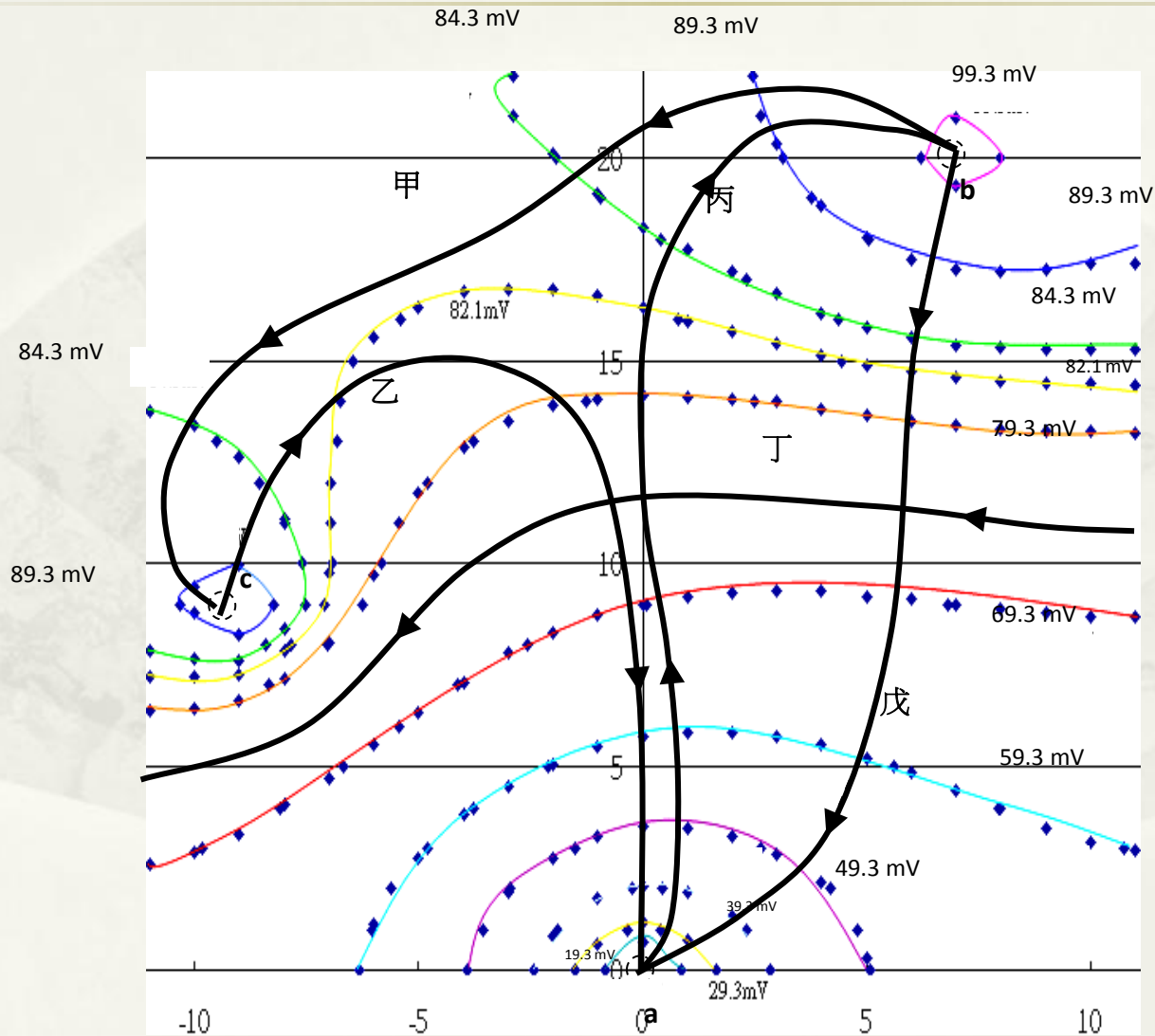
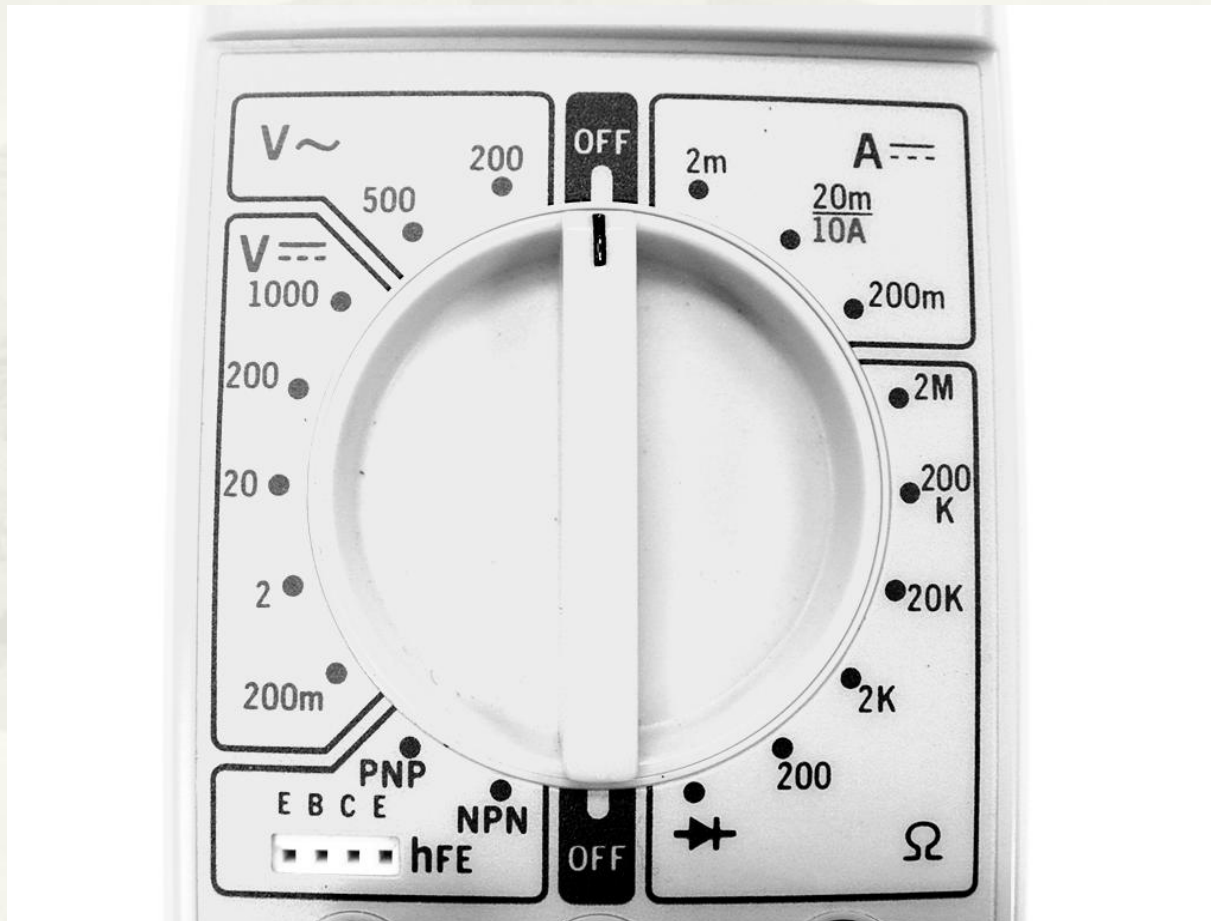


圖4

4. 此實驗中，筱雯應該把三用電表的功能選擇鈕旋轉到哪一位置，能測得較精確的測量結果？



測量鋁片的等電位線

